

# Analog Engineer's

## Pocket Reference

Art Kay and Tim Green, Editors

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TEXAS INSTRUMENTS



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# Analog Engineer's Pocket Reference

Fifth Edition

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## Message from the editors:

This pocket reference is intended as a valuable quick guide for often used board- and system-level design formulae. This collection of formulae is based on a combined 50 years of analog board- and system-level expertise. Much of the material herein was referred to over the years via a folder stuffed full of printouts. Those worn pages have been organized and the information is now available via this guide in a bound and hard-to-lose format!

Here is a brief overview of the key areas included:

- Key constants and conversions
- Discrete components
- AC and DC analog equations
- Op amp basic configurations
- OP amp bandwidth and stability
- Overview of sensors
- PCB trace R, L, C
- Wire L, R, C
- Binary, hex and decimal formats
- A/D and D/A conversions

We hope you find this collection of formulae as useful as we have. Please send any comments and/or ideas you have for the next edition of the *Analog Engineer's Pocket Reference* to

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## Additional resources to explore:

### TI Precision Labs

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- On-demand courses and tutorials ranging from introductory to advanced concepts that focus on application-specific problem solving
- Hands-on labs and evaluation modules (EVM) available
  - TIPL Op Amps experimentation platform, [ti.com/TIPL-amp-evm](http://ti.com/TIPL-amp-evm)
  - TIPL SAR ADC experimentation platform, [ti.com/TIPL-adc-evm](http://ti.com/TIPL-adc-evm)

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Table 1: Physical constants

| Constant                       | Symbol       | Value                                  | Units                            |
|--------------------------------|--------------|----------------------------------------|----------------------------------|
| Speed of light in a vacuum     | $c$          | $2.997\,924\,58 \times 10^8$           | m/s                              |
| Permittivity of vacuum         | $\epsilon_0$ | $8.854\,187\,817\,620 \times 10^{-12}$ | F/m                              |
| Permeability of free space     | $\mu_0$      | $1.256\,637\,0614 \times 10^{-6}$      | H/m                              |
| Planck's constant              | $h$          | $6.626\,069\,57 \times 10^{-34}$       | J•s                              |
| Boltzmann's constant           | $k$          | $1.380\,648\,8 \times 10^{-23}$        | J/K                              |
| Faraday's constant             | $F$          | $9.648\,533\,99 \times 10^4$           | C/mol                            |
| Avogadro's constant            | $N_A$        | $6.022\,141\,29 \times 10^{23}$        | 1/mol                            |
| Unified atomic mass unit       | $m_u$        | $1.660\,538\,921 \times 10^{-27}$      | kg                               |
| Electronic charge              | $q$          | $1.602\,176\,565 \times 10^{-19}$      | C                                |
| Rest mass of electron          | $m_e$        | $9.109\,382\,15 \times 10^{-31}$       | kg                               |
| Mass of proton                 | $m_p$        | $1.672\,621\,777 \times 10^{-27}$      | kg                               |
| Gravitational constant         | $G$          | $6.673\,84 \times 10^{-11}$            | Nm <sup>2</sup> /kg <sup>2</sup> |
| Standard gravity               | $g_n$        | 9.806 65                               | m/s <sup>2</sup>                 |
| Ice point                      | $T_{ice}$    | 273.15                                 | K                                |
| Maximum density of water       | $\rho$       | $1.00 \times 10^3$                     | kg/m <sup>3</sup>                |
| Density of mercury (0°C)       | $\rho_{Hg}$  | $1.362\,8 \times 10^4$                 | kg/m <sup>3</sup>                |
| Gas constant                   | $R$          | 8.314 462 1                            | J/(K•mol)                        |
| Speed of sound in air (at 0°C) | $c_{air}$    | $3.312 \times 10^2$                    | m/s                              |

Table 2: Standard decimal prefixes

| Multiplier | Prefix | Abbreviation |
|------------|--------|--------------|
| $10^{12}$  | tera   | T            |
| $10^9$     | giga   | G            |
| $10^6$     | mega   | M            |
| $10^3$     | kilo   | k            |
| $10^{-3}$  | milli  | m            |
| $10^{-6}$  | micro  | $\mu$        |
| $10^{-9}$  | nano   | n            |
| $10^{-12}$ | pico   | p            |
| $10^{-15}$ | femto  | f            |
| $10^{-18}$ | atto   | a            |

Table 3: Imperial to metric conversions

| Unit         | Symbol        | Equivalent                                         | Unit               | Symbol        |
|--------------|---------------|----------------------------------------------------|--------------------|---------------|
| inches       | in            | 25.4 mm/in                                         | millimeter         | mm            |
| mil          | mil           | 0.0254 mm/mil                                      | millimeter         | mm            |
| feet         | ft            | 0.3048 m/ft                                        | meters             | m             |
| yards        | yd            | 0.9144 m/yd                                        | meters             | m             |
| miles        | mi            | 1.6093 km/mi                                       | kilometers         | km            |
| circular mil | cir mil       | $5.067 \times 10^{-4} \text{ mm}^2/\text{cir mil}$ | square millimeters | $\text{mm}^2$ |
| square yards | $\text{yd}^2$ | $0.8361 \text{ m}^2$                               | square meters      | $\text{m}^2$  |
| pints        | pt            | 0.5682 L/pt                                        | liters             | L             |
| ounces       | oz            | 28.35 g/oz                                         | grams              | g             |
| pounds       | lb            | 0.4536 kg/lb                                       | kilograms          | kg            |
| calories     | cal           | 4.184 J/cal                                        | joules             | J             |
| horsepower   | hp            | 745.7 W/hp                                         | watts              | W             |

Table 4: Metric to imperial conversions

| Unit               | Symbol        | Conversion                                 | Unit         | Symbol        |
|--------------------|---------------|--------------------------------------------|--------------|---------------|
| millimeter         | mm            | 0.0394 in/mm                               | inch         | in            |
| millimeter         | mm            | 39.4 mil/mm                                | mil          | mil           |
| meters             | m             | 3.2808 ft/m                                | feet         | ft            |
| meters             | m             | 1.0936 yd/m                                | yard         | yd            |
| kilometers         | km            | 0.6214 mi/km                               | miles        | mi            |
| square millimeters | $\text{mm}^2$ | $1974 \text{ cir mil}/\text{mm}^2$         | circular mil | cir mil       |
| square meters      | $\text{m}^2$  | $1.1960 \text{ yd}^2/\text{m}^2$           | square yards | $\text{yd}^2$ |
| liters             | L             | 1.7600 pt/L                                | pints        | pt            |
| grams              | g             | 0.0353 oz/g                                | ounces       | oz            |
| kilograms          | kg            | 2.2046 lb/kg                               | pounds       | lb            |
| joules             | J             | 0.239 cal/J                                | calories     | cal           |
| watts              | W             | $1.341 \times 10^{-3} \text{ hp}/\text{W}$ | horsepower   | hp            |

Example

Convert 10 mm to mil.

Answer

$10 \text{ mm} \times 39.4 \frac{\text{mil}}{\text{mm}} = 394 \text{ mil}$

Table 5: Temperature conversions

|                                                          |                       |
|----------------------------------------------------------|-----------------------|
| $^{\circ}\text{C} = \frac{5}{9} (^{\circ}\text{F} - 32)$ | Fahrenheit to Celsius |
| $^{\circ}\text{F} = \frac{9}{5} (^{\circ}\text{C}) + 32$ | Celsius to Fahrenheit |
| $\text{K} = ^{\circ}\text{C} + 273.15$                   | Celsius to Kelvin     |
| $^{\circ}\text{C} = \text{K} - 273.15$                   | Kelvin to Celsius     |

Table 6: Error conversions

|                                                                                                              |                                      |
|--------------------------------------------------------------------------------------------------------------|--------------------------------------|
| $\text{Error}(\%) = \frac{\text{Measured} - \text{Ideal}}{\text{Ideal}} \times 100$                          | Error in measured value              |
| $\text{Error}(\% \text{ FSR}) = \frac{\text{Measured} - \text{Ideal}}{\text{Full - scale range}} \times 100$ | Error in percent of full-scale range |
| $\% = \frac{\text{ppm}}{10^6} \times 100$                                                                    | Part per million to percent          |
| $\text{m}\% = \frac{\text{ppm}}{10^6} \times 100 \times 1000$                                                | Part per million to milli-percent    |
| $\text{ppm} = \% \times 10^4$                                                                                | Percent to part per million          |
| $\text{ppm} = \text{m}\% \times 10$                                                                          | Milli-percent to part per million    |

Example

Compute the error for a measured value of 0.12V when the ideal value is 0.1V and the range is 5V.

Answer

|                                                                                          |                         |
|------------------------------------------------------------------------------------------|-------------------------|
| $\text{Error}(\%) = \frac{0.12\text{V} - 0.1\text{V}}{0.1\text{V}} \times 100 = 20\%$    | Error in measured value |
| $\text{Error}(\% \text{ FSR}) = \frac{0.12 - 0.1\text{V}}{5\text{V}} \times 100 = 0.4\%$ | Percent FSR             |

Example

Convert 10 ppm to percent and milli-percent.

Answer

|                                                                      |                                   |
|----------------------------------------------------------------------|-----------------------------------|
| $\frac{10 \text{ ppm}}{10^6} \times 100 = 0.001\%$                   | Part per million to percent       |
| $\frac{10 \text{ ppm}}{10^6} \times 100 \times 1000 = 1 \text{ m}\%$ | Part per million to milli-percent |

**Table 7: Conversion between codes, mV, %, and ppm**

|       | Codes                                                                  | mV                                                                        | %                                                                              | ppm                                                                             |
|-------|------------------------------------------------------------------------|---------------------------------------------------------------------------|--------------------------------------------------------------------------------|---------------------------------------------------------------------------------|
| Codes | *                                                                      | $\text{Codes} \cdot \left( \frac{V_{\text{FSR}}}{2^N} \right) \cdot 1000$ | $\text{Codes} \cdot \left( \frac{1}{2^N} \right) \cdot 100$                    | $\text{Codes} \cdot \left( \frac{1}{2^N} \right) \cdot 10^6$                    |
| mV    | $\text{mV} \cdot \left( \frac{2^N}{V_{\text{FSR}} \cdot 1000} \right)$ | *                                                                         | $\text{mV} \cdot \left( \frac{1}{V_{\text{FSR}} \cdot 1000} \right) \cdot 100$ | $\text{mV} \cdot \left( \frac{1}{V_{\text{FSR}} \cdot 1000} \right) \cdot 10^6$ |
| %     | $\% \cdot \left( \frac{2^N}{100} \right)$                              | $\% \cdot \left( \frac{V_{\text{FSR}} \cdot 1000}{100} \right)$           | *                                                                              | $\% \cdot \left( \frac{10^6}{100} \right)$                                      |
| ppm   | $\text{ppm} \cdot \left( \frac{2^N}{10^6} \right)$                     | $\text{ppm} \cdot \left( \frac{V_{\text{FSR}} \cdot 1000}{10^6} \right)$  | $\text{ppm} \cdot \left( \frac{1}{10^6} \right) \cdot 100$                     | *                                                                               |

**Where**

N = resolution of ADC

$V_{\text{FSR}}$  = full scale range of ADC in voltage. Full scale range is double for a bipolar ADC compared with unipolar ADC.

Codes, %, and ppm = the equivalent value ADC codes, percentage, and parts per million

## Notes

[illegible]

# Discrete Components

- Resistor color code •
- Standard resistor values •
- Capacitance specifications •
- Capacitance type overview •
- Standard capacitance values •
- Capacitance marking and tolerance •

Discrete  
components

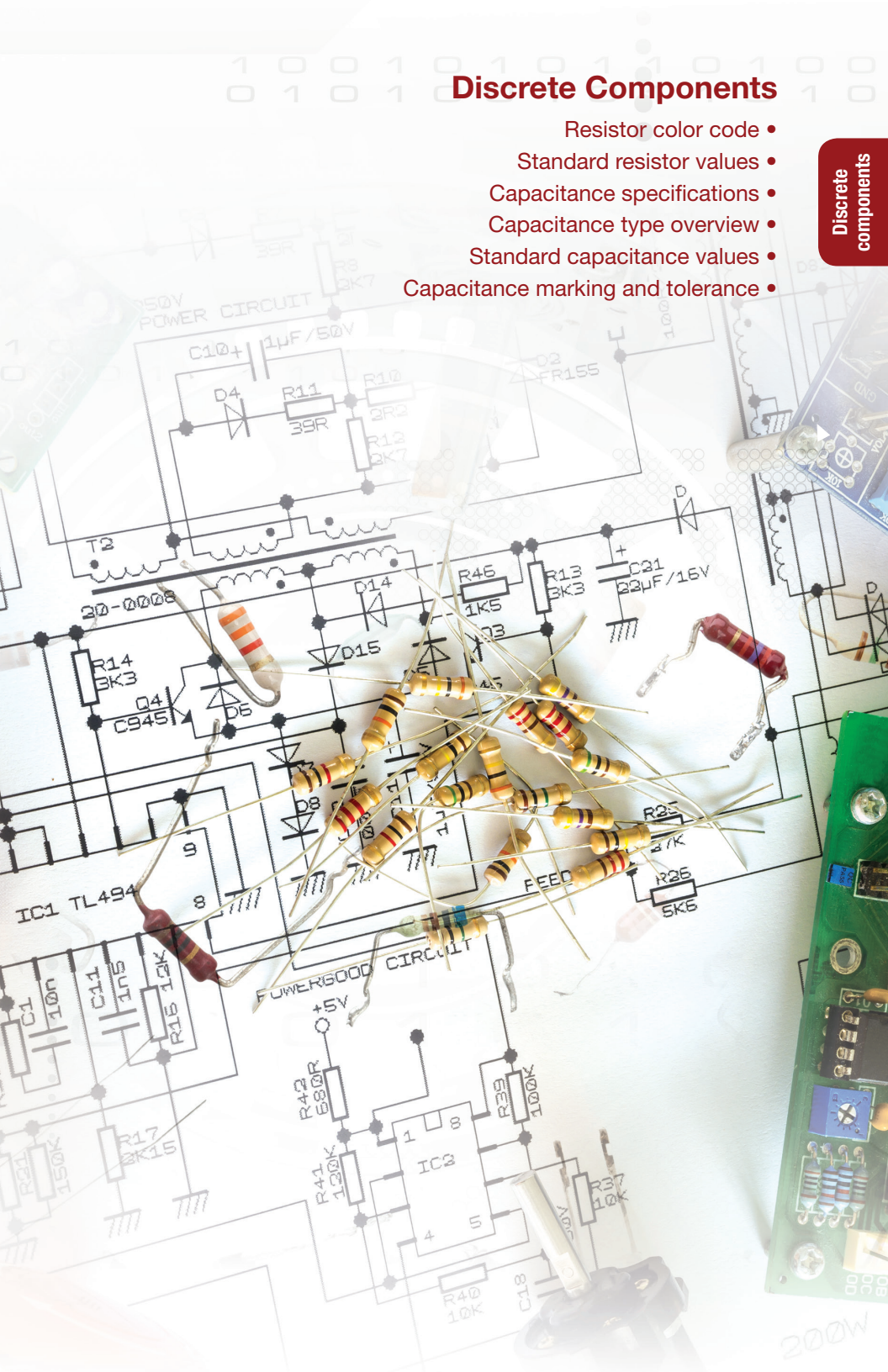


Table 8: Resistor color code

| Color   | Digit | Additional Zeros | Tolerance | Temperature Coefficient | Failure Rate |
|---------|-------|------------------|-----------|-------------------------|--------------|
| Black   | 0     | 0                |           | 250                     |              |
| Brown   | 1     | 1                | 1%        | 100                     | 1            |
| Red     | 2     | 2                | 2%        | 50                      | 0.1          |
| Orange  | 3     | 3                |           | 15                      | 0.01         |
| Yellow  | 4     | 4                |           | 25                      | 0.001        |
| Green   | 5     | 5                | 0.5%      | 20                      |              |
| Blue    | 6     | 6                | 0.25%     | 10                      |              |
| Violet  | 7     | 7                | 0.1%      | 5                       |              |
| Grey    | 8     | 8                | 0.05%     | 1                       |              |
| White   | 9     | 9                |           |                         |              |
| Gold    | -na-  | -1               | 5%        |                         |              |
| Silver  | -na-  | -2               | 10%       |                         |              |
| No Band | -na-  | -na-             | 20%       |                         |              |

4 band example: yellow violet orange silver indicate 4,7 and 3 zeros;  
i.e. a 47kΩ, 10% resistor.

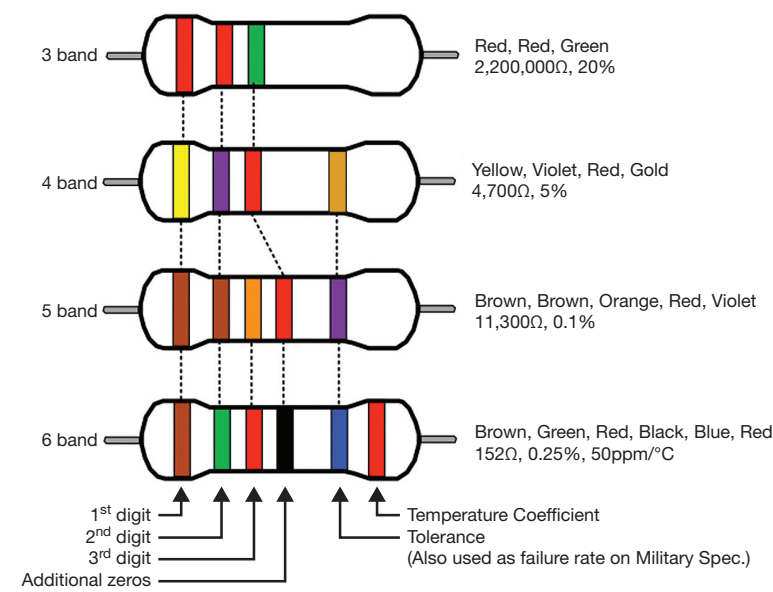


Figure 1: Resistor color code examples

Table 9: Standard resistor values

| Standard resistance values for the 10 to 100 decade |           |                 |                       |           |                 |                       |           |                 |                       |           |                 |                       |           |                 |                       |           |                 |                       |           |                 |                       |           |                 |
|-----------------------------------------------------|-----------|-----------------|-----------------------|-----------|-----------------|-----------------------|-----------|-----------------|-----------------------|-----------|-----------------|-----------------------|-----------|-----------------|-----------------------|-----------|-----------------|-----------------------|-----------|-----------------|-----------------------|-----------|-----------------|
| 0.1%<br>0.25%<br>0.5%                               | 1%<br>10% | 2%<br>5%<br>10% | 0.1%<br>0.25%<br>0.5% | 1%<br>10% | 2%<br>5%<br>10% | 0.1%<br>0.25%<br>0.5% | 1%<br>10% | 2%<br>5%<br>10% | 0.1%<br>0.25%<br>0.5% | 1%<br>10% | 2%<br>5%<br>10% | 0.1%<br>0.25%<br>0.5% | 1%<br>10% | 2%<br>5%<br>10% | 0.1%<br>0.25%<br>0.5% | 1%<br>10% | 2%<br>5%<br>10% | 0.1%<br>0.25%<br>0.5% | 1%<br>10% | 2%<br>5%<br>10% | 0.1%<br>0.25%<br>0.5% | 1%<br>10% | 2%<br>5%<br>10% |
|                                                     |           |                 |                       |           |                 |                       |           |                 |                       |           |                 |                       |           |                 |                       |           |                 |                       |           |                 |                       |           |                 |
| 10.0                                                | 10.0      | 10              | 14.7                  | 14.7      | 15              | 21.5                  | 21.5      | 21.5            | 31.6                  | 31.6      | 31.6            | 46.4                  | 46.4      | 46.4            | 68.1                  | 68.1      | 68.1            | 68.1                  | 68.1      | 68.1            | 68.1                  | 68.1      | 68              |
| 10.1                                                |           |                 | 14.9                  | 14.9      |                 | 21.8                  | 21.8      |                 | 32.0                  | 32.0      |                 | 47.0                  | 47.0      |                 | 69.0                  | 69.0      |                 | 69.0                  |           |                 |                       |           |                 |
| 10.2                                                | 10.2      |                 | 15.0                  | 15.0      | 15              | 22.1                  | 22.1      | 22              | 32.4                  | 32.4      | 32.4            | 47.5                  | 47.5      | 47.5            | 69.8                  | 69.8      |                 | 69.8                  |           |                 |                       |           |                 |
| 10.4                                                |           |                 | 15.2                  | 15.2      |                 | 22.3                  | 22.3      |                 | 32.8                  | 32.8      |                 | 48.1                  | 48.1      |                 | 70.6                  | 70.6      |                 | 70.6                  |           |                 |                       |           |                 |
| 10.5                                                | 10.5      |                 | 15.4                  | 15.4      |                 | 22.6                  | 22.6      |                 | 33.2                  | 33.2      | 33              | 48.7                  | 48.7      |                 | 71.5                  | 71.5      |                 | 71.5                  |           |                 |                       |           |                 |
| 10.6                                                |           |                 | 15.6                  | 15.6      |                 | 22.9                  | 22.9      |                 | 33.6                  | 33.6      |                 | 49.3                  | 49.3      |                 | 72.3                  | 72.3      |                 | 72.3                  |           |                 |                       |           |                 |
| 10.7                                                | 10.7      |                 | 15.8                  | 15.8      |                 | 23.2                  | 23.2      |                 | 34.0                  | 34.0      |                 | 50.5                  | 50.5      |                 | 73.2                  | 73.2      |                 | 73.2                  |           |                 |                       |           |                 |
| 10.9                                                |           |                 | 16.0                  | 16.0      | 16              | 23.4                  | 23.4      |                 | 34.4                  | 34.4      |                 | 51.1                  | 51.1      |                 | 74.1                  | 74.1      |                 | 74.1                  |           |                 |                       |           |                 |
| 11.0                                                | 11.0      | 11              | 16.2                  | 16.2      |                 | 23.7                  | 23.7      | 24              | 34.8                  | 34.8      |                 | 51.7                  | 51.7      | 51              | 75.0                  | 75.0      | 75              | 75.0                  | 75.0      | 75.0            | 75.0                  | 75.0      | 75              |
| 11.1                                                |           |                 | 16.4                  | 16.4      |                 | 24.0                  | 24.0      |                 | 35.2                  | 35.2      |                 | 52.3                  | 52.3      |                 | 75.9                  | 75.9      |                 | 75.9                  |           |                 |                       |           |                 |
| 11.3                                                | 11.3      |                 | 16.5                  | 16.5      |                 | 24.3                  | 24.3      |                 | 35.7                  | 35.7      | 36              | 53.0                  | 53.0      |                 | 76.8                  | 76.8      |                 | 76.8                  |           |                 |                       |           |                 |
| 11.4                                                |           |                 | 16.7                  | 16.7      |                 | 24.6                  | 24.6      |                 | 36.1                  | 36.1      |                 | 53.6                  | 53.6      |                 | 77.7                  | 77.7      |                 | 77.7                  |           |                 |                       |           |                 |
| 11.5                                                | 11.5      |                 | 16.9                  | 16.9      |                 | 24.9                  | 24.9      |                 | 36.5                  | 36.5      |                 | 54.2                  | 54.2      |                 | 78.7                  | 78.7      |                 | 78.7                  |           |                 |                       |           |                 |
| 11.7                                                |           |                 | 17.2                  | 17.2      |                 | 25.2                  | 25.2      |                 | 37.0                  | 37.0      |                 | 55.6                  | 55.6      |                 | 79.6                  | 79.6      |                 | 79.6                  |           |                 |                       |           |                 |
| 11.8                                                | 11.8      |                 | 17.4                  | 17.4      |                 | 25.5                  | 25.5      |                 | 37.4                  | 37.4      |                 | 56.2                  | 56.2      |                 | 80.6                  | 80.6      |                 | 80.6                  |           |                 |                       |           |                 |
| 12.0                                                |           | 12              | 17.6                  | 17.6      |                 | 25.8                  | 25.8      |                 | 37.9                  | 37.9      |                 | 56.9                  | 56.9      |                 | 81.6                  | 81.6      |                 | 81.6                  |           |                 |                       |           |                 |
| 12.1                                                | 12.1      |                 | 17.8                  | 17.8      | 18              | 26.1                  | 26.1      |                 | 38.3                  | 38.3      |                 | 57.6                  | 57.6      | 56              | 82.5                  | 82.5      | 82              | 82.5                  | 82.5      | 82.5            | 82.5                  | 82.5      | 82              |
| 12.3                                                |           |                 | 18.0                  | 18.0      |                 | 26.4                  | 26.4      |                 | 38.8                  | 38.8      |                 | 58.3                  | 58.3      |                 | 83.5                  | 83.5      |                 | 83.5                  |           |                 |                       |           |                 |
| 12.4                                                | 12.4      |                 | 18.2                  | 18.2      |                 | 26.7                  | 26.7      |                 | 39.2                  | 39.2      | 39              | 59.0                  | 59.0      |                 | 84.5                  | 84.5      |                 | 84.5                  |           |                 |                       |           |                 |
| 12.6                                                |           |                 | 18.4                  | 18.4      |                 | 27.1                  | 27.1      | 27              | 39.7                  | 39.7      |                 | 59.7                  | 59.7      |                 | 85.6                  | 85.6      |                 | 85.6                  |           |                 |                       |           |                 |
| 12.7                                                | 12.7      |                 | 18.7                  | 18.7      |                 | 27.4                  | 27.4      |                 | 40.2                  | 40.2      |                 | 60.4                  | 60.4      |                 | 86.6                  | 86.6      |                 | 86.6                  |           |                 |                       |           |                 |
| 12.9                                                |           |                 | 18.9                  | 18.9      |                 | 27.7                  | 27.7      |                 | 40.7                  | 40.7      |                 | 61.2                  | 61.2      |                 | 87.6                  | 87.6      |                 | 87.6                  |           |                 |                       |           |                 |
| 13.0                                                | 13.0      | 13              | 19.1                  | 19.1      |                 | 28.0                  | 28.0      |                 | 41.2                  | 41.2      |                 | 62.6                  | 62.6      | 62              | 88.7                  | 88.7      |                 | 88.7                  |           |                 |                       |           |                 |
| 13.2                                                |           |                 | 19.3                  | 19.3      |                 | 28.4                  | 28.4      |                 | 41.7                  | 41.7      |                 | 63.4                  | 63.4      |                 | 89.8                  | 89.8      |                 | 89.8                  |           |                 |                       |           |                 |
| 13.3                                                | 13.3      |                 | 19.6                  | 19.6      |                 | 28.7                  | 28.7      |                 | 42.2                  | 42.2      |                 | 64.2                  | 64.2      |                 | 90.9                  | 90.9      | 91              | 90.9                  | 90.9      | 90.9            | 90.9                  | 90.9      | 91              |
| 13.5                                                |           |                 | 19.8                  | 19.8      |                 | 29.1                  | 29.1      |                 | 42.7                  | 42.7      |                 | 65.5                  | 65.5      |                 | 92.0                  | 92.0      |                 | 92.0                  |           |                 |                       |           |                 |
| 13.7                                                | 13.7      |                 | 20.0                  | 20.0      | 20              | 29.4                  | 29.4      |                 | 43.2                  | 43.2      | 43              | 66.5                  | 66.5      |                 | 93.1                  | 93.1      |                 | 93.1                  |           |                 |                       |           |                 |
| 13.8                                                |           |                 | 20.3                  | 20.3      |                 | 29.8                  | 29.8      |                 | 43.7                  | 43.7      |                 | 67.3                  | 67.3      |                 | 94.2                  | 94.2      |                 | 94.2                  |           |                 |                       |           |                 |
| 14.0                                                | 14.0      |                 | 20.5                  | 20.5      |                 | 30.1                  | 30.1      | 30              | 44.2                  | 44.2      |                 | 68.1                  | 68.1      |                 | 95.3                  | 95.3      |                 | 95.3                  |           |                 |                       |           |                 |
| 14.2                                                |           |                 | 20.8                  | 20.8      |                 | 30.5                  | 30.5      |                 | 44.8                  | 44.8      |                 | 69.8                  | 69.8      |                 | 96.5                  | 96.5      |                 | 96.5                  |           |                 |                       |           |                 |
| 14.3                                                | 14.3      |                 | 21.0                  | 21.0      |                 | 30.9                  | 30.9      |                 | 45.3                  | 45.3      |                 | 70.6                  | 70.6      |                 | 97.6                  | 97.6      |                 | 97.6                  |           |                 |                       |           |                 |
| 14.5                                                |           |                 | 21.3                  | 21.3      |                 | 31.2                  | 31.2      |                 | 45.9                  | 45.9      |                 | 71.5                  | 71.5      |                 | 98.8                  | 98.8      |                 | 98.8                  |           |                 |                       |           |                 |

Practical capacitor model and specifications

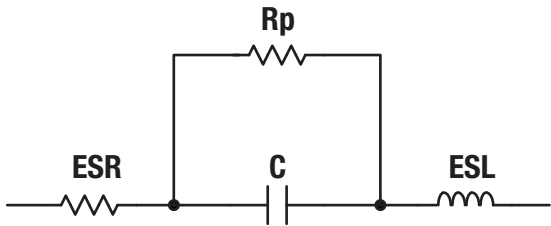


Figure 2: Model of a practical capacitor

Table 10: Capacitor specifications

| Parameter               | Description                                                                                                                                                                                                                                                                          |
|-------------------------|--------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| C                       | The nominal value of the capacitance<br>Table 12 lists standard capacitance values                                                                                                                                                                                                   |
| ESR                     | Equivalent series resistance<br>Ideally this is zero<br>Ceramic capacitors have the best ESR (typically in milliohms). Tantalum Electrolytic have ESR in the hundreds of milliohms and Aluminum Electrolytic have ESR in the ohms                                                    |
| ESL                     | Equivalent series inductance<br>Ideally this is zero<br>ESL ranges from 100 pH to 10 nH                                                                                                                                                                                              |
| Rp                      | Rp is a parallel leakage resistance (or insulation resistance)<br>Ideally this is infinite<br>This can range from tens of megaohms for some electrolytic capacitors to tens of gigohms for ceramic                                                                                   |
| Voltage rating          | The maximum voltage that can be applied to the capacitor<br>Exceeding this rating damages the capacitor                                                                                                                                                                              |
| Voltage coefficient     | The change in capacitance with applied voltage in ppm/V<br>A high-voltage coefficient can introduce distortion<br>COG capacitors have the lowest coefficient<br>The voltage coefficient is most important in applications that use capacitors in signal processing such as filtering |
| Temperature coefficient | The change in capacitance with across temperature in ppm/°C<br>Ideally, the temperature coefficient is zero<br>The maximum specified drift generally ranges from 10 to 100ppm/°C or greater depending on the capacitor type (See Table 11 for details)                               |

Practical capacitors vs. frequency

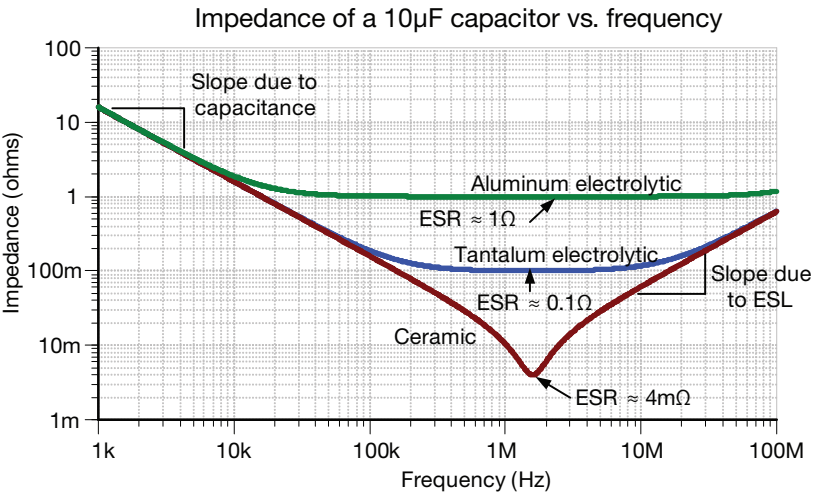


Figure 3: Effect of ESR and ESL on capacitor frequency response

Table 11: Capacitor type overview

| Capacitor type                      | Description                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          |
|-------------------------------------|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| <b>COG/NPO<br/>(Type 1 ceramic)</b> | Use in signal path, filtering, low distortion, audio, and precision<br>Limited capacitance range: 0.1 pF to 0.47 $\mu$ F<br>Lowest temperature coefficient: $\pm 30$ ppm/ $^{\circ}$ C<br>Low-voltage coefficient<br>Minimal piezoelectric effect<br>Good tolerance: $\pm 1\%$ to $\pm 10\%$<br>Temperature range: $-55^{\circ}$ C to $125^{\circ}$ C ( $150^{\circ}$ C and higher)<br>Voltage range may be limited for larger capacitance values                                                                                                    |
| <b>X7R<br/>(Type 2 ceramic)</b>     | Use for decoupling and other applications where accuracy and low distortion are not required<br>X7R is an example of a type 2 ceramic capacitor<br>See EIA capacitor tolerance table for details on other types<br>Capacitance range: 10 pF to 47 $\mu$ F<br>Temperature coefficient: $\pm 833$ ppm/ $^{\circ}$ C ( $\pm 15\%$ across temp range)<br>Substantial voltage coefficient<br>Tolerance: $\pm 5\%$ to $-20\%/+80\%$<br>Temperature range: $-55^{\circ}$ C to $125^{\circ}$ C<br>Voltage range may be limited for larger capacitance values |
| <b>Y5V<br/>(Type 2 ceramic)</b>     | Use for decoupling and other applications where accuracy and low distortion are not required<br>Y5V is an example of a type 2 ceramic capacitor<br>See EIA capacitor tolerance table for details on other types<br>Temperature coefficient: $-20\%/+80\%$ across temp range<br>Temperature range: $-30^{\circ}$ C to $85^{\circ}$ C<br>Other characteristics are similar to X7R and other type 2 ceramic                                                                                                                                             |
| <b>Aluminum oxide electrolytic</b>  | Use for bulk decoupling and other applications where large capacitance is required<br>Note that electrolytic capacitors are polarized and will be damaged, if a reverse polarity connection is made<br>Capacitance range: 1 $\mu$ F to 68,000 $\mu$ F<br>Temperature coefficient: $\pm 30$ ppm/ $^{\circ}$ C<br>Substantial voltage coefficient Tolerance: $\pm 20\%$<br>Temperature range: $-55^{\circ}$ C to $125^{\circ}$ C ( $150^{\circ}$ C and higher)<br>Higher ESR than other types                                                          |
| <b>Tantalum electrolytic</b>        | Capacitance range: 1 $\mu$ F to 150 $\mu$ F<br>Similar to aluminum oxide but smaller size                                                                                                                                                                                                                                                                                                                                                                                                                                                            |
| <b>Polypropylene film</b>           | Capacitance range: 100 pF to 10 $\mu$ F<br>Very low voltage coefficient (low distortion)<br>Higher cost than other types<br>Larger size per capacitance than other types<br>Temperature coefficient: 2% across temp range<br>Temperature range: $-55^{\circ}$ C to $100^{\circ}$ C                                                                                                                                                                                                                                                                   |

Table 12: Standard capacitance table

| Standard capacitance table |     |     |     |     |     |     |     |     |     |     |     |  |
|----------------------------|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|--|
| 1                          | 1.1 | 1.2 | 1.3 | 1.5 | 1.6 | 1.8 | 2   | 2.2 | 2.4 | 2.7 | 3   |  |
| 3.3                        | 3.6 | 3.9 | 4.3 | 4.7 | 5.1 | 5.6 | 6.2 | 6.8 | 7.5 | 8.2 | 9.1 |  |

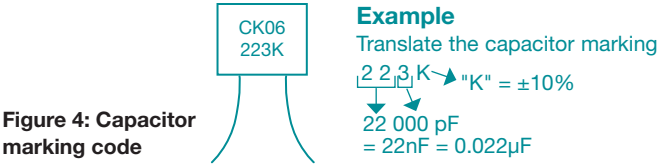


Table 13: Ceramic capacitor tolerance markings

| Code | Tolerance | Code | Tolerance   |
|------|-----------|------|-------------|
| B    | ± 0.1 pF  | J    | ± 5%        |
| C    | ± 0.25 pF | K    | ± 10%       |
| D    | ± 0.5 pF  | M    | ± 20%       |
| F    | ± 1%      | Z    | + 80%, -20% |
| G    | ± 2%      |      |             |

Table 14: EIA capacitor tolerance markings (Type 2 capacitors)

| First letter symbol | Low temp limit | Second number symbol | High temp limit | Second letter symbol | Max. capacitance change over temperature rating |
|---------------------|----------------|----------------------|-----------------|----------------------|-------------------------------------------------|
| Z                   | +10°C          | 2                    | +45°C           | A                    | ±1.0%                                           |
| Y                   | -30°C          | 4                    | +65°C           | B                    | ±1.5%                                           |
| X                   | -55°C          | 5                    | +85°C           | C                    | ±2.2%                                           |
|                     |                | 6                    | +105°C          | D                    | ±3.3%                                           |
|                     |                | 7                    | +125°C          | E                    | ±4.7%                                           |
|                     |                |                      |                 | F                    | ±7.5%                                           |
|                     |                |                      |                 | P                    | ±10.0%                                          |
|                     |                |                      |                 | R                    | ±15.0%                                          |
|                     |                |                      |                 | S                    | ±22.0%                                          |
|                     |                |                      |                 | T                    | ±22% ~ 33%                                      |
|                     |                |                      |                 | U                    | ±22% ~ 56%                                      |
|                     |                |                      |                 | V                    | ±22% ~ 82%                                      |

**Example**  
X7R: -55°C to +125°C, ±15.0%

Diodes and LEDs

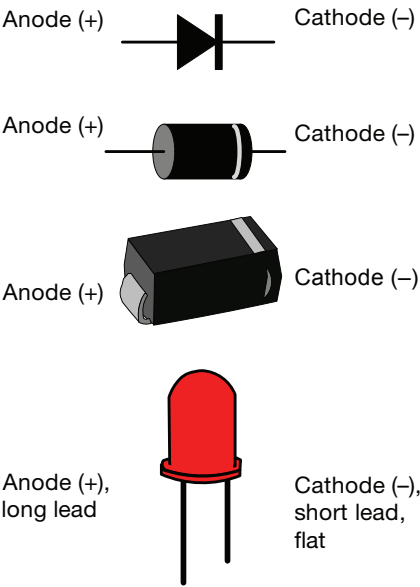


Figure 5: Diode and LED pin names

Table 15: LED forward voltage drop by color

| Color           | Wavelength (nm) | Voltage (approximate range) |
|-----------------|-----------------|-----------------------------|
| Infrared        | 940-850         | 1.4 to 1.7                  |
| Red             | 660-620         | 1.7 to 1.9                  |
| Orange / Yellow | 620-605         | 2 to 2.2                    |
| Green           | 570-525         | 2.1 to 3.0                  |
| Blue/White      | 470-430         | 3.4 to 3.8                  |

Note: The voltages given are approximate, and are intended to show the general trend for forward voltage drop of LED diodes. Consult the manufacturer's data sheet for more precise values.

## Bipolar junction transistors (BJT)

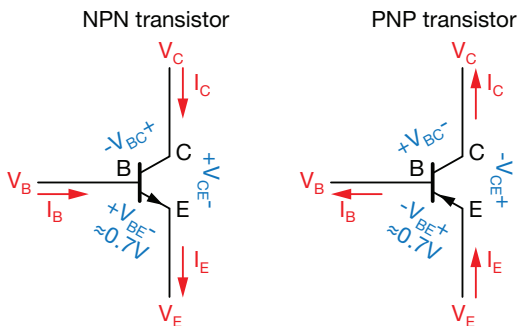


Figure 6: Bipolar transistors

$$I_C = I_B \cdot \beta$$

$$I_C = I_B + I_E$$

$$V_{BE} \approx 0.7V$$

$V_{BC}$  is reversed biased

$$V_{CE} \approx V_{BC} + V_{BE}$$

(1) Current gain

(2) Current law for bipolar transistors

(3) Voltage base to emitter is forward bias for normal operation. Approximately 0.7V.

(4) Voltage base to collector is reverse bias for normal operation

(5) Collector to emitter voltage

## Where

B, E, C = base, emitter, and collector

$I_B$ ,  $I_E$ ,  $I_C$  = base, emitter, and collector current

$\beta = h_{fe}$  = current gain

$V_{CE}$  = collector to emitter voltage

$V_{BC}$  = base to collector voltage

$V_{BE}$  = base to emitter voltage

Junction field effect transistors (JFET)

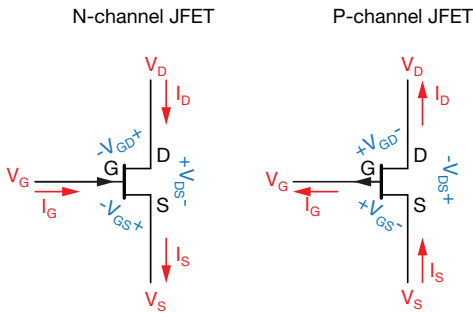


Figure 7: JFET transistors

- $I_G \approx 0V$   
 $I_D = I_S$   
 $I_D = \frac{2I_{DSS}}{V_P^2} \left( V_{GS} - V_P - \frac{V_{DS}}{2} \right) V_{DS}$   
 $I_D = I_{DSS} \left( 1 - \frac{V_{GS}}{V_P} \right)^2$
- (6) Gate to source reverse biased for normal operation

(7) Drain current equal to source current

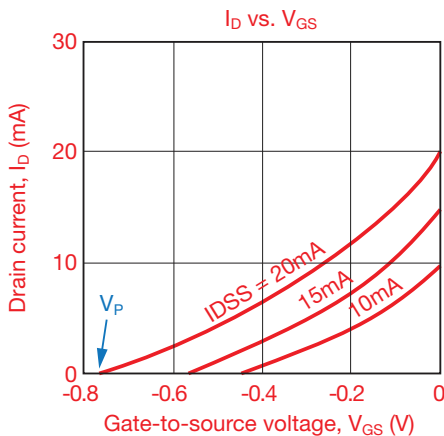
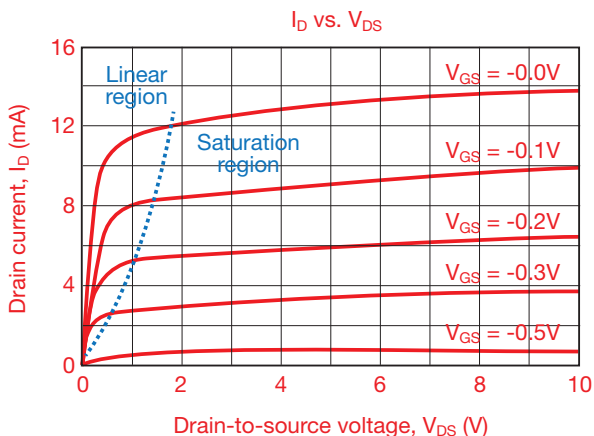
(8) Drain current in linear region

(9) Drain current in saturation region

Where

- G, D, S = gate, drain, and source
- $I_{DSS}$  = saturation current at zero gate to source voltage
- $V_P$  = pinch off voltage where the drain-to-source current stops
- $I_D = I_S$  = drain current, source current. These will be equal.
- $V_{GS}$  = gate to source voltage
- $V_{DS}$  = drain to source voltage

## Junction field effect transistors (JFET)

Figure 8: N-channel JFET characteristic curve  $I_D$  vs  $V_{GS}$ Figure 9: N-channel JFET characteristic curve  $I_D$  vs  $V_{GS}$ 

- The maximum gate-to-source voltage is 0V for an N-channel JFET. Greater than 0V will forward bias the gate-to-source junction and cause abnormal operation.
- The P-channel FET has similar characteristic curves but the polarity is opposite.

Metal oxide semiconductor field effect transistor (MOSFET)

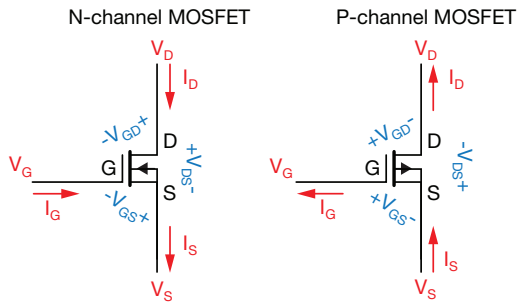


Figure 10: MOSFET transistors

$I_G \approx 0A$  (10) Gate is insulated so that input current is negligible

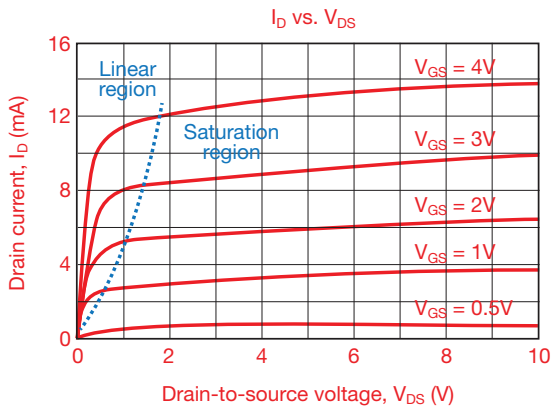
$I_D = I_S$  (11) Drain current equal to source current

$I_D = \mu_n C_{OX} \frac{W}{L} \left( (V_{GS} - V_{TH}) V_{DS} - \frac{V_{DS}^2}{2} \right)$  (12) Drain current in linear region (triode)

$I_D = \frac{\mu_n C_{OX}}{2} \frac{W}{L} (V_{GS} - V_{TH})^2 (1 + \lambda (V_{DS} - V_{DSsat}))$  (13) Drain current in saturation region

Where

- G, D, S = gate, drain, and source
- $\mu_n$  = charge-carrier effective mobility
- $C_{OX}$  = capacitance of oxide
- W, L = width and length of gate
- $V_{GS}$  = gate to source voltage
- $V_{DS}$  = drain to source voltage
- $V_{TH}$  = threshold voltage
- $\lambda$  = channel length modulation

**Metal oxide semiconductor field effect transistor (MOSFET)****Figure 11: N-channel MOSFET characteristic curve,  $I_D$  vs.  $V_{DS}$** 

- The parameters, such as  $\mu_n$ ,  $C_{OX}$ ,  $W$ , and  $L$ , may not be given in discrete MOSFET data sheets.
- The P-channel FET has similar characteristic curves but the polarity is opposite.

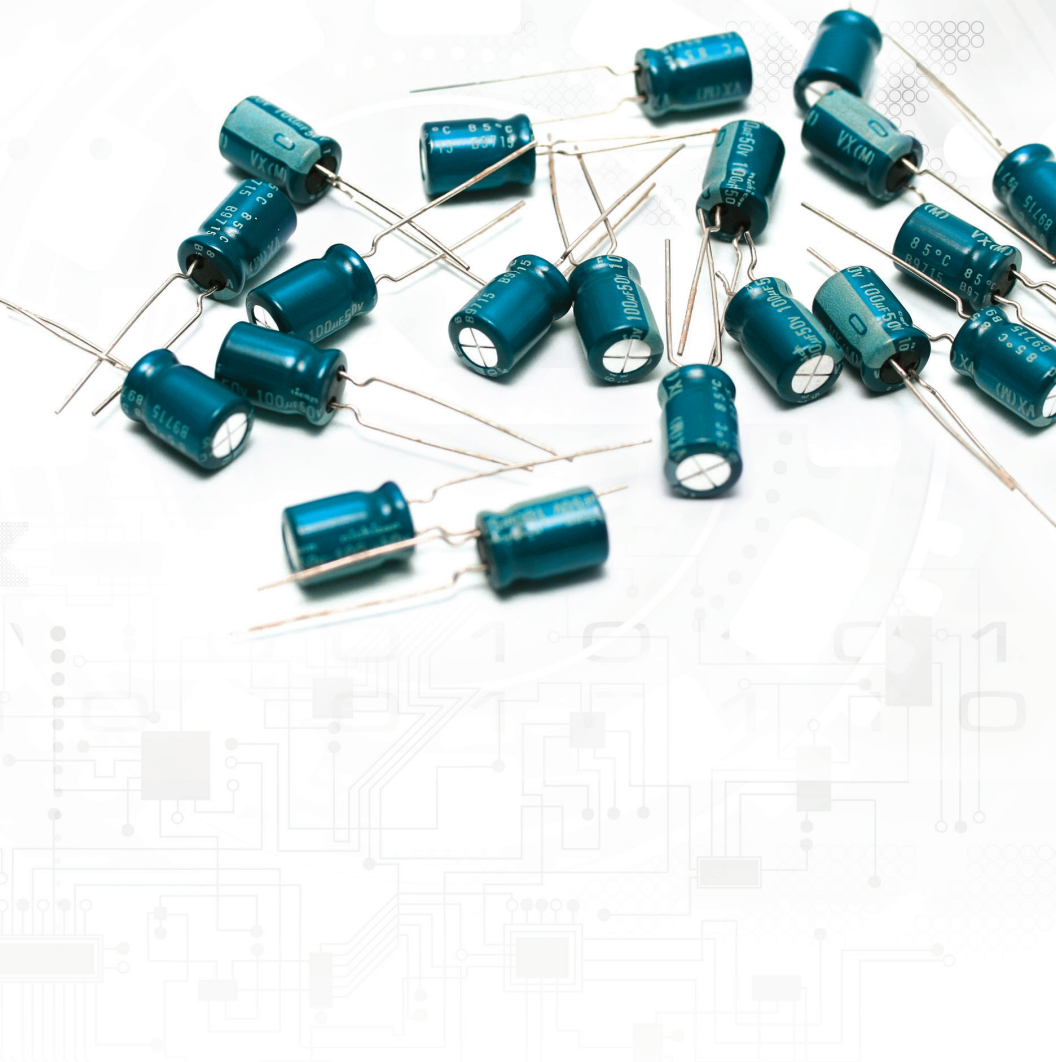
## Notes

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# Analog

- Resistor equations •
- Power equations •
- Capacitor equations (series, parallel, charge, energy) •
- Inductor equations (series, parallel, energy) •
- Capacitor charge and discharge •
- RMS and mean voltage definition •
- RMS for common signals •
- Logarithm laws •
- dB definitions •
- Pole and zero definition with examples •

Analog



## Resistor equations

$$R_T = R_1 + R_2 + \dots + R_N \quad (14) \text{ Series resistors}$$

$$R_T = \frac{R_1 \cdot R_2}{R_1 + R_2} \quad (15) \text{ Two parallel resistors}$$

$$R_T = \frac{1}{\frac{1}{R_1} + \frac{1}{R_2} + \dots + \frac{1}{R_N}} \quad (16) \text{ Parallel resistors}$$

Analog

### Where

$R_T$  = equivalent total resistance

$R_1, R_2, R_3, \dots, R_N$  = component resistors

## Ohm's law and voltage divider equation

$$V = I \cdot R \quad (17) \text{ Ohm's law}$$

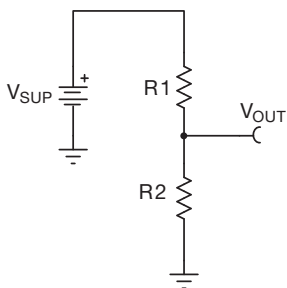
$$V_{OUT} = \left( \frac{R_2}{R_1 + R_2} \right) \cdot V_{sup} \quad (18) \text{ Voltage divider equation}$$

### Where

$V$  = voltage in volts (V)

$I$  = current in amps (A)

$R$  = resistance in ohms ( $\Omega$ )



**Figure 12:** Voltage divider

**Power equations**

|                     |                                                |
|---------------------|------------------------------------------------|
| $P = I \cdot V$     | (19) Power equation for voltage and current    |
| $P = \frac{V^2}{R}$ | (20) Power equation for voltage and resistance |
| $P = I^2 \cdot R$   | (21) Power equation for current and resistance |

**Where**

- P = power in watts (W)
- V = voltage in volts (V)
- I = current in amps (A)
- R = resistance in ohms ( $\Omega$ )

|                                                         |                        |
|---------------------------------------------------------|------------------------|
| $P = \frac{1}{2} \cdot V_p \cdot I_p \cdot \cos \theta$ | (22) AC power equation |
|---------------------------------------------------------|------------------------|

**Where**

- P = average power in watts (W) for sinusoidal signals
- $V_p$  = peak voltage in volts (V)
- $I_p$  = peak current in amps (A)
- $\theta$  = phase angle between the voltage and current sine waves

## Capacitor equations

$$C_t = \frac{1}{\frac{1}{C_1} + \frac{1}{C_2} + \dots + \frac{1}{C_N}} \quad (23) \text{ Series capacitors}$$

$$C_t = \frac{C_1 C_2}{C_1 + C_2} \quad (24) \text{ Two series capacitors}$$

$$C_t = C_1 + C_2 + \dots + C_N \quad (25) \text{ Parallel capacitors}$$

### Where

$C_t$  = equivalent total capacitance

$C_1, C_2, C_3 \dots C_N$  = component capacitors

$$Q = CV \quad (26) \text{ Charge storage}$$

$$Q = It \quad (27) \text{ Charge defined}$$

### Where

$Q$  = charge in coulombs (C)

$C$  = capacitance in farads (F)

$V$  = voltage in volts (V)

$I$  = current in amps (A)

$t$  = time in seconds (s)

$$i = C \frac{dv}{dt} \quad (28) \text{ Instantaneous current through a capacitor}$$

### Where

$i$  = instantaneous current through the capacitor

$C$  = capacitance in farads (F)

$\frac{dv}{dt}$  = the instantaneous rate of voltage change

$$E = \frac{1}{2} CV^2 \quad (29) \text{ Energy stored in a capacitor}$$

### Where

$E$  = energy stored in a capacitor in joules (J)

$V$  = voltage in volts

$C$  = capacitance in farads (F)

**Inductor equations**

$$L_t = L_1 + L_2 + \dots + L_N \quad (30) \text{ Series inductors}$$

$$L_t = \frac{1}{\frac{1}{L_1} + \frac{1}{L_2} + \dots + \frac{1}{L_N}} \quad (31) \text{ Parallel inductors}$$

$$L_t = \frac{L_1 L_2}{L_1 + L_2} \quad (32) \text{ Two parallel inductors}$$

**Where**

$L_t$  = equivalent total inductance

$L_1, L_2, L_3 \dots L_N$  = component inductance

$$v = L \frac{di}{dt} \quad (33) \text{ Instantaneous voltage across an inductor}$$

**Where**

$v$  = instantaneous voltage across the inductor

$L$  = inductance in henries (H)

$\frac{di}{dt}$  = instantaneous rate of current change

$$E = \frac{1}{2} L I^2 \quad (34) \text{ Energy stored in an inductor}$$

**Where**

$E$  = energy stored in an inductor in joules (J)

$I$  = current in amps

$L$  = inductance in henries (H)

Equation for charging an RC circuit

$$V_C = V_S \left[ 1 - e^{\left( \frac{-t}{\tau} \right)} \right]$$

(35) General relationship

Where

$V_C$  = voltage across the capacitor at any instant in time ( $t$ )

$V_S$  = the source voltage charging the RC circuit

$t$  = time in seconds

$\tau$  = RC, the time constant for charging and discharging capacitors

Graphing equation 35 produces the capacitor charging curve below. Note that the capacitor is 99.3% charged at five time constants. It is common practice to consider this *fully charged*.

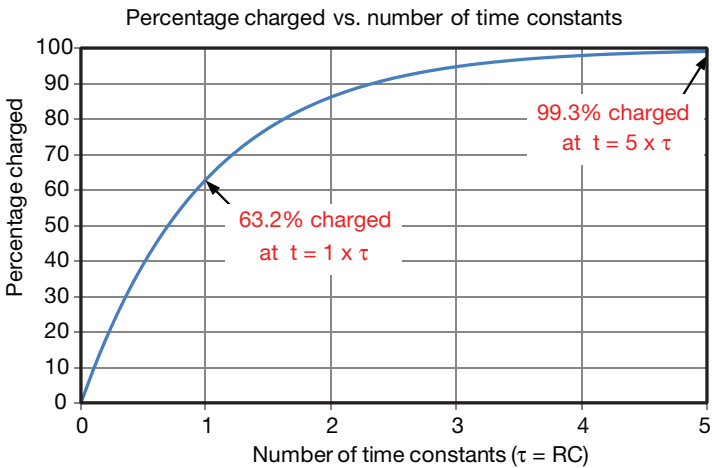


Figure 13: RC charge curve

## Equation for discharging an RC circuit

$$V_C = V_i \left[ e^{\left( \frac{-t}{\tau} \right)} \right] \quad (36) \text{ General Relationship}$$

### Where

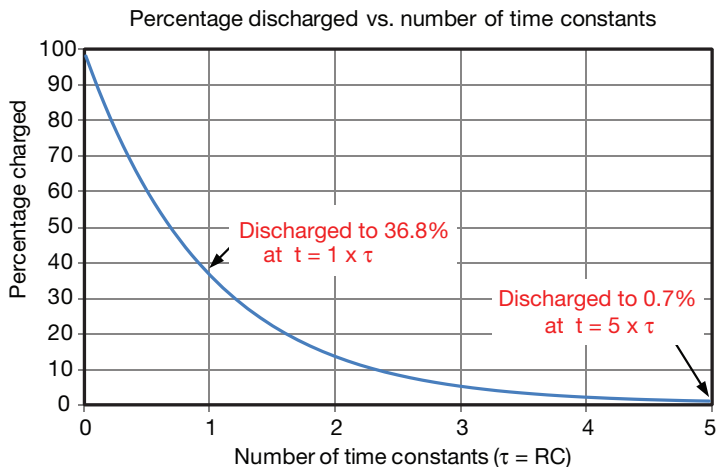
$V_C$  = voltage across the capacitor at any instant in time ( $t$ )

$V_i$  = the initial voltage of the capacitor at  $t = 0s$

$t$  = time in seconds

$\tau = RC$ , the time constant for charging and discharging capacitors

Graphing equation 36 produces the capacitor discharge curve below. Note that the capacitor is discharged to 0.7% at five time constants. It is common practice to consider this *fully discharged*.



**Figure 14: RC discharge curve**

## Capacitor with constant current source

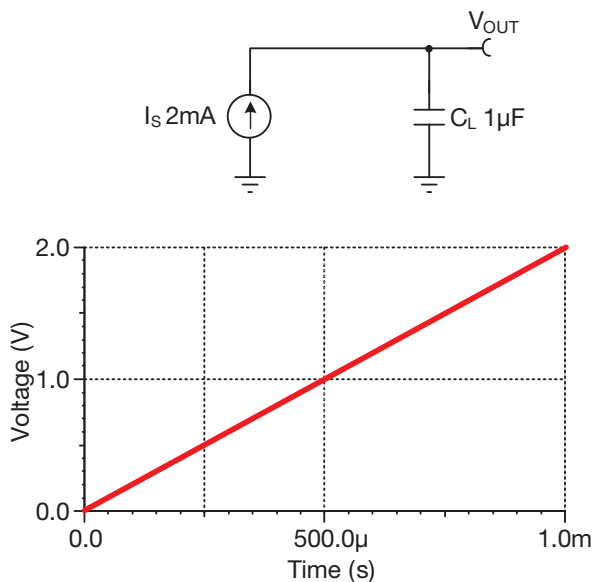


Figure 15: Capacitor with constant current source

$$dv = \frac{i}{C} dt \quad (37) \text{ General equation for capacitor voltage current}$$

$$V_{OUT} = \frac{I_S}{C_L} t \quad (38) \text{ For constant current}$$

## Where

$I_S$  = constant current source in amps (A)

$V_{OUT}$  = voltage developed across the capacitor in volts (V)

$C_L$  = load capacitance in farads (F)

$t$  = time in seconds (s)

## RMS and mean voltage

### RMS voltage

$$V_{\text{RMS}} = \sqrt{\frac{1}{(T_2 - T_1)} \int_{T_1}^{T_2} [V(t)]^2 dt} \quad (39) \text{ General relationship}$$

#### Where

$V(t)$  = continuous function of time

$t$  = time in seconds

$T_1 \leq t \leq T_2$  = the time interval that the function is defined over

### Mean voltage

$$V_{\text{MEAN}} = \frac{1}{(T_2 - T_1)} \int_{T_1}^{T_2} V(t) dt \quad (40) \text{ General relationship}$$

#### Where

$V(t)$  = continuous function of time

$t$  = time in seconds

$T_1 \leq t \leq T_2$  = the time interval that the function is defined over

$$V_{\text{RMS}} = \frac{V_{\text{PEAK}}}{\sqrt{2}} \quad (41) \text{ RMS for full wave rectified sine wave}$$

$$V_{\text{MEAN}} = \frac{2 \times V_{\text{PEAK}}}{\pi} \quad (42) \text{ Mean for full wave rectified sine wave}$$

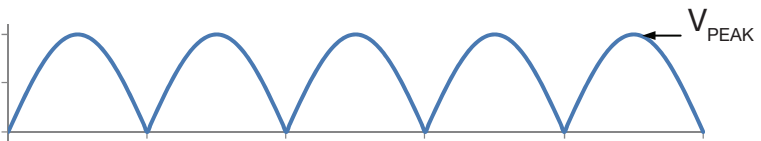


Figure 16: Full wave rectified sine wave

RMS voltage and mean voltage (cont.)

$$V_{\text{RMS}} = V_{\text{PEAK}} \sqrt{\frac{\tau}{2T}}$$

(43) RMS for a half-wave rectified sine wave

$$V_{\text{MEAN}} = \frac{2 \cdot V_{\text{PEAK}}}{\pi} \left( \frac{\tau}{T} \right)$$

(44) Mean for a half-wave rectified sine wave

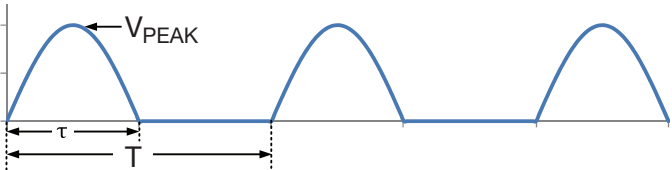


Figure 17: Half-wave rectified sine wave

$$V_{\text{RMS}} = V_{\text{PEAK}} \sqrt{\frac{\tau}{T}}$$

(45) RMS for a square wave

$$V_{\text{MEAN}} = V_{\text{PEAK}} \left( \frac{\tau}{T} \right)$$

(46) Mean for a square wave

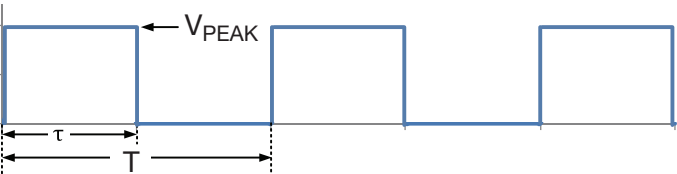
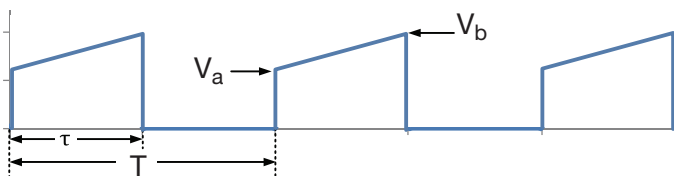


Figure 18: Square wave

**RMS voltage and mean voltage (cont.)**

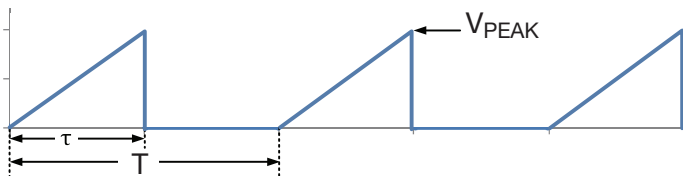
$$V_{\text{RMS}} = \sqrt{\left( \frac{V_a^2 + V_a \cdot V_b + V_b^2}{3} \right) \left( \frac{\tau}{T} \right)} \quad (47) \text{ RMS for a trapezoid}$$

$$V_{\text{MEAN}} = \frac{\tau}{2T} (V_a + V_b) \quad (48) \text{ Mean for a trapezoid}$$

**Figure 19: Trapezoidal wave**

$$V_{\text{RMS}} = V_{\text{PEAK}} \sqrt{\frac{\tau}{3T}} \quad (49) \text{ RMS for a triangle wave}$$

$$V_{\text{MEAN}} = \frac{\tau}{2T} V_{\text{PEAK}} \quad (50) \text{ Mean for a triangle wave}$$

**Figure 20: Triangle wave**

**Logarithmic mathematical definitions**

$$\log\left(\frac{A}{B}\right) = \log(A) - \log(B) \quad (51) \text{ Log of dividend}$$

$$\log(AB) = \log(A) + \log(B) \quad (52) \text{ Log of product}$$

$$\log(A^x) = x \log(A) \quad (53) \text{ Log of exponent}$$

$$\log_b(X) = \frac{\log_a(X)}{\log_a(b)} \quad (54) \text{ Changing the base of log function}$$

$$\log_2(X) = \frac{\log_{10}(X)}{\log_{10}(2)} \quad (55) \text{ Example changing to log base 2}$$

$$\ln(X) = \log_e(X) \quad (56) \text{ Natural log is log base e}$$

$$e = 2.718282 \quad (57) \text{ Exponential function to 6 digits}$$

**Alternative notations**

$$\exp(x) = e^x \quad (58) \text{ Different notation for exponential function}$$

$$3.54\text{E} - 2 = 3.54 \times 10^{-2} \quad (59) \text{ Different notation for scientific notation, sometimes confused with exponential function}$$

## dB definitions

### Bode plot basics

The frequency response for the magnitude or gain plot is the change in voltage gain as frequency changes. This change is specified on a Bode plot, a plot of frequency versus voltage gain in dB (decibels). Bode plots are usually plotted as semi-log plots with frequency on the x-axis, log scale, and gain on the y-axis, linear scale. The other half of the frequency response is the phase shift versus frequency and is plotted as frequency versus degrees phase shift. Phase plots are usually plotted as semi-log plots with frequency on the x-axis, log scale, and phase shift on the y-axis, linear scale.

### Definitions

$$\text{Voltage gain (dB)} = 20 \log \left( \frac{V_{\text{OUT}}}{V_{\text{IN}}} \right) \quad (60) \text{ Voltage gain in decibels}$$

$$\text{Power gain (dB)} = 10 \log \left( \frac{P_{\text{OUT}}}{P_{\text{IN}}} \right) \quad (61) \text{ Power gain in decibels}$$

$$\text{Power measured (dBm)} = 10 \log \left( \frac{\text{Power measured (W)}}{1 \text{ mW}} \right) \quad (62) \text{ Used for input or output power}$$

| A (V/V)    | A (dB) |
|------------|--------|
| 0.001      | -60    |
| 0.01       | -40    |
| 0.1        | -20    |
| 1          | 0      |
| 10         | 20     |
| 100        | 40     |
| 1,000      | 60     |
| 10,000     | 80     |
| 100,000    | 100    |
| 1,000,000  | 120    |
| 10,000,000 | 140    |

**Table 16: Examples of common gain values and dB equivalent**

Roll-off rate is the decrease in gain with frequency

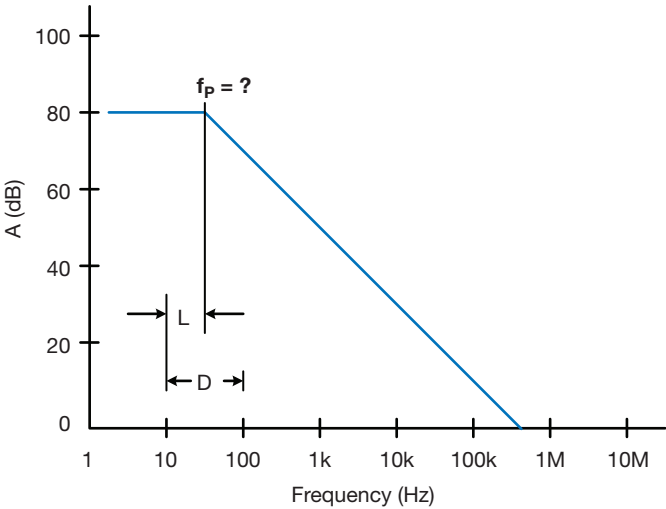
Decade is a tenfold increase or decrease in frequency  
(from 10 Hz to 100 Hz is one decade)

Octave is the doubling or halving of frequency  
(from 10 Hz to 20 Hz is one octave)

Log scale

**Figure 21** illustrates a method to graphically determine values on a logarithmic axis that are not directly on an axis grid line.

- 1. Given  $L = 1\text{ cm}$ ;  $D = 2\text{ cm}$ , measured with a ruler
- 2.  $L/D = \log_{10}(f_p)$
- 3.  $f_p = 10^{(L/D)} = 10^{(1\text{ cm}/2\text{ cm})} = 3.16$
- 4. Adjust for the decade range (for this example,  $f_p = 31.6\text{ Hz}$ )



**Figure 21: Finding values on logarithmic axis not directly on a grid line**

## Time to phase shift

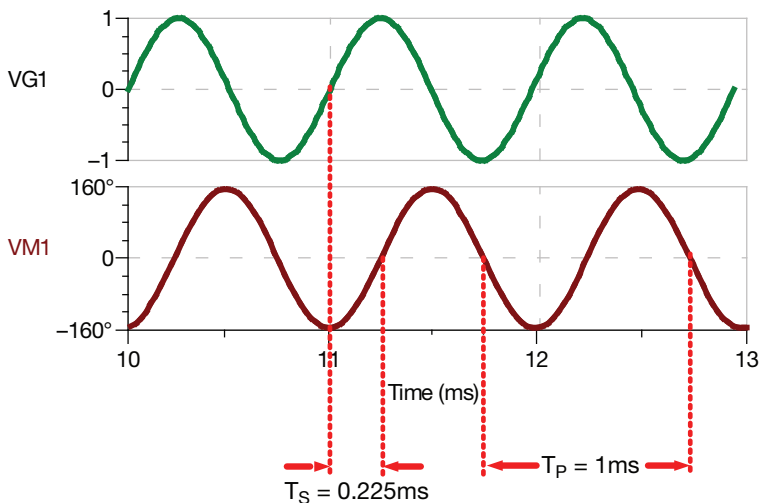


Figure 22: Time to phase shift

$$\theta = \frac{T_S}{T_P} \times 360^\circ$$

(63) Phase shift from time

## Where

 $T_S$  = time shift from input to output signal $T_P$  = period of signal $\theta$  = phase shift of the signal from input to output

## Example

Calculate the phase shift in degrees for Figure 24.

## Answer

$$\theta = \frac{T_S}{T_P} \cdot 360^\circ = \left( \frac{0.225\text{ ms}}{1\text{ ms}} \right) \cdot 360^\circ = 81^\circ$$

## Bode plots: Poles

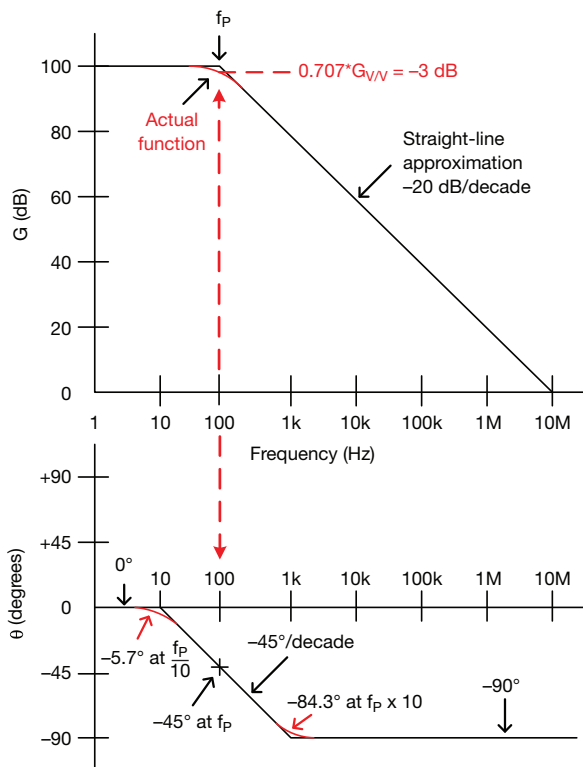


Figure 23: Pole gain and phase

## Where

Pole location =  $f_P$  (cutoff freq)

Magnitude ( $f < f_P$ ) =  $G_{DC}$  (for example, 100 dB)

Magnitude ( $f = f_P$ ) =  $-3$  dB

Magnitude ( $f > f_P$ ) =  $-20$  dB/decade

Phase ( $f = f_P$ ) =  $-45^\circ$

Phase ( $0.1 f_P < f < 10 f_P$ ) =  $-45^\circ/\text{decade}$

Phase ( $f > 10 f_P$ ) =  $-90^\circ$

Phase ( $f < 0.1 f_P$ ) =  $0^\circ$

**Pole (equations)**

$$G_V = \frac{V_{OUT}}{V_{IN}} = \frac{G_{DC}}{j \left( \frac{f}{f_P} \right) + 1} \quad (64) \text{ As a complex number}$$

$$G_V = \frac{V_{OUT}}{V_{IN}} = \frac{G_{DC}}{\sqrt{\left( \frac{f}{f_P} \right)^2 + 1}} \quad (65) \text{ Magnitude}$$

$$\theta = -\tan^{-1} \left( \frac{f}{f_P} \right) \quad (66) \text{ Phase shift}$$

$$G_{dB} = 20 \log(G_V) \quad (67) \text{ Magnitude in dB}$$

**Where**

$G_V$  = voltage gain in V/V

$G_{dB}$  = voltage gain in decibels

$G_{DC}$  = the dc or low frequency voltage gain

$f$  = frequency in Hz

$f_P$  = frequency at which the pole occurs

$\theta$  = phase shift of the signal from input to output

$j$  = indicates imaginary number or  $\sqrt{-1}$

Bode plots (zeros)

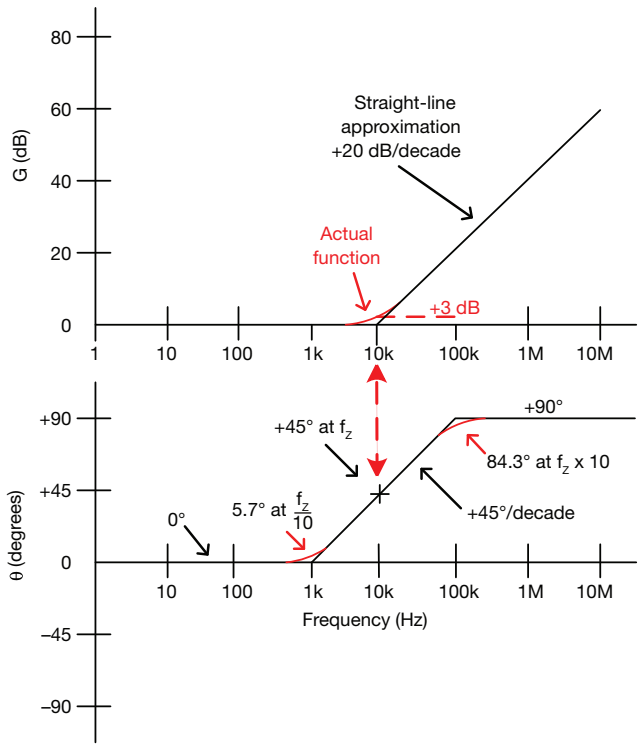


Figure 24: Zero gain and phase

Where

- Zero location =  $f_z$
- Magnitude ( $f < f_z$ ) = 0 dB
- Magnitude ( $f = f_z$ ) = +3 dB
- Magnitude ( $f > f_z$ ) = +20 dB/decade
- Phase ( $f = f_z$ ) = +45°
- Phase ( $0.1 f_z < f < 10 f_z$ ) = +45°/decade
- Phase ( $f > 10 f_z$ ) = +90°
- Phase ( $f < 0.1 f_z$ ) = 0°

**Zero (equations)**

$$G_V = \frac{V_{OUT}}{V_{IN}} = G_{DC} \left[ j \left( \frac{f}{f_Z} \right) + 1 \right] \quad (68) \text{ As a complex number}$$

$$G_V = \frac{V_{OUT}}{V_{IN}} = G_{DC} \sqrt{\left( \frac{f}{f_Z} \right)^2 + 1} \quad (69) \text{ Magnitude}$$

$$\theta = \tan^{-1} \left( \frac{f}{f_Z} \right) \quad (70) \text{ Phase shift}$$

$$G_{dB} = 20 \text{ Log}(G_V) \quad (71) \text{ Magnitude in dB}$$

**Where**

$G_V$  = voltage gain in V/V

$G_{dB}$  = voltage gain in decibels

$G_{DC}$  = the dc or low frequency voltage gain

$f$  = frequency in Hz

$f_Z$  = frequency at which the zero occurs

$\theta$  = phase shift of the signal from input to output

$j$  = indicates imaginary number or  $\sqrt{-1}$

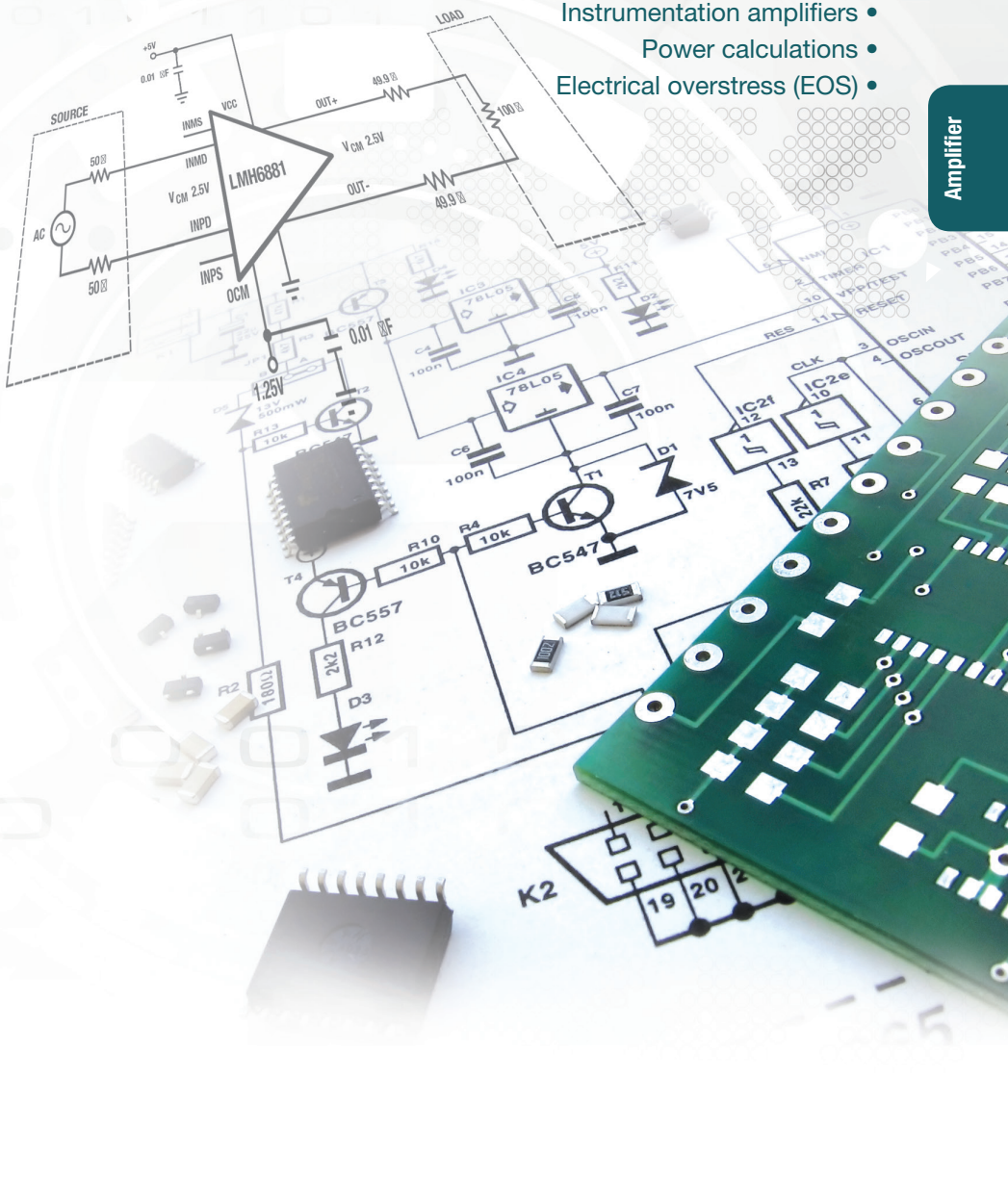
## Notes

[illegible]

# Amplifier

- Calculating amplifier offset •
- Op amp bandwidth •
- Full power bandwidth •
- Large signal step response •
- Settling time •
- Noise equations •
- Stability equations •
- Instrumentation amplifiers •
- Power calculations •
- Electrical overstress (EOS) •

Amplifier



Basic op amp configurations

$G_{CL} = 1$

(72) Gain for buffer configuration

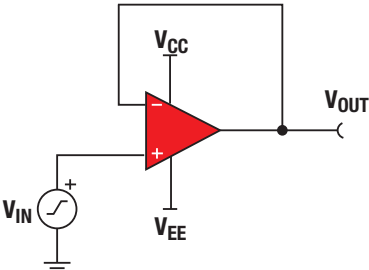


Figure 25: Buffer configuration

$G_{CL} = \frac{R_f}{R_1} + 1$

(73) Gain for non-inverting configuration

$Z_{in} = \text{Op amp input impedance}$

(74) Input impedance. See data sheet for value, but typically greater than 100MΩ to 100TΩ.

$V_{cm} = V_{IN}$

(75) The common mode voltage is equal to the input signal. Check for common mode limitations.

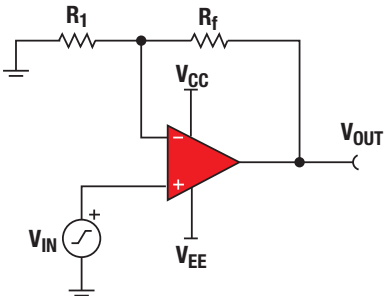


Figure 26: Non-inverting configuration

## Basic op amp configurations (cont.)

$$G_{CL} = -\frac{R_f}{R_1}$$

(76) Gain for inverting configuration

$$Z_{in} = R_1$$

(77) Input impedance. Low compared to the non-inverting configuration.

$$V_{cm} = 0V$$

(78) The common mode voltage held constant at 0V so the common mode range and CMRR is not a concern

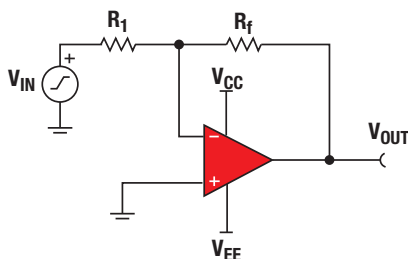


Figure 27: Inverting configuration

$$V_{OUT} = -R_f \left( \frac{V_1}{R_1} + \frac{V_2}{R_2} + \dots + \frac{V_N}{R_N} \right)$$

(79) Transfer function for inverting summing amplifier

$$V_{OUT} = -\frac{R_f}{R_1} (V_1 + V_2 + \dots + V_N)$$

(80) Transfer function for inverting summing amplifier, assuming  $R_1 = R_2 = \dots = R_N$

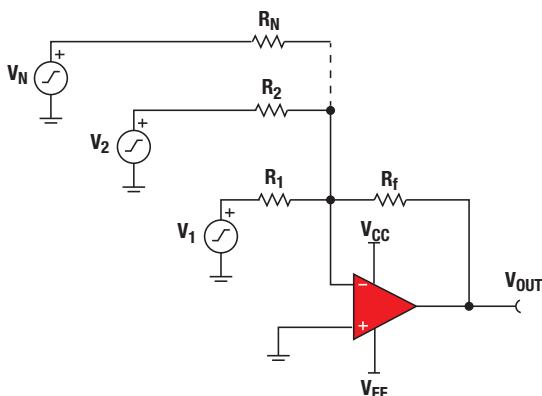


Figure 28: Inverting summing configuration

Basic op amp configurations (cont.)

$$V_{OUT} = \left( \frac{R_f}{R_{in}} + 1 \right) \left[ \frac{V_1}{N} + \frac{V_2}{N} + \dots + \frac{V_N}{N} \right]$$

(81) Transfer function for noninverting summing amplifier for equal input resistors

Where

$R_1 = R_2 = \dots = R_N$   
 $N$  = number of input resistors

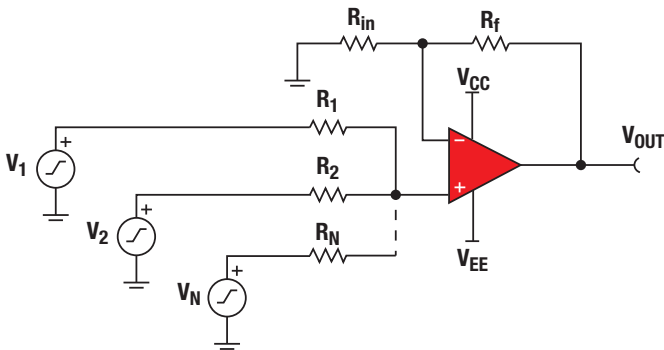


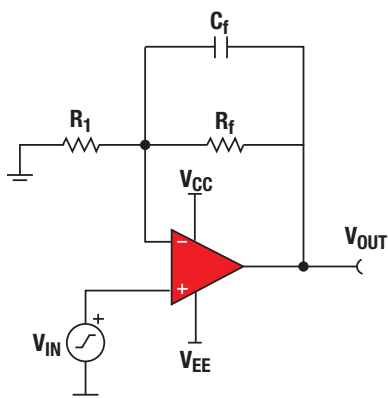
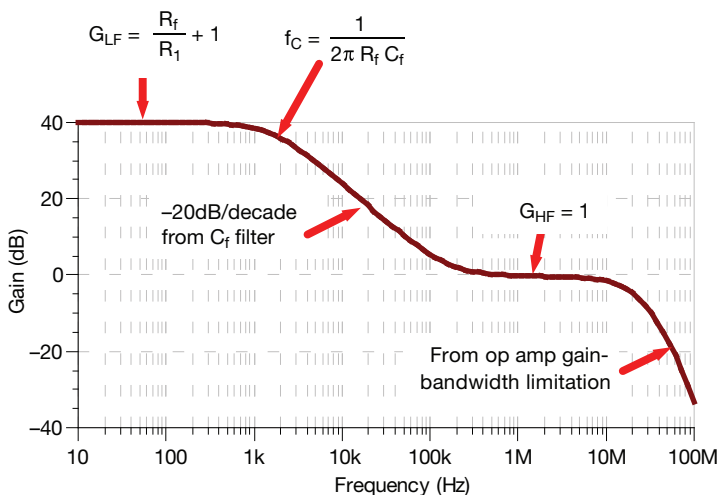
Figure 29: Non-inverting summing configuration

Simple non-inverting amp with  $C_f$  filter

$$G_{LF} = \frac{R_f}{R_1} + 1 \quad (82) \text{ Gain for non-inverting configuration for } f < f_C$$

$$G_{HF} = 1 \quad (83) \text{ Gain for non-inverting configuration for } f \gg f_C$$

$$f_C = \frac{1}{2\pi R_f C_f} \quad (84) \text{ Cut off frequency for non-inverting configuration}$$

Figure 30: Non-inverting amplifier with  $C_f$  filterFigure 31: Frequency response for non-inverting op amp with  $C_f$  filter

Simple inverting amp with  $C_f$  filter

$$G_{LF} = -\frac{R_f}{R_1}$$

(85) Gain for inverting configuration for  $f < f_C$

$$G_{HF} = -20\text{dB/decade after } f_C \text{ until op amp bandwidth limitation}$$

(86) Gain for inverting configuration for  $f > f_C$

$$f_C = \frac{1}{2\pi R_f C_f}$$

(87) Cutoff frequency for inverting configuration

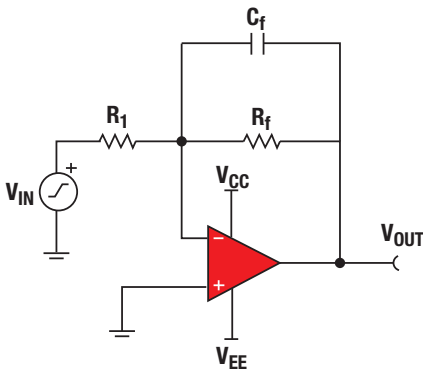


Figure 32: Inverting amplifier with  $C_f$  filter

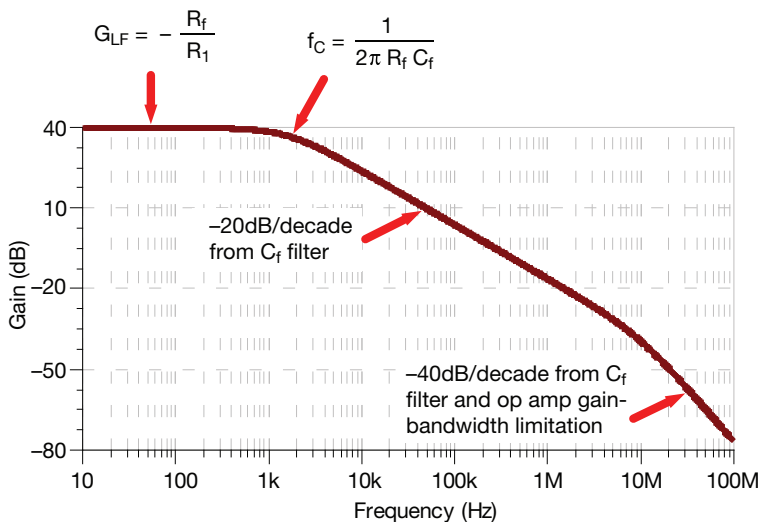


Figure 33: Frequency response for inverting op amp with  $C_f$  filter

## Differential filter cutoff

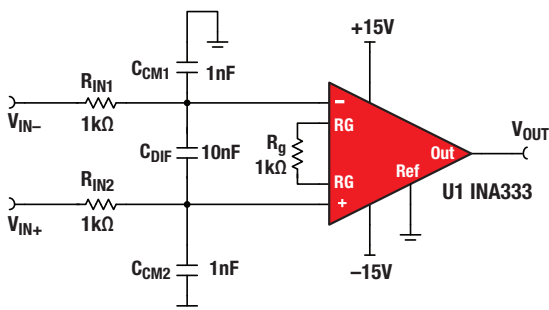


Figure 34: Input filter for instrumentation amplifier

Select  $C_{DIF} \geq 10C_{CM1}$

(88) Differential capacitor is sized 10 times the common-mode capacitor

$R_{IN1} = R_{IN2}$

(89) Input resistors must be equal

$C_{CM1} = C_{CM2}$

(90) Common-mode capacitors must be equal

$$f_{CM} = \frac{1}{2\pi R_{IN1} C_{CM1}}$$

(91) Common-mode filter cutoff

$$f_{DIF} = \frac{1}{2\pi(2R_{IN1})\left(C_{DIF} + \frac{1}{2}C_{CM1}\right)}$$

(92) Differential filter cutoff

## Where

$f_{DIF}$  = differential cutoff frequency

$f_{CM}$  = common-mode cutoff frequency

$R_{IN}$  = input resistance

$C_{CM}$  = common-mode filter capacitance

$C_{DIF}$  = differential filter capacitance

Note: Selecting  $C_{DIF} \geq 10 C_{CM}$  sets the differential mode cutoff frequency about 20 times lower than the common-mode cutoff frequency. This prevents common-mode noise from being converted into differential noise due to component tolerances.

## Calculating amplifier offset voltage

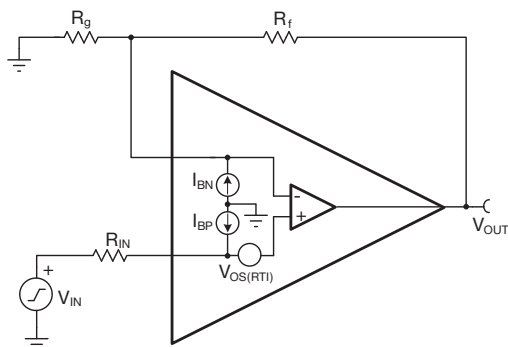


Figure 35: Op amp bias current and offset calculations

$$R_{eq} = \frac{R_f \cdot R_g}{R_f + R_g} \quad (93) \text{ Equivalent feedback resistance}$$

$$V_{OS(IBN)} = I_{BN} \cdot R_{eq} \quad (94) \text{ Offset RTI from } I_{BN} \text{ flowing into feedback}$$

$$V_{OS(IBP)} = I_{BP} \cdot R_{IN} \quad (95) \text{ Offset RTI from } I_{BP} \text{ flowing into source impedance}$$

$$V_{OS(\text{total worst})} = \pm V_{OS(\text{Amp})} \pm V_{OS(IBN)} \pm V_{OS(IBP)} \quad (96) \text{ Directly adding the offset components. Conservative estimate.}$$

$$V_{OS(\text{total stat})} = \sqrt{V_{OS(\text{Amp})}^2 + V_{OS(IBN)}^2 + V_{OS(IBP)}^2} \quad (97) \text{ Statistically adding the offset components. More realistic estimate.}$$

$$G_n = \frac{R_f}{R_g} + 1 \quad (98) \text{ Noise gain of op amp (always non-inverting gain)}$$

$$V_{OS(RTO)} = V_{OS(RTI)} \cdot G_n \quad (99) \text{ Offset referred to the output}$$

### Where

$R_f$ ,  $R_g$  = the feedback and gain setting resistors

$R_{IN}$  = resistance seen by noninverting input

$I_{BN}$ ,  $I_{BP}$  = the current flowing from the inverting ( $I_{BN}$ ) and noninverting ( $I_{BP}$ ) op amp input as specified in the data sheet

$V_{OS(\text{amp})}$  = the input offset voltage specification from the op amp data sheet

$V_{OS(RTI)}$  = this is the offset referred to the input. This can be either  $V_{OS(\text{total worst})}$  or

$V_{OS(\text{total stat})}$ .

## Op amp bandwidth

$$GBW = G_n \cdot BW$$

(100) Gain bandwidth product defined

### Where

GBW = gain bandwidth product, listed in op amp data sheet specification table

$G_n$  = closed loop noise gain, always non-inverting gain

BW = the bandwidth limitation of the amplifier

### Example

Determine bandwidth using equation 95, where

$G_n = 100$  (from amplifier configuration)

GBW = 22MHz (from data sheet)

### Answer

$$BW = \frac{GBW}{G_n} = \frac{22\text{MHz}}{100} = 220\text{kHz}$$

Note that the same result can be graphically determined using the  $A_{OL}$  curve as shown below.

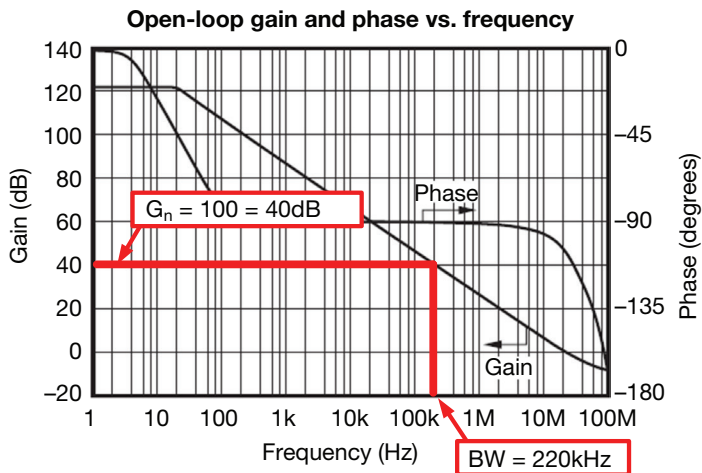


Figure 36: Using  $A_{OL}$  to find closed-loop bandwidth

Small signal step response

$$\tau_R = \frac{0.35}{f_C}$$

(101) Rise time for a small signal step

Where

- $\tau_R$  = the rise time of a small signal step response
- $f_C$  = the closed-loop bandwidth of the op amp circuit

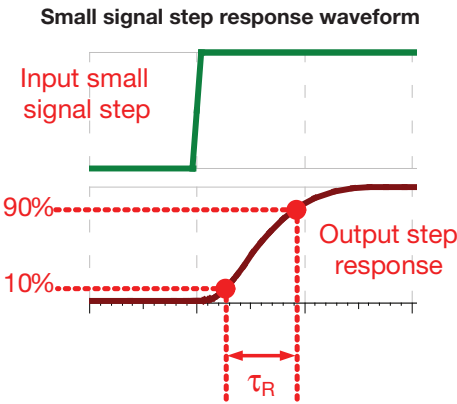


Figure 37: Small signal step response

## Full power bandwidth

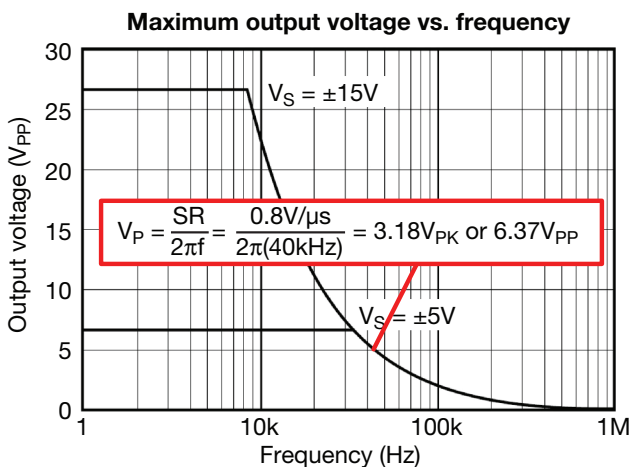
$$V_P = \frac{SR}{2\pi f} \quad (102) \text{ Maximum output without slew-rate induced distortion}$$

### Where

$V_P$  = maximum peak output voltage before slew induced distortion occurs

SR = slew rate

f = frequency of applied signal



**Figure 38: Maximum output without slew-rate induced distortion**

Notice that the above figure is graphed using equation 96 for the OPA277. The example calculation shows the peak voltage for the OPA277 at 40kHz. This can be determined graphically or with the equation.

### Example

$$V_P = \frac{SR}{2\pi f} = \frac{0.8V/\mu s}{2\pi(40kHz)} = 3.18V_{PK} \text{ or } 6.37V_{PP}$$

Large signal response (slew rate)

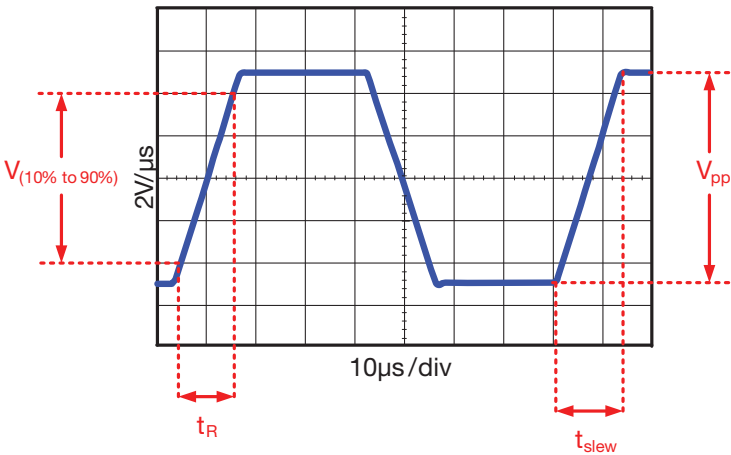


Figure 39: Large signal step response

$$t_R = \frac{V_{(10\% \text{ to } 90\%)}}{SR}$$
 (103) Rise time for large signal step response

$$t_{slew} \approx \frac{V_{pp}}{SR}$$
 (104) Approximate total time for waveform to transition from peak to peak for large signal response

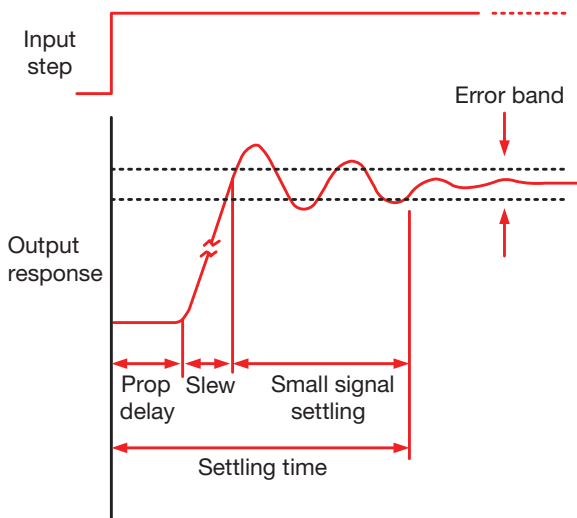
Where

$V_{(10\% \text{ TO } 90\%)}$  = the change in output voltage from 10% to 90% for a step input

$SR$  = the slew rate of the amplifier

$V_{pp}$  = peak-to-peak square wave voltage for a step response

## Settling Time



**Figure 40: Small signal step response**

### Where

Settling time = the time from when an input step is applied until the output settles inside an error guard band. Settling time is measured with a large step (near full scale) input.

Prop delay = propagation delay. The time from when the input step is applied until the output begins to respond

Slew = the output is transitioning at the maximum rate given by the slew rate specification in the amplifier data sheet

## Combining noise sources

$$e_{nT} = \sqrt{(e_{n1})^2 + (e_{n2})^2} \quad (105) \text{ Combining two uncorrelated noise sources}$$

$$e_{nT} = \sqrt{(e_{n1})^2 + (e_{n2})^2 + 2 \cdot C \cdot e_{n1} \cdot e_{n2}} \quad (106) \text{ Combining two correlated noise sources}$$

### Where

$e_{nT}$  = total noise

$e_{n1}$ ,  $e_{n2}$  = noise sources

$C$  = correlation factor, ranges from -1 to +1.  $C = 0$  for uncorrelated sources,  $C = -1$  for inversely correlated, and  $C = +1$  for directly correlated.

## Averaging noise sources

$$e_{nAvg} = \frac{e_n}{\sqrt{N}} \quad (107) \text{ Averaging noise}$$

### Where

$e_{nAvg}$  = the noise amplitude after averaging

$e_n$  = the noise amplitude before averaging

$N$  = the number of averages

Noise bandwidth calculation

$BW_n = K_n \cdot f_c$  (108) Noise bandwidth

Where

$BW_n$  = noise bandwidth of the system  
 $K_n$  = the brick wall correction factor for different filter order  
 $f_c$  = -3 dB bandwidth of the system

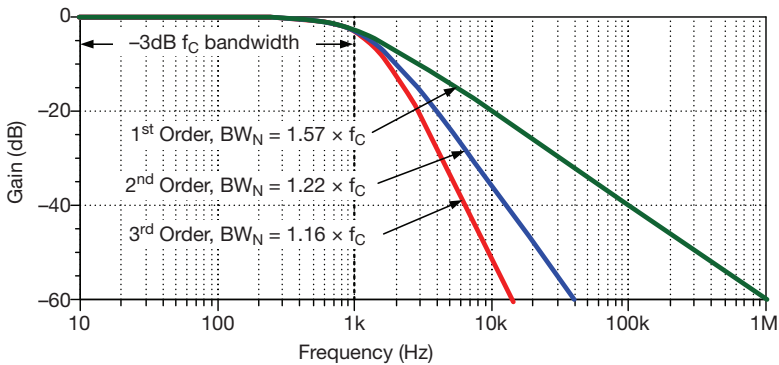


Figure 41: Op amp bandwidth for three different filter orders

Table 17: Brick wall correction factors for noise bandwidth

| Number of poles | $K_n$ brick wall correction factor |
|-----------------|------------------------------------|
| 1               | 1.57                               |
| 2               | 1.22                               |
| 3               | 1.13                               |
| 4               | 1.12                               |

Broadband total noise calculation

$E_{n(BB)} = e_n \cdot \sqrt{BW_n}$  (109) Total RMS noise from broadband

Where

$E_{n(BB)}$  = total RMS noise from broadband noise  
 $e_n$  = broadband noise spectral density ( $nV/\sqrt{Hz}$ )  
 $BW_n$  = noise bandwidth (Hz)

1/f total noise calculation

$$E_{n(\text{normal})} = e_{n(\text{flicker})} \sqrt{f_o}$$

(110) Normalized 1/f noise at 1 Hz

Where

- $E_{n(\text{normal})}$  = 1/f noise normalized to 1 Hz
- $e_{n(\text{flicker})}$  = noise spectral density measured in the 1/f region
- $f_o$  = the frequency at which the 1/f noise  $e_{n(\text{flicker})}$  is measured

$$E_{n(\text{flicker})} = E_{n(\text{normal})} \sqrt{\ln\left(\frac{f_H}{f_L}\right)}$$

(111) 1/f total noise calculation

Where

- $E_{n(\text{flicker})}$  = total RMS noise from flicker
- $E_{n(\text{normal})}$  = 1/f noise normalized to 1Hz
- $f_H$  = upper cutoff frequency or noise bandwidth
- $f_L$  = lower cutoff frequency, normally set to 0.1Hz

Table 18: Peak-to-peak conversion

| Number of standard deviations | Percent chance reading is in range |
|-------------------------------|------------------------------------|
| 2σ (same as ±1σ)              | 68.3%                              |
| 3σ (same as ±1.5σ)            | 86.6%                              |
| 4σ (same as ±2σ)              | 95.4%                              |
| 5σ (same as ±2.5σ)            | 98.8%                              |
| 6σ (same as ±3σ)              | 99.7%                              |
| 6.6σ (same as ±3.3σ)          | 99.9%                              |

## Thermal noise calculation

$$E_{n(R)} = \sqrt{4 \cdot k \cdot T_K \cdot R \cdot BW_n} \quad (112) \text{ Total RMS thermal noise}$$

$$e_{n(R)} = \sqrt{4 \cdot k \cdot T_K \cdot R} \quad (113) \text{ Thermal noise spectral density}$$

### Where

$E_{n(R)}$  = total RMS noise from resistance, also called thermal noise (V RMS)

$e_{n(R)}$  = noise spectral density from resistance, also called thermal noise (V/ $\sqrt{\text{Hz}}$ )

$k$  = Boltzmann's constant  $1.38 \times 10^{-23} \text{ J/K}$

$T_K$  = temperature in Kelvin, to convert degrees Celsius to Kelvin  $T_K = T_C + 273.15$

$BW_n$  = noise bandwidth in Hz

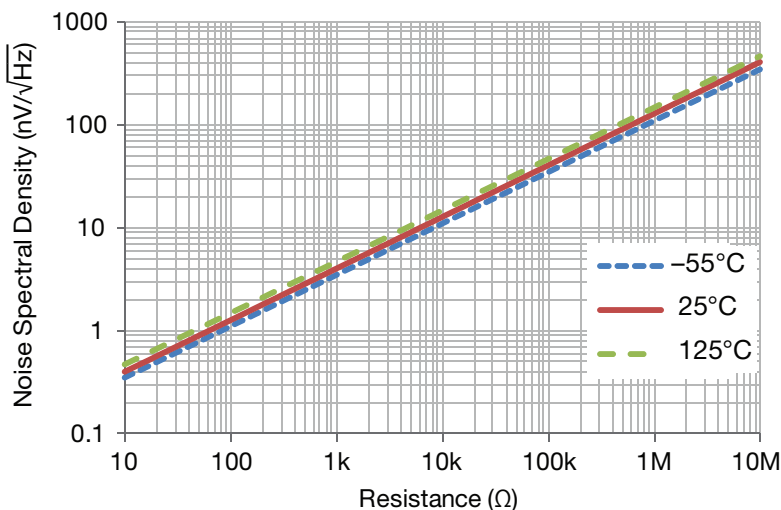


Figure 42: Noise spectral density vs. resistance

Op amp noise model

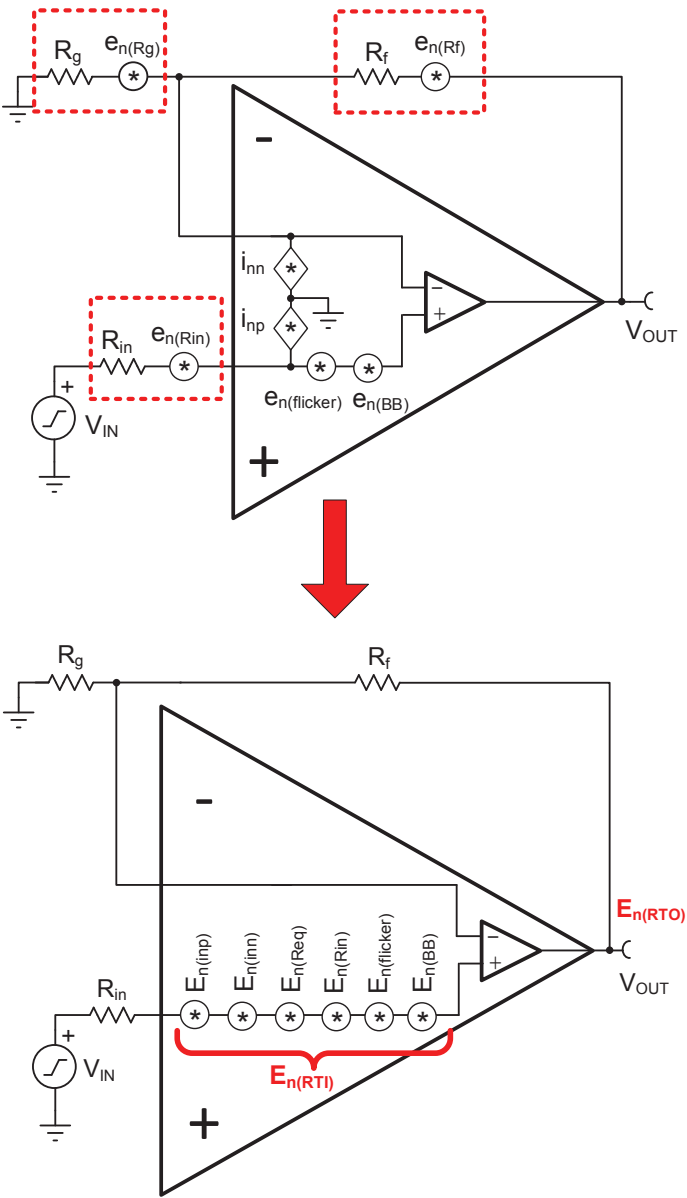


Figure 43: Op amp noise model

## Total noise calculations

$$R_{eq} = \frac{R_f \cdot R_g}{R_f + R_g} \quad (114) \text{ Equivalent feedback resistance}$$

$$e_{n(inn)} = i_{nn} \cdot R_{eq} \quad (115) \text{ Noise RTI from } i_{nn} \text{ flowing into feedback resistors}$$

$$e_{n(inp)} = i_{np} \cdot R_{in} \quad (116) \text{ Noise RTI from } i_{np} \text{ flowing into input resistance}$$

$$e_{n(Req)} = \sqrt{4 \cdot k \cdot T_K \cdot R_{eq}} \quad (117) \text{ Thermal noise RTI from feedback network}$$

$$e_{n(Rin)} = \sqrt{4 \cdot k \cdot T_K \cdot R_{in}} \quad (118) \text{ Thermal noise RTI from input resistor}$$

$$e_{n(BB)} \quad (119) \text{ Broadband noise from data sheet}$$

$$E_n = e_n \cdot \sqrt{BW_n} \quad (120) \text{ General equation to convert spectral density to RMS}$$

$$E_{n(normal)} = e_{n(flicker)} \sqrt{f_o} \quad (121) \text{ Flicker noise normalized to 1Hz}$$

$$E_{n(flicker)} = E_{n(normal)} \cdot \sqrt{\ln\left(\frac{f_H}{f_L}\right)} \quad (122) \text{ Op amp RMS flicker noise}$$

$$E_{n(RTI)} = \sqrt{E_{n(BB)}^2 + E_{n(flicker)}^2 + E_{n(Rin)}^2 + E_{n(Req)}^2 + E_{n(inp)}^2 + E_{n(inn)}^2} \quad (123) \text{ Total noise RTI}$$

$$G_n = \frac{R_f}{R_g} + 1 \quad (124) \text{ Noise gain}$$

$$E_{n(RTO)} = E_{n(RTI)} \cdot G_n \quad (125) \text{ Total noise RTO}$$

**Note 1:** equations above were defined previously

**Note 2:** capital letter (e.g. “E”) indicates RMS noise, and lowercase letter (e.g. “e”) indicate noise density (e.g.  $V / \sqrt{Hz}$ )

RTO = referred to the output

RTI = referred to the input

AC response versus frequency (dominant 2-pole system)

Figure 43 illustrates a bode plot with four different examples of AC peaking.

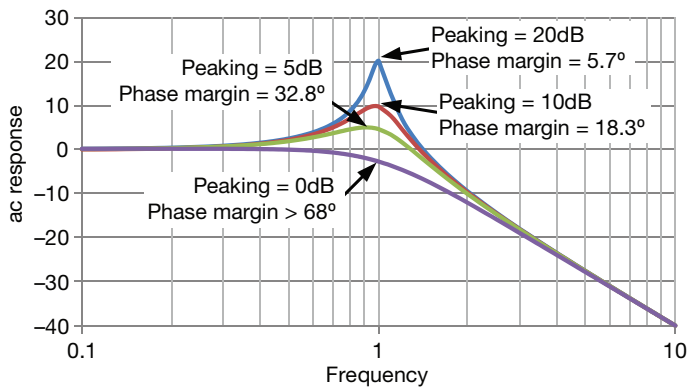


Figure 44: Stability – AC peaking relationship example

Phase margin versus AC peaking

This graph illustrates the phase margin for any given level of AC peaking. Note that 45° of phase margin or greater is required for stable operation.

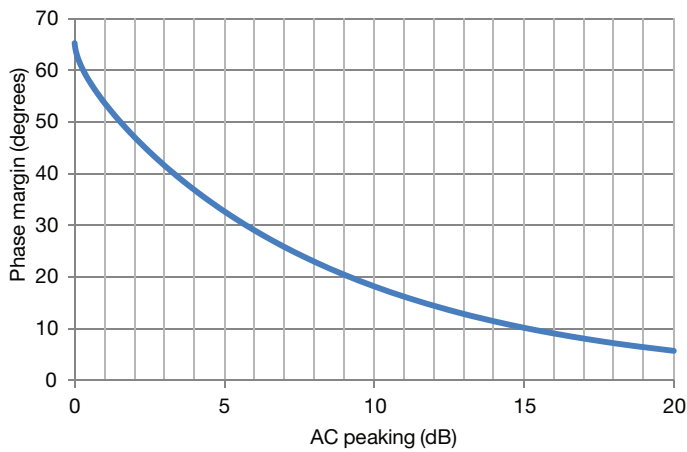


Figure 45: Stability – phase margin vs. peaking for a two-pole system

Transient overshoot (dominant 2-pole system)

Figure 46 illustrates a transient response with two different examples of percentage overshoot.

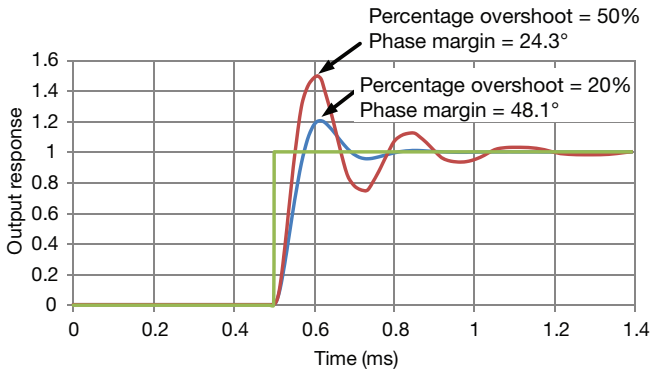


Figure 46: Stability – transient overshoot example

Phase margin versus percentage overshoot

This graph illustrates the phase margin for any given level of transient overshoot. Note that 45° of phase margin or greater is required for stable operation.

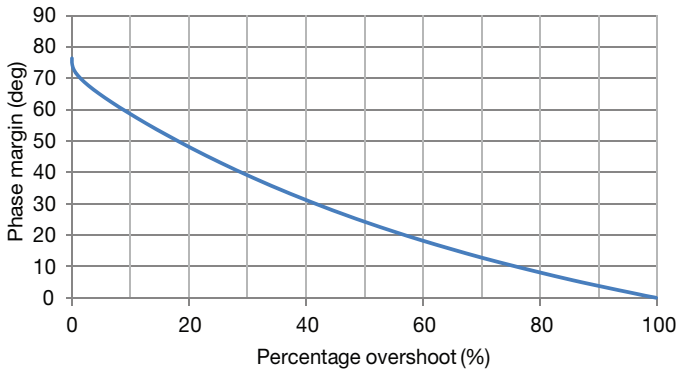
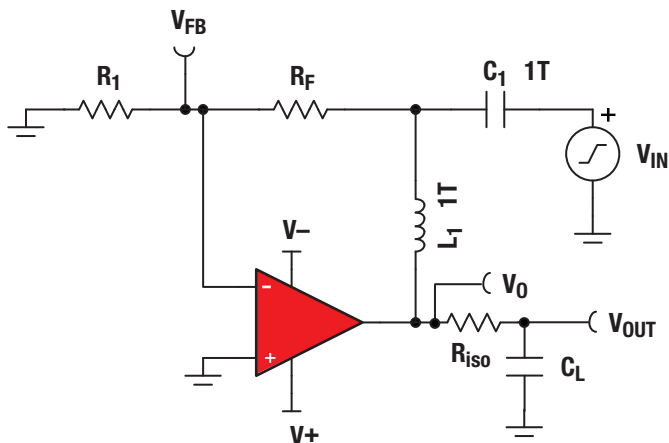


Figure 47: Stability – phase margin vs. percentage overshoot

## Stability open loop SPICE analysis



**Figure 48: Common spice test circuit used for stability**

$$A_{OL\_LOADED} = \frac{V_O}{V_{FB}} \quad (126) \text{ Loaded open-loop gain}$$

$$\beta = V_{FB} \quad (127) \text{ Feedback factor}$$

$$\frac{1}{\beta} = \frac{1}{V_{FB}} \quad (128) \text{ Closed-loop noise gain}$$

$$A_{OL\_LOADED} \times \beta = V_O \quad (129) \text{ Loop gain}$$

### Where

$V_O$  = the voltage at the output of the op amp

$V_{OUT}$  = the voltage output delivered to the load, which may be important to the application but is not considered in stability analysis

$V_{FB}$  = feedback voltage

$R_F$ ,  $R_1$ ,  $R_{iso}$  and  $C_L$  = the op amp feedback network and load.

Other op amp topologies will have different feedback networks; however, the test circuit will be the same for most cases.

Figure 47 shows the exception to the rule (multiple feedback).

$C_1$  and  $L_1$  = components that facilitate SPICE analysis. They are large (1TF, 1TH) to make the circuit closed-loop for DC, but open loop for AC frequencies. SPICE requires closed-loop operation at DC for convergence.

## Stability open loop SPICE analysis (cont.)

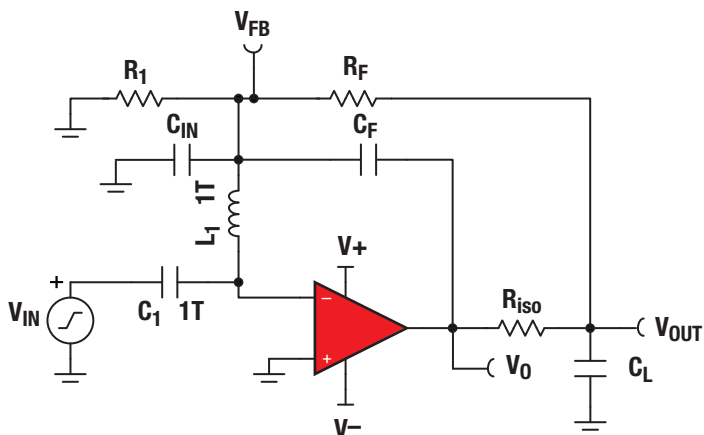


Figure 49: Alternative (multiple feedback) SPICE test circuit used for stability

$$A_{OL\_LOADED} = V_O \quad (130) \text{ Loaded open loop gain}$$

$$\beta = \frac{V_{FB}}{V_O} \quad (131) \text{ Feedback factor}$$

$$\frac{1}{\beta} = \frac{V_O}{V_{FB}} \quad (132) \text{ Closed-loop noise gain}$$

$$A_{OL\_LOADED} \times \beta = V_{FB} \quad (133) \text{ Loop gain}$$

## Where

$V_O$  = the voltage at the output of the op amp

$V_{OUT}$  = the voltage output delivered to the load. This may be important to the application but is not considered in stability analysis.

$V_{FB}$  = feedback voltage

$R_F$ ,  $R_1$ ,  $R_{ISO}$  and  $C_F$  = the op amp feedback network. Because there are two paths for feedback, the loop is broken at the input.

$C_1$  and  $L_1$  = components that facilitate SPICE analysis. They are large (1TF, 1TH) to make the circuit closed loop for DC, but open loop for AC frequencies. SPICE requires closed-loop operation at DC for convergence.

$C_{IN}$  = the equivalent input capacitance taken from the op amp datasheet. This capacitance normally does not need to be added because the model includes it. However, when using this simulation method the capacitance is isolated by the 1TH inductor.

## Stability transient square wave lab test

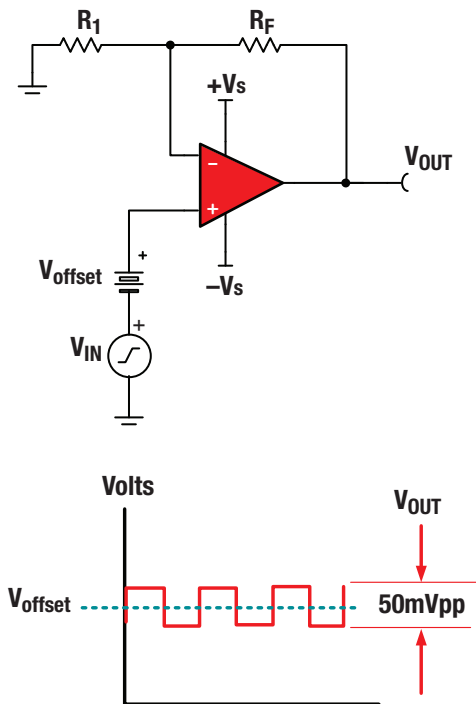


Figure 50: Transient real world stability test

### Test tips

- Choose test frequency  $\ll f_{cl}$
- Small signal ( $V_{pp} \leq 50$  mV) ac output square wave (for example, 1 kHz)
- Adjust  $V_{IN}$  amplitude to yield output  $\leq 50$  mVpp
- Worst case is usually when  $V_{offset} = 0$  (largest  $R_O$ , for  $I_{OUT} = 0A$ )
- Use  $V_{offset}$  as desired to check all output operating points for stability
- Set scope = AC coupled and expand vertical scope scale to look for amount of overshoot, undershoot, and ringing on  $V_{OUT}$
- Use 1x attenuation scope probe on  $V_{OUT}$  for best resolution
- Use percentage overshoot to determine phase margin using Figure 47

## Stability AC sine wave lab test

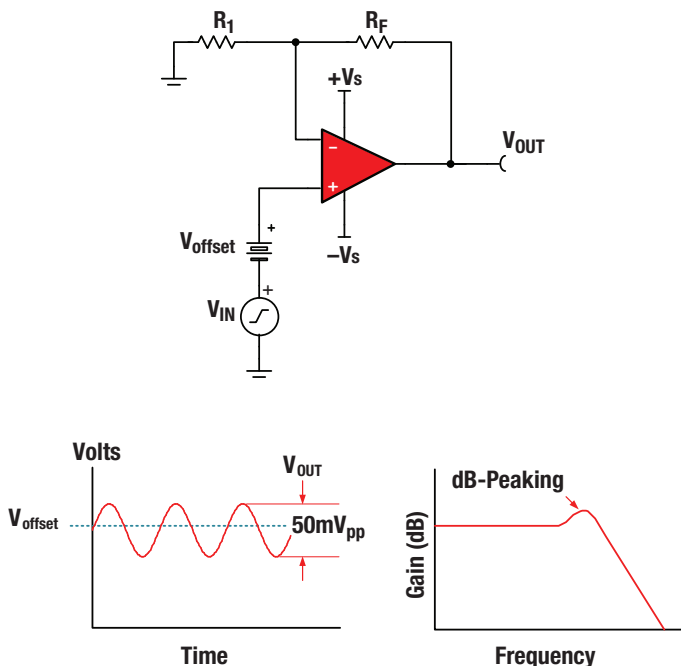
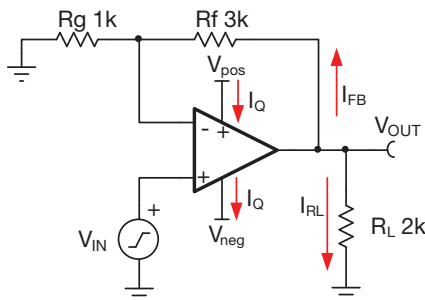


Figure 51: AC sweep real world stability test

## Test tips

- Small signal ( $V_{pp} \leq 50\text{ mV}$ ) AC output sine wave
- Adjust  $V_{IN}$  amplitude to yield output  $\leq 50\text{ mV}_{pp}$
- Worst case is usually when  $V_{offset} = 0$  (largest  $R_O$ , for  $I_{OUT} = 0\text{A}$ )
- Use  $V_{offset}$  as desired to check all output operating points for stability
- Sweep input frequency or use network analyzer to automatically sweep frequency
- Use AC coupling
- Use 1x attenuation scope probe on  $V_{OUT}$  for best resolution
- Use AC peaking in decibels to determine phase margin using Figure 45

## Power dissipation calculation



**Figure 52: Current and power dissipation for non-inverting amplifier**

Non-inverting amplifier power dissipation for specific  $V_{OUT}$

$$I_{RL} = \frac{V_{OUT}}{R_L} \quad (134) \text{ Current through load resistor}$$

$$I_{FB} = \frac{V_{OUT}}{R_F + R_g} \quad (135) \text{ Current through feedback network}$$

$$P_L = (|I_{RL}| + |I_{FB}|)(|V_{sup}| - |V_{OUT}|) \quad (136) \text{ Power dissipated inside op amp from load current.}$$

$V_{sup} = V_{pos}$  if the amplifier is sourcing.  
 $V_{sup} = V_{neg}$  if the amplifier is sinking.

$$P_Q = (V_{pos} - V_{neg}) \cdot I_Q \quad (137) \text{ Total power from quiescent current}$$

$$P_T = P_L + P_Q \quad (138) \text{ Total power dissipated inside the op amp}$$

Non-inverting amplifier maximum power dissipation

$$R_{L\_EQ} = (R_L) \parallel (R_g + R_F) \quad (139) \text{ Equivalent load resistance}$$

$$P_{dc\_max} = \frac{V_{sup}^2}{4 \cdot R_{L\_EQ}} \quad (140) \text{ Maximum DC power dissipation inside the amplifier. Max power occurs when } V_{OUT} = \frac{1}{2} V_{sup}.$$

$V_{sup} = V_{pos} = |V_{neg}|$  for a dual symmetrical supply.  
 $V_{sup} = V_{pos}$  for single supply configuration.

$$P_{ac\_max\_avg} = \frac{2 \cdot V_{sup}^2}{\pi^2 \cdot R_{L\_EQ}} \quad (141) \text{ Maximum AC average power dissipation for a sinusoidal signal on dual supply configuration.}$$

Max average power occurs when the  $V_{OUT\_pk} = (2 \cdot V_{cc} / \pi)$ .  $V_{sup} = V_{pos} = V_{neg}$  for a dual symmetrical supply. For single supply max average AC power is equal to  $P_{dc\_max}$ . This assumes sinewave is centered at mid-supply.

$$T_j = \theta_{ja} \cdot P + T_a \quad (142) \text{ Junction temperature as a function of power and ambient temperature. } T_j = \text{junction temperature. } \theta_{ja} = \text{junction to ambient thermal resistance. } P = P_{dc\_max} \text{ or } P_{ac\_max\_avg} \text{ depending on your application. } T_a = \text{ambient temperature.}$$

## Power dissipation calculation (cont.)

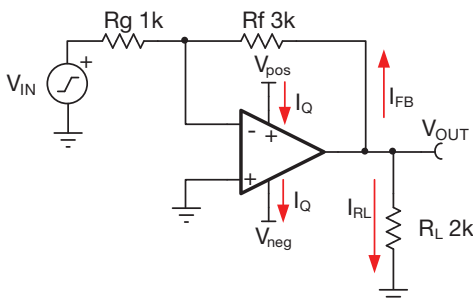


Figure 53: Current and power dissipation for inverting amplifier

Inverting amplifier power dissipation for specific  $V_{OUT}$

$$I_{RL} = \frac{V_{OUT}}{R_L} \quad (143) \text{ Current through load resistor}$$

$$I_{FB} = \frac{V_{OUT}}{R_F} \quad (144) \text{ Current through feedback network}$$

$$P_L = (|I_{RL}| + |I_{FB}|)(|V_{sup}| - |V_{OUT}|) \quad (145) \text{ Power dissipated in op amp from load current, where } V_{sup} = V_{pos} \text{ if the amplifier is sourcing, or } V_{neg} \text{ if the amplifier is sinking}$$

$$P_Q = (V_{pos} - V_{neg}) \cdot I_Q \quad (146) \text{ Total power from quiescent current}$$

$$P_T = P_L + P_Q \quad (147) \text{ Total power dissipated inside the op amp}$$

$$P_{L\_EQ} = (R_L) \parallel (R_F) \quad (148) \text{ Equivalent load resistance}$$

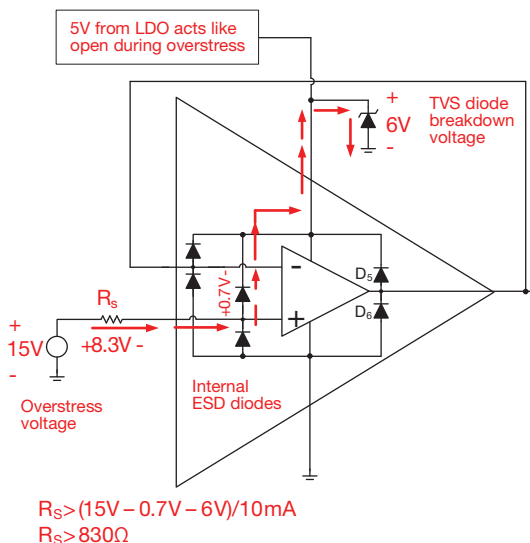
Inverting amplifier maximum power dissipation

$$P_{dc\_max} = \frac{V_{sup}^2}{4 \cdot R_{L\_EQ}} \quad (149) \text{ Maximum DC power dissipation inside the amplifier. Max power occurs when } V_{OUT} = \frac{1}{2} V_{sup}. V_{sup} = V_{pos} = |V_{neg}| \text{ for a dual symmetrical supply. } V_{sup} = V_{pos} \text{ for single supply configuration.}$$

$$P_{ac\_max\_avg} = \frac{2 \cdot V_{sup}^2}{\pi^2 \cdot R_{L\_EQ}} \quad (150) \text{ Maximum AC average power dissipation for a sinusoidal signal on dual supply configuration. Max average power occurs when the } V_{OUT\_pk} = (2 \cdot V_{cc} / \pi). V_{sup} = V_{pos} = V_{neg} \text{ for a dual symmetrical supply. For single supply max average AC power is equal to } P_{dc\_max}. \text{ This assumes sinewave is centered at mid-supply.}$$

$$T_j = \theta_{ja} \cdot P + T_a \quad (151) \text{ Junction temperature as a function of power and ambient temperature. } T_j = \text{junction temperature. } \theta_{ja} = \text{junction to ambient thermal resistance. } P = P_{dc\_max} \text{ or } P_{ac\_max\_avg} \text{ depending on your application. } T_a = \text{ambient temperature.}$$

## Electrical overstress (EOS) protection



**Figure 54: EOS protection during overstress event**

### Method for selecting EOS protection

1. Choose a unidirectional transient voltage suppressor (TVS) diode that has a reverse standoff equal to the normal operating supply voltage. For example, reverse standoff of  $V_R = 5V$ , for an amplifier with a 5V supply. This assures a low TVS diode leakage.
2. Try to find a TVS diode that also breaks down below the absolute maximum rating for the device that is being protected. For example, breakdown of  $V_{BR} \leq 6V$  for an absolute maximum of 6V. Note that this may not always be possible. Choose the lowest breakdown available.
3. Choose a series resistor,  $R_s$ , to limit the current to the absolute maximum input current. This is commonly 10mA for many devices.  
 $R_s > (V_{overstress} - 0.7V - V_{BR})$ . For this example,  
 $R_s = (15V - 0.7V - 6V) = 830\Omega$ .
4. Increase the value of the series resistor for more design margin.

## Electrical overstress (EOS) protection

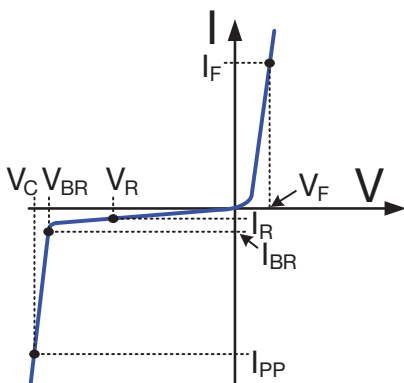


Figure 55: Typical unidirectional TVS I-V curve

### Where

$V_{BR}$  = breakdown voltage

$V_R$  = stand-off voltage. The normal operating voltage with a guaranteed reverse leakage current.

$V_C$  = clamping voltage. The voltage across the TVS when maximum current is flowing.

$V_F$  = forward voltage drop, typically 0.7V for a unipolar TVS diode

$I_{BR}$  = breakdown current @  $V_{BR}$

$I_R$  = reverse leakage @  $V_R$ . Typically in the microamps.

$I_F$  = forward current @  $V_F$

$I_{PP}$  = maximum peak pulse current @  $V_C$ , applied for a limited time (microseconds)

## Notes

[illegible]

## PCB and Wire

- PCB trace resistance for 1oz and 2oz Cu
- Conductor spacing in a PCB for safe operation
- Current carrying capacity of copper conductors
- Package types and dimensions
- PCB trace capacitance and inductance
- PCB via capacitance and inductance
- Common coaxial cable specifications
- Coaxial cable equations
- Resistance per length for wire types
- Maximum current for wire types

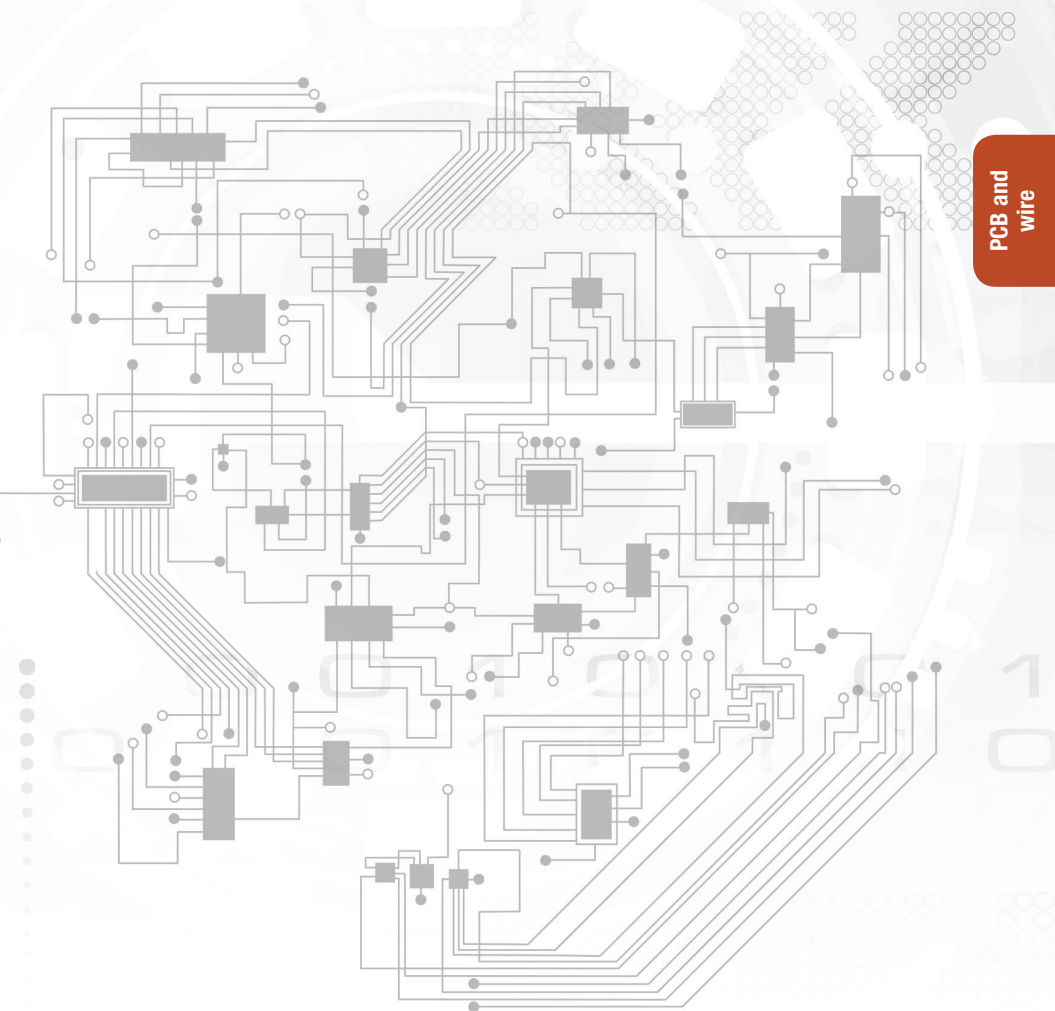
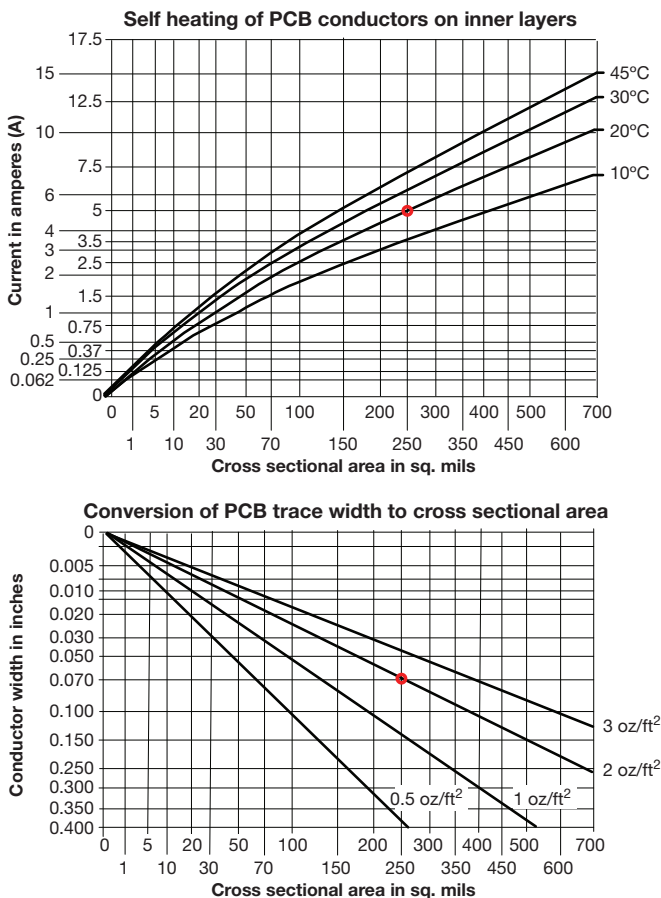


Table 19: Printed circuit board conductor spacing

| Voltage between<br>conductors<br>(DC or AC<br>peaks) | Minimum spacing         |                        |                       |                         |                         |                         |                         |
|------------------------------------------------------|-------------------------|------------------------|-----------------------|-------------------------|-------------------------|-------------------------|-------------------------|
|                                                      | Bare board              |                        |                       |                         | Assembly                |                         |                         |
|                                                      | B1                      | B2                     | B3                    | B4                      | A5                      | A6                      | A7                      |
| 0-15                                                 | 0.05 mm<br>[0.00197 in] | 0.1 mm<br>[0.0039 in]  | 0.1 mm<br>[0.0039 in] | 0.05 mm<br>[0.00197 in] | 0.13 mm<br>[0.00512 in] | 0.13 mm<br>[0.00512 in] | 0.13 mm<br>[0.00512 in] |
| 16-30                                                | 0.05 mm<br>[0.00197 in] | 0.1 mm<br>[0.0039 in]  | 0.1 mm<br>[0.0039 in] | 0.05 mm<br>[0.00197 in] | 0.13 mm<br>[0.00512 in] | 0.25 mm<br>[0.00984 in] | 0.13 mm<br>[0.00512 in] |
| 31-50                                                | 0.1 mm<br>[0.0039 in]   | 0.6 mm<br>[0.024 in]   | 0.6 mm<br>[0.024 in]  | 0.13 mm<br>[0.00512 in] | 0.13 mm<br>[0.00512 in] | 0.4 mm<br>[0.016 in]    | 0.13 mm<br>[0.00512 in] |
| 51-100                                               | 0.1 mm<br>[0.0039 in]   | 0.6 mm<br>[0.024 in]   | 1.5 mm<br>[0.0591 in] | 0.13 mm<br>[0.00512 in] | 0.13 mm<br>[0.00512 in] | 0.5 mm<br>[0.020 in]    | 0.13 mm<br>[0.00512 in] |
| 101-150                                              | 0.2 mm<br>[0.0079 in]   | 0.6 mm<br>[0.024 in]   | 3.2 mm<br>[0.126 in]  | 0.4 mm<br>[0.016 in]    | 0.4 mm<br>[0.016 in]    | 0.8 mm<br>[0.031 in]    | 0.4 mm<br>[0.016 in]    |
| 151-170                                              | 0.2 mm<br>[0.0079 in]   | 1.25 mm<br>[0.0492 in] | 3.2 mm<br>[0.126 in]  | 0.4 mm<br>[0.016 in]    | 0.4 mm<br>[0.016 in]    | 0.8 mm<br>[0.031 in]    | 0.4 mm<br>[0.016 in]    |
| 171-250                                              | 0.2 mm<br>[0.0079 in]   | 1.25 mm<br>[0.0492 in] | 6.4 mm<br>[0.252 in]  | 0.4 mm<br>[0.016 in]    | 0.4 mm<br>[0.016 in]    | 0.8 mm<br>[0.031 in]    | 0.4 mm<br>[0.016 in]    |
| 251-300                                              | 0.2 mm<br>[0.0079 in]   | 1.25 mm<br>[0.0492 in] | 12.5 mm<br>[0.492 in] | 0.4 mm<br>[0.016 in]    | 0.4 mm<br>[0.016 in]    | 0.8 mm<br>[0.031 in]    | 0.8 mm<br>[0.031 in]    |
| 301-500                                              | 0.25 mm<br>[0.00984 in] | 2.5 mm<br>[0.0984 in]  | 12.5 mm<br>[0.492 in] | 0.8 mm<br>[0.031 in]    | 0.8 mm<br>[0.031 in]    | 1.5 mm<br>[0.0591 in]   | 0.8 mm<br>[0.031 in]    |

- Where
- B1 = internal conductors
  - B2 = external conductors uncoated sea level to 3050m
  - B3 = external conductors uncoated above 3050m
  - B4 = external conductors coated with permanent polymer coating (any elevation)
  - A5 = external conductors with conformal coating over assembly (any elevation)
  - A6 = external component lead/termination, uncoated, sea level to 3050m
  - A7 = external component lead termination, with conformal coating (any elevation)

Extracted with permission from IPC-2221B, Table 6-1  
For additional information, the entire specification can be downloaded at [www.ipc.org](http://www.ipc.org)



**Figure 56: Self heating of PCB traces on inside layer**

### Example

Find the current that will cause a 20°C temperature rise in a PCB trace that is 0.1 inch wide and uses 2 oz/ft<sup>2</sup> copper. (Assume traces are on inner layer of PCB.)

### Answer

First translate 0.1 inch to 250 sq. mils. using bottom chart. Next find the current associated with 20°C and 250 sq. mils. using top chart (Answer = 5A).

Extracted with permission from IPC-2152, Figure 5-1

For additional information the entire specification can be downloaded at [www.ipc.org](http://www.ipc.org)

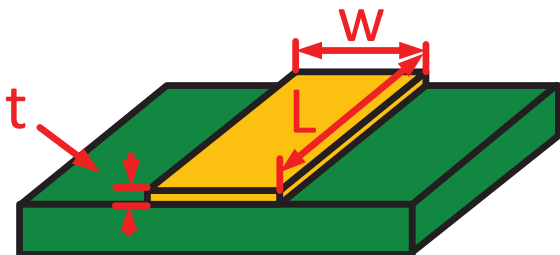


Figure 57: PCB trace resistance

$$R = \rho \frac{L}{t \cdot W} [1 + \alpha(T - 25^\circ\text{C})] \quad (152) \text{ Trace resistance}$$

**Where**

$\rho$  = resistivity of trace (for copper =  $17 \cdot 10^{-6} \Omega \cdot \text{mm}$ )

$\alpha$  = temperature coefficient (for copper =  $3.9 \cdot 10^{-3} / ^\circ\text{C}$ )

$L, W$  = length and width of trace in mm or mil. Note:  $L$  and  $W$  must both be in the same units.

$t$  = thickness of trace in mm (1 oz copper = 0.0348mm, 2 oz copper = 0.0696mm)

$T$  = temperature in  $^\circ\text{C}$

**Example**

What is the resistance of a 20 mil long, 5 mil wide trace for a 1 oz Cu thickness at  $25^\circ\text{C}$  and  $125^\circ\text{C}$ ?

**Answer**

$R_{25^\circ\text{C}} = 1.95\text{m}\Omega$ ,  $R_{125^\circ\text{C}} = 2.72\text{m}\Omega$

$$R = (17 \cdot 10^{-6} \Omega \cdot \text{mm}) \frac{20\text{mil}}{(0.0348\text{mm}) \cdot 5\text{mil}} [1 + 3.9 \cdot 10^{-3} / ^\circ\text{C} (125^\circ\text{C} - 25^\circ\text{C})] = 2.72\text{m}\Omega$$

PCB trace resistance for 1 oz-Cu

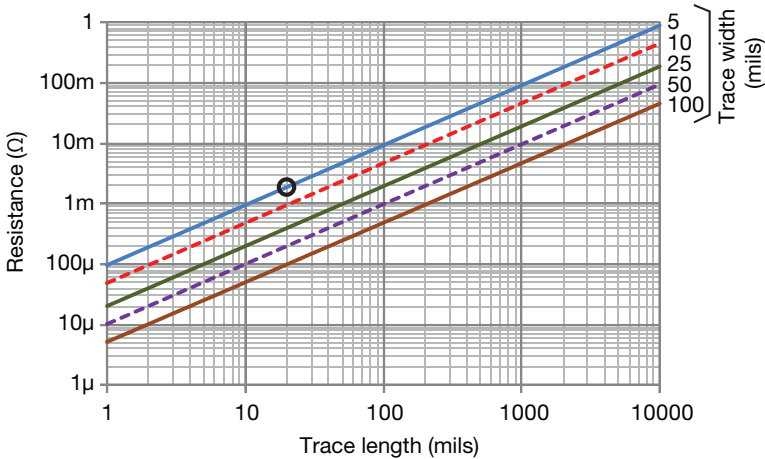


Figure 58: PCB trace resistance vs. length and width for 1 oz-Cu, 25°C

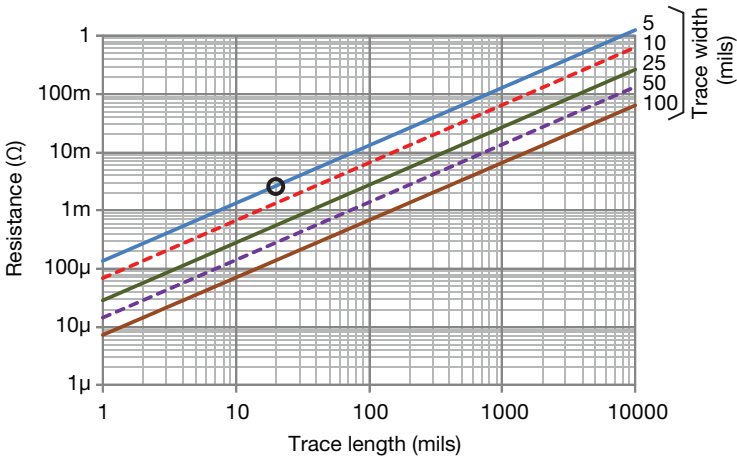


Figure 59: PCB trace resistance vs. length and width for 1 oz-Cu, 125°C

Example

What is the resistance of a 20 mil long, 5 mil wide trace for a 1 oz-Cu thickness at 25°C and 125°C?

Answer

R25C = 2 m $\Omega$ , R125C = 3 m $\Omega$ . The points are circled on the curves.

PCB trace resistance for 2 oz-Cu

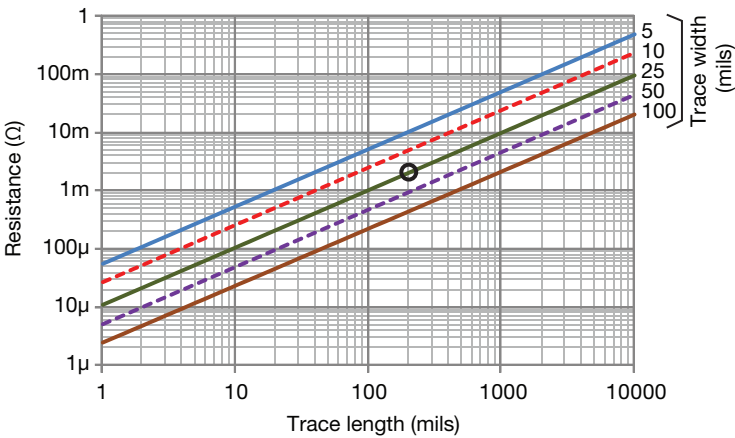


Figure 60: PCB trace resistance vs. length and width for 2 oz-Cu, 25°C

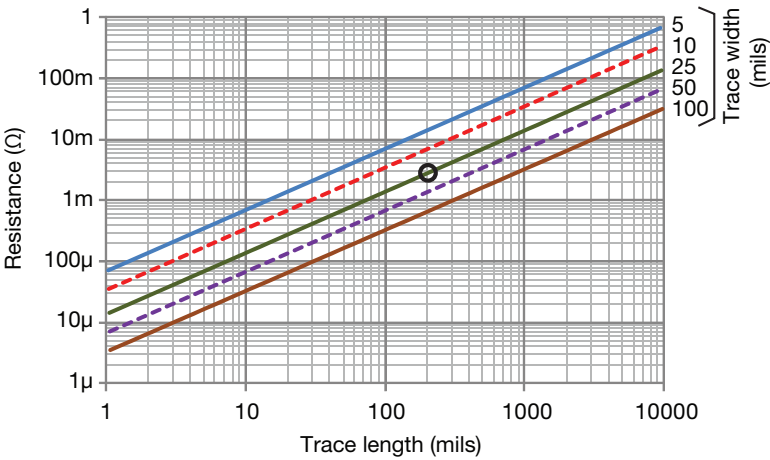


Figure 61: PCB trace resistance vs. length and width for 2 oz-Cu, 125°C

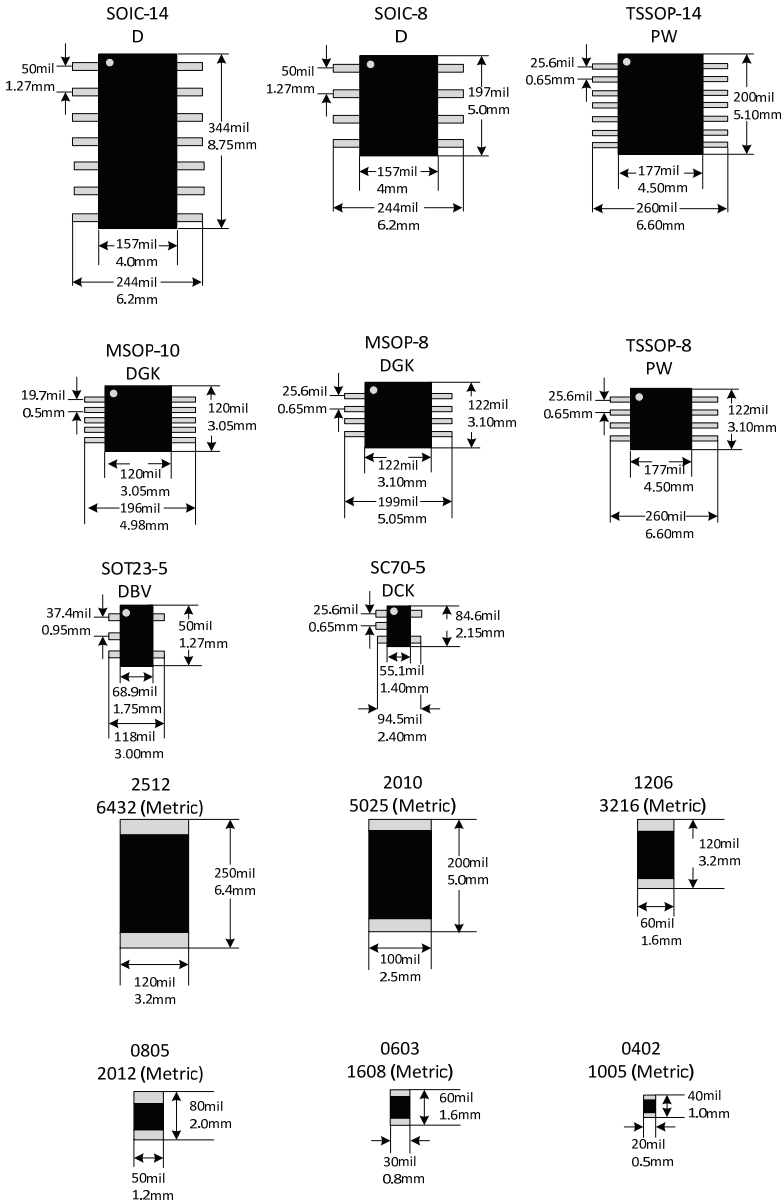
Example

What is the resistance of a 200 mil long, 25 mil wide trace for a 2 oz-Cu thickness at 25°C and 125°C?

Answer

R25C = 2 m $\Omega$ , R125C = 3 m $\Omega$ . The points are circled on the curves.

Common package type and dimensions



## PCB parallel plate capacitance

$$C(\text{pF}) = \frac{k \cdot l \cdot w \cdot \epsilon_r}{h} \quad (153) \text{ Capacitance for parallel copper planes}$$

## Where

$k$  = permittivity of free space.

Both the metric and imperial version of the constant are given.

$k = 8.854 \times 10^{-3} \text{ pF/mm}$ , or  $2.247 \times 10^{-4} \text{ pF/mil}$

$l$  = length (metric in mm, or imperial in mil)

$w$  = width (metric in mm, or imperial in mil)

$h$  = separation between planes (metric in mm, or imperial in mil)

$\epsilon_r$  = PCB relative dielectric constant ( $\epsilon_r \approx 4.5$  for FR-4)

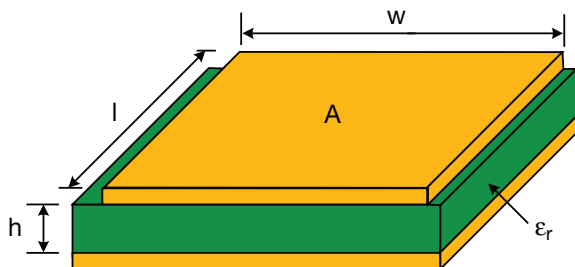


Figure 62: PCB parallel plate capacitance

## Example

Calculate the total capacitance if  $l = 5.08\text{mm}$ ,  $w = 12.7\text{mm}$ ,  $h = 1.575\text{mm}$ , and  $\epsilon_r = 4.5$ .

## Answer

$$C(\text{pF}) = \frac{(8.854 \times 10^{-3} \text{ pF/mm}) \times 5.08\text{mm} \times 12.7\text{mm} \times 4.5}{1.575\text{mm}} = 1.63\text{pF}$$

## Example

Calculate the total capacitance if  $l = 200\text{mil}$ ,  $w = 500\text{mil}$ ,  $h = 62\text{mil}$ , and  $\epsilon_r = 4.5$ .

## Answer

$$C(\text{pF}) = \frac{(2.247 \times 10^{-4} \text{ pF/mil}) \times 200\text{mil} \times 500\text{mil} \times 4.5}{62\text{mil}} = 1.63\text{pF}$$

## PCB microstrip capacitance and inductance

$$L(\text{nH}) = k_L \cdot l \cdot \ln\left(\frac{5.98 \cdot h}{0.8 \cdot w + t}\right) \quad (154) \text{ Inductance for microstrip}$$

$$C(\text{pF}) = \frac{k_C \cdot l \cdot (\epsilon_r + 1.41)}{\ln\left(\frac{5.98 \cdot h}{0.8 \cdot w + t}\right)} \quad (155) \text{ Capacitance for microstrip}$$

$$Z_0 = \sqrt{\frac{L}{C}} = \frac{87\Omega}{\sqrt{(\epsilon_r + 1.41)}} \cdot \ln\left(\frac{5.98 \cdot h}{0.8 \cdot w + t}\right) \quad (156) \text{ Characteristic impedance for microstrip}$$

### Where

$k_L$  = PCB inductance per unit length.

Both the metric and imperial version of the constant are given.

$k_L = 2\text{nH/cm}$ , or  $5.071\text{nH/in}$

$k_C$  = PCB capacitance per unit length.

Both the metric and imperial version of the constant are given.

$k_C = 0.264\text{pF/cm}$ , or  $0.67056\text{pF/in}$

$l$  = length of microstrip (metric in cm, or imperial in inches)

$w$  = width of microstrip (metric in mm, or imperial in mil)

$t$  = thickness of copper (metric in mm, or imperial in mil)

$h$  = separation between planes (metric in mm, or imperial in mil)

$\epsilon_r$  = PCB dielectric constant ( $\epsilon_r \approx 4.5$  for FR-4)

For imperial:  
Copper thickness (mils) =  
 $1.37 \times (\text{number of ounces})$   
i.e. 1oz Cu = 1.37mils  
i.e. ½oz Cu = 0.684mils

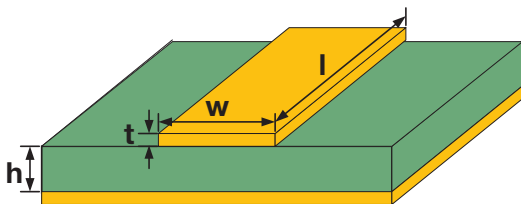


Figure 63: PCB Microstrip capacitance and inductance

### Example

Calculate the total inductance and capacitance if  $l = 2.54\text{cm}$ ,  $w = 0.254\text{mm}$ ,  $t = 0.0356\text{mm}$ ,  $h = 0.8\text{mm}$ , and  $\epsilon_r = 4.5$  for FR-4.

### Answer

$$L(\text{nH}) = (2\text{nH/cm}) \cdot (2.54\text{cm}) \cdot \ln\left(\frac{5.98 \cdot 0.8\text{mm}}{0.8 \cdot 0.254\text{mm} + 0.0356\text{mm}}\right) = 15.2\text{nH}$$

$$C(\text{pF}) = \frac{(0.264\text{pF/cm}) \cdot (2.54\text{cm}) \cdot (4.5 + 1.41)}{\ln\left(\frac{5.98 \cdot 0.8\text{mm}}{0.8 \cdot 0.254\text{mm} + 0.0356\text{mm}}\right)} = 1.3\text{pF}$$

## PCB adjacent copper traces

$$C(\text{pF}) \approx \frac{k \cdot t \cdot l}{d} \quad (157) \text{ Same layer}$$

$$C(\text{pF}) \approx \frac{k \cdot \epsilon_r \cdot w \cdot l}{h} \quad (158) \text{ Different layers}$$

## Where

$l$  = length of the copper trace (mil or mm)

$k = 8.854 \times 10^{-3} \text{pF/mm}$ , or  $k = 2.247 \times 10^{-4} \text{pF/mil}$

$t$  = thickness of trace (mil or mm)

$d$  = distance between traces if on same layer (mil or mm)

$w$  = width of trace (mil or mm)

$h$  = separation between planes (mil or mm)

$\epsilon_r$  = PCB dielectric constant ( $\epsilon_r \approx 4.5$  for FR-4)

For imperial:  
Copper thickness (mils) =  
 $1.37 \times (\text{number of ounces})$   
i.e. 1oz Cu = 1.37mils  
i.e. ½oz Cu = 0.684mils

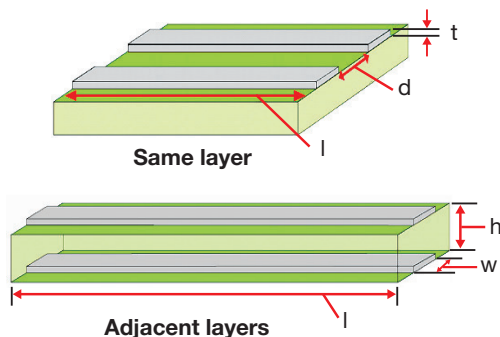


Figure 64: Capacitance for adjacent copper traces

## Example

Calculate the total capacitance for both cases if  $l = 2.54\text{mm}$ ,  $t = 0.0348\text{mm}$ ,  $d = 0.254\text{mm}$ ,  $w = 0.635\text{mm}$ ,  $h = 1.6\text{mm}$ , and  $\epsilon_r = 4.5$  for FR-4.

## Answer

$$C(\text{pF}) \approx \frac{(8.854 \times 10^{-3} \text{pF/mm})(0.0348\text{mm})(2.54\text{mm})}{0.254\text{mm}} = 0.0031\text{pF} \quad (\text{same layer})$$

$$C(\text{pF}) \approx \frac{(8.854 \times 10^{-3} \text{pF/mm})(4.5\text{mm})(0.635\text{mm})(2.54\text{mm})}{1.6\text{mm}} = 0.04\text{pF} \quad (\text{adjacent layers})$$

## Example

Calculate the total capacitance for both cases if  $l = 100\text{mil}$ ,  $t = 1.37\text{mil}$ ,  $d = 10\text{mil}$ ,  $w = 25\text{mil}$ ,  $h = 63\text{mil}$ , and  $\epsilon_r = 4.5$  for FR-4.

## Answer

$C = 0.0031\text{pF}$  (same layer),  $C = 0.4\text{pF}$  (adjacent layers). Note: this is the same example as above with imperial units.

## PCB via capacitance and inductance

$$L(\text{nH}) \approx k_L \cdot h \left[ 1 + \ln \left( \frac{4h}{d} \right) \right] \quad (159) \text{ Inductance for via}$$

$$C(\text{pF}) \approx \frac{k_C \cdot \epsilon_r \cdot h \cdot d_1}{d_2 - d_1} \quad (160) \text{ Capacitance for via}$$

### Where

$k_L$  = PCB inductance per unit length.

Both the metric and imperial version of the constant are given.

$k_L = 0.2\text{nH/mm}$ , or  $5.076 \times 10^{-3}\text{nH/mil}$

$k_C$  = PCB capacitance per unit length.

Both the metric and imperial version of the constant are given.

$k_C = 0.0555\text{pF/mm}$ , or  $1.41 \times 10^{-3}\text{pF/mil}$

$h$  = separation between planes

$d$  = diameter of via hole

$d_1$  = diameter of the pad surrounding the via

$d_2$  = distance to inner layer ground plane

$\epsilon_r$  = PCB dielectric constant ( $\epsilon_r \approx 4.5$  for FR-4)

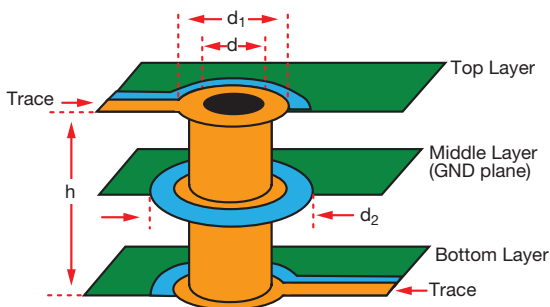


Figure 65: Inductance and capacitance of via

### Example

Calculate the total inductance and capacitance if  $h = 1.6\text{mm}$ ,  $d = 0.4\text{mm}$ ,  $d_1 = 0.8\text{mm}$ , and  $d_2 = 1.5\text{mm}$ .

### Answer

$$L(\text{nH}) \approx (0.2\text{nH/mm}) \cdot (1.6\text{mm}) \left[ 1 + \ln \left( \frac{4 \cdot 1.6\text{mm}}{0.4\text{mm}} \right) \right] = 1.2\text{nH}$$

$$C(\text{pF}) \approx \frac{(0.0555\text{pF/mm}) \cdot (4.5) \cdot (1.6\text{mm}) \cdot (0.8\text{mm})}{1.5\text{mm} - 0.8\text{mm}} = 0.46\text{pF}$$

### Example

Calculate the total inductance and capacitance if  $h = 63\text{mil}$ ,  $d = 15.8\text{mil}$ ,  $d_1 = 31.5\text{mil}$ , and  $d_2 = 59\text{mil}$ .

### Answer

$L = 1.2\text{nH}$ ,  $C = 0.46\text{pF}$ . Note: this is the same example as above with imperial units.

Table 20: Coaxial cable information

| Type     | $Z_0$         | Capacitance / length (pF/feet) | Outside diameter (inches) | dB attenuation /100 ft at 750 MHz | Dielectric type | Application                                                                                                                                  |
|----------|---------------|--------------------------------|---------------------------|-----------------------------------|-----------------|----------------------------------------------------------------------------------------------------------------------------------------------|
| RG-58    | 53.5 $\Omega$ | 28.8                           | 0.195                     | 13.1                              | PE              | Test equipment and RF power to a few hundred watts, and a couple hundred MHz                                                                 |
| RG-8     | 52 $\Omega$   | 29.6                           | 0.405                     | 5.96                              | PE              | RF power to a few kW, up to several hundred MHz                                                                                              |
| RG-214/U | 50 $\Omega$   | 30.8                           | 0.425                     | 6.7                               | PE              |                                                                                                                                              |
| 9914     | 50 $\Omega$   | 26.0                           | 0.405                     | 4.0                               | PE              |                                                                                                                                              |
| RG-6     | 75 $\Omega$   | 20                             | 0.270                     | 5.6                               | PF              | Video and CATV applications. RF to a few hundred watts, up to a few hundred MHz, sometimes to higher frequencies if losses can be tolerated. |
| RG-59/U  | 73 $\Omega$   | 29                             | 0.242                     | 9.7                               | PE              |                                                                                                                                              |
| RG-11/U  | 75 $\Omega$   | 17                             | 0.412                     | 3.65                              | PE              | RF power to a few kW, up to several hundred MHz                                                                                              |
| RG-62/U  | 93 $\Omega$   | 13.5                           | 0.242                     | 7.1                               | ASP             | Used in some test equipment and 100 $\Omega$ video applications                                                                              |
| RG-174   | 50 $\Omega$   | 31                             | 0.100                     | 23.5                              | PE              | Miniature coax used primarily for test equipment interconnection. Usually short runs due to higher loss.                                     |
| RG-178/U | 50 $\Omega$   | 29                             | 0.071                     | 42.7                              | ST              |                                                                                                                                              |

## Coaxial cable equations

$$\frac{C}{l} = \frac{2\pi\epsilon}{\ln\left(\frac{D}{d}\right)} \quad (161) \text{ Capacitance per length}$$

$$\frac{L}{l} = \frac{\mu}{2\pi} \ln\left(\frac{D}{d}\right) \quad (162) \text{ Inductance per length}$$

$$Z_o = \sqrt{\frac{L}{C}} = \frac{1}{2\pi} \cdot \sqrt{\frac{\mu}{\epsilon}} \cdot \ln\left(\frac{D}{d}\right) \quad (163) \text{ Characteristic impedance}$$

### Where

L = inductance in henries (H)

C = capacitance in farads (F)

Z = impedance in ohms ( $\Omega$ )

d = diameter of inner conductor

D = inside diameter of shield, or diameter of dielectric insulator

$\epsilon$  = dielectric constant of insulator ( $\epsilon = \epsilon_r \epsilon_o$ )

$\mu$  = magnetic permeability ( $\mu = \mu_r \mu_o$ )

l = length of the cable

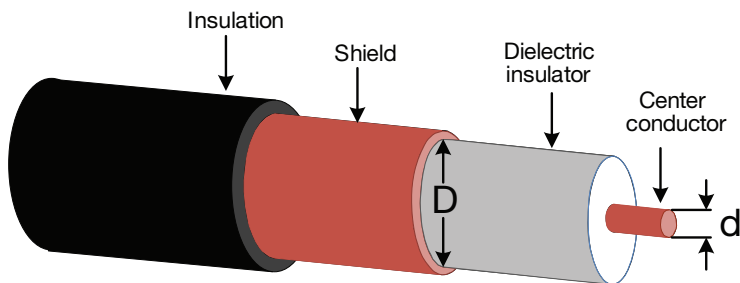


Figure 66: Coaxial cable cutaway

Table 21: Resistance per length for different wire types (AWG)

| AWG | Stds  | Outside diameter |       | Area          |                 | DC resistance |        |
|-----|-------|------------------|-------|---------------|-----------------|---------------|--------|
|     |       | in               | mm    | circular mils | mm <sup>2</sup> | Ω / 1000 ft   | Ω / km |
| 36  | Solid | 0.005            | 0.127 | 25            | 0.013           | 445           | 1460   |
| 36  | 7/44  | 0.006            | 0.152 | 28            | 0.014           | 371           | 1271   |
| 34  | Solid | 0.0063           | 0.160 | 39.7          | 0.020           | 280           | 918    |
| 34  | 7/42  | 0.0075           | 0.192 | 43.8          | 0.022           | 237           | 777    |
| 32  | Solid | 0.008            | 0.203 | 67.3          | 0.032           | 174           | 571    |
| 32  | 7/40  | 0.008            | 0.203 | 67.3          | 0.034           | 164           | 538    |
| 30  | Solid | 0.010            | 0.254 | 100           | 0.051           | 113           | 365    |
| 30  | 7/38  | 0.012            | 0.305 | 112           | 0.057           | 103           | 339    |
| 28  | Solid | 0.013            | 0.330 | 159           | 0.080           | 70.8          | 232    |
| 28  | 7/36  | 0.015            | 0.381 | 175           | 0.090           | 64.9          | 213    |
| 26  | Solid | 0.016            | 0.409 | 256           | 0.128           | 43.6          | 143    |
| 26  | 10/36 | 0.021            | 0.533 | 250           | 0.128           | 41.5          | 137    |
| 24  | Solid | 0.020            | 0.511 | 404           | 0.205           | 27.3          | 89.4   |
| 24  | 7/32  | 0.024            | 0.610 | 448           | 0.229           | 23.3          | 76.4   |
| 22  | Solid | 0.025            | 0.643 | 640           | 0.324           | 16.8          | 55.3   |
| 22  | 7/30  | 0.030            | 0.762 | 700           | 0.357           | 14.7          | 48.4   |
| 20  | Solid | 0.032            | 0.813 | 1020          | 0.519           | 10.5          | 34.6   |
| 20  | 7/28  | 0.038            | 0.965 | 1111          | 0.562           | 10.3          | 33.8   |
| 18  | Solid | 0.040            | 1.020 | 1620          | 0.823           | 6.6           | 21.8   |
| 18  | 7/26  | 0.048            | 1.219 | 1770          | 0.902           | 5.9           | 19.2   |
| 16  | Solid | 0.051            | 1.290 | 2580          | 1.310           | 4.2           | 13.7   |
| 16  | 7/24  | 0.060            | 1.524 | 2828          | 1.442           | 3.7           | 12.0   |
| 14  | Solid | 0.064            | 1.630 | 4110          | 2.080           | 2.6           | 8.6    |
| 14  | 7/22  | 0.073            | 1.854 | 4480          | 2.285           | 2.3           | 7.6    |

Table 22: Maximum current vs. AWG

| Wire gauge | Polyethylene<br>Neoprene<br>Polyvinylchloride<br>(semi-ridged) at 80°C | Polypropylene<br>Polyethylene<br>(high density) at 90°C | Polyvinylchloride Nylon at<br>105°C | Kynar<br>Polyethylene<br>Thermoplastic at 125°C | Kapton<br>Teflon<br>Silicone at 200°C |
|------------|------------------------------------------------------------------------|---------------------------------------------------------|-------------------------------------|-------------------------------------------------|---------------------------------------|
| AWG        | I <sub>max</sub> (A)                                                   | I <sub>max</sub> (A)                                    | I <sub>max</sub> (A)                | I <sub>max</sub> (A)                            | I <sub>max</sub> (A)                  |
| 30         | 2                                                                      | 3                                                       | 3                                   | 3                                               | 4                                     |
| 28         | 3                                                                      | 4                                                       | 4                                   | 5                                               | 6                                     |
| 26         | 4                                                                      | 5                                                       | 5                                   | 6                                               | 7                                     |
| 24         | 6                                                                      | 7                                                       | 7                                   | 8                                               | 10                                    |
| 22         | 8                                                                      | 9                                                       | 10                                  | 11                                              | 13                                    |
| 20         | 10                                                                     | 12                                                      | 13                                  | 14                                              | 17                                    |
| 18         | 15                                                                     | 17                                                      | 18                                  | 20                                              | 24                                    |
| 16         | 19                                                                     | 22                                                      | 24                                  | 26                                              | 32                                    |
| 14         | 27                                                                     | 30                                                      | 33                                  | 40                                              | 45                                    |
| 12         | 36                                                                     | 40                                                      | 45                                  | 50                                              | 55                                    |
| 10         | 47                                                                     | 55                                                      | 58                                  | 70                                              | 75                                    |

Note: The table shows the current required to raise the temperature of a single insulated conductor in free air (30°C ambient) to the limits of various insulation types.

Example

What is the maximum current that can be applied to a 30 gauge Teflon wire in a room temperature environment? What will the self-heating be?

Answer

I<sub>max</sub> = 4A  
Wire temperature = 200°C

## Notes

This image shows a full page of white paper with horizontal ruling lines. The lines are evenly spaced and extend across the width of the page, providing a template for writing or drawing. There are no margins, text, or other markings on the page.

## Sensor

- Thermistor •
- Resistive temperature detector (RTD) •
- Diode temperature characteristics •
- Thermocouple (J and K) •



Table 23: Temperature sensor overview

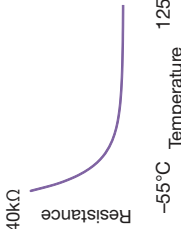
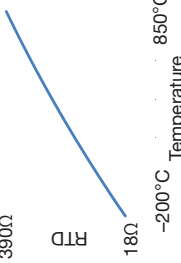
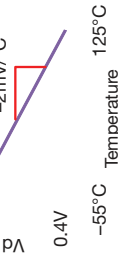
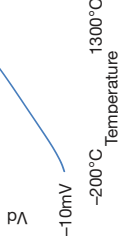
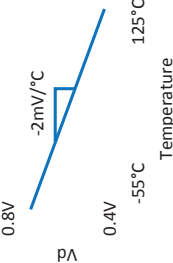
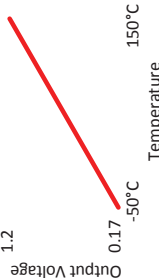
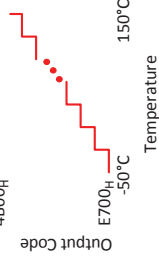
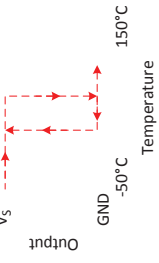
|              | Thermistor                                                                                                                                                                | RTD                                                                                                                                                                | Diode                                                                                                                                                                           | Thermocouple                                                                                                                                                        |
|--------------|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------|--------------------------------------------------------------------------------------------------------------------------------------------------------------------|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|---------------------------------------------------------------------------------------------------------------------------------------------------------------------|
|              |  <p>Resistance</p> <p>40kΩ</p> <p>18Ω</p> <p>Temperature</p> <p>-55°C</p> <p>125°C</p> |  <p>RTD</p> <p>390Ω</p> <p>18Ω</p> <p>Temperature</p> <p>-200°C</p> <p>850°C</p> |  <p>Vd</p> <p>0.8V</p> <p>0.4V</p> <p>Temperature</p> <p>-55°C</p> <p>125°C</p> <p>-2mV/°C</p> |  <p>Vd</p> <p>80mV</p> <p>-10mV</p> <p>Temperature</p> <p>-200°C</p> <p>1300°C</p> |
| Temp range   | -55°C < T < 150°C                                                                                                                                                         | -200°C < T < 850°C                                                                                                                                                 | -55°C < T < 150°C                                                                                                                                                               | -250°C < T < 1800°C                                                                                                                                                 |
| Cost         | Very low                                                                                                                                                                  | High                                                                                                                                                               | Low                                                                                                                                                                             | Low                                                                                                                                                                 |
| Accuracy     | Good accuracy at one temperature<br>Less accurate over full range                                                                                                         | Excellent accuracy                                                                                                                                                 | Poor accuracy without calibration                                                                                                                                               | Good accuracy with polynomial correction                                                                                                                            |
| Linearity    | Very nonlinear.<br>Follows reciprocal of logarithmic function                                                                                                             | Fairly linear<br>Nonlinearity < 4.5% of full scale<br>Relatively simple quadratic function                                                                         | Fairly linear slope ≈ -2mV/°C<br>Slope varies according to current excitation, diode type, and diode processing                                                                 | Fairly linear<br>Nonlinearity < 10% of full scale<br>Complex 10th order polynomial                                                                                  |
| Construction | Less rugged                                                                                                                                                               | Depends on type (can be rugged)                                                                                                                                    | Rugged                                                                                                                                                                          | Most rugged                                                                                                                                                         |
| Output range | Typically 10s to 100s of kΩ full scale<br>Very wide variation in resistance                                                                                               | 18 to 390 Ω for PT100<br>180 to 3.9 kΩ for PT1000                                                                                                                  | 0.4 to 0.8V                                                                                                                                                                     | 10s of millivolts                                                                                                                                                   |
| Applications | General purpose                                                                                                                                                           | Scientific and industrial                                                                                                                                          | Low cost temperature monitor<br>Low cost linear response                                                                                                                        | Industrial temperature measurement                                                                                                                                  |
| General      | Requires excitation                                                                                                                                                       | Requires excitation                                                                                                                                                | Requires excitation                                                                                                                                                             | Self-powered<br>Requires cold junction comp                                                                                                                         |

Table 24: IC temperature sensor overview

|              | Diode                                                                                                                               | Analog IC temperature sensor                                                                           | Digital IC temperature sensor                                                       | Temperature switch/<br>thermostat                                                 |
|--------------|-------------------------------------------------------------------------------------------------------------------------------------|--------------------------------------------------------------------------------------------------------|-------------------------------------------------------------------------------------|-----------------------------------------------------------------------------------|
|              |                                                  |                      |    |  |
| Temp range   | -55°C < T < 150°C                                                                                                                   | -55°C < T < 150°C                                                                                      | -55°C < T < 150°C                                                                   | -55°C < T < 150°C                                                                 |
| Cost         | Very low                                                                                                                            | Low                                                                                                    | Low                                                                                 | Low                                                                               |
| Accuracy     | Poor accuracy without calibration                                                                                                   | Good device accuracy without calibration. Total T <sub>error</sub> ≤ 0.13°C.                           | Zero calibration required. Total T <sub>error</sub> including ADC ≤ 0.1°C.          | Zero calibration required. Total T <sub>error</sub> including comparator ≤ 0.1°C. |
| Linearity    | Fairly linear ≈ -2mV/°C. Slope varies according to current excitation, diode type, and diode processing from -5.5mV/C to +19.5mV/C. | Fairly linear. With analog sensors a variety of slope options in the range from -5.5mV/C to +19.5mV/C. | Direct readout of temperature value. 8 to 16 bits of resolution.                    | Programmable temperature threshold                                                |
| Construction | Rugged                                                                                                                              | Rugged                                                                                                 | Rugged                                                                              | Rugged                                                                            |
| Output range | 0.4V to 0.8V                                                                                                                        | 0 to 3V for analog. Different output ranges for different devices.                                     | Digital interfaces: I2C, SPI, UART                                                  | Active high or active low output                                                  |
| Applications | Low cost temperature monitor. Low cost linear response.                                                                             | General purpose, industrial and automotive                                                             | General purpose, industrial and automotive                                          | General purpose, industrial and automotive                                        |
| General      | Requires excitation                                                                                                                 | No external excitation required. Analog output normally directly connected to ADC.                     | Integrated temperature sensor and ADC/comparator. Options to measure remote diodes. | Resistor programmable, pin programmable, factory preset                           |

RTD equation temperature to resistance (T≥0°C and T<0°C)

R<sub>RTD</sub> = R<sub>0</sub> [ 1 + A<sub>0</sub>T + B<sub>0</sub>T<sup>2</sup> + C<sub>0</sub>(T - 100)T<sup>3</sup> ] (164) RTD resistance for T<0°C

R<sub>RTD</sub> = R<sub>0</sub> [ 1 + A<sub>0</sub>T + B<sub>0</sub>T<sup>2</sup> ] (165) RTD resistance for T≥0°C

Where

R<sub>RTD</sub> = resistance of RTD over temperature range of (-200°C < T < 850°C)

R<sub>0</sub> = 100Ω for PT-100, 1000Ω for PT-1000

A<sub>0</sub>, B<sub>0</sub>, C<sub>0</sub> = Callendar-Van Dusen coefficients

T = temperature in degrees Celsius (°C)

RTD equation resistance to temperature (T≥0°C or R<sub>RTD</sub> ≥ R<sub>0</sub>)

T = 
$$\frac{-A_0 + \sqrt{A_0^2 - 4B_0 \left(1 - \frac{R_{RTD}}{R_0}\right)}}{2B_0}$$
 (166) Temperature for T≥0°C or R<sub>RTD</sub> ≥ R<sub>0</sub>

Where

R<sub>RTD</sub> = resistance of RTD over temperature range of (T≥0°C)

R<sub>0</sub> = 100Ω for PT-100, 1000Ω for PT-1000

A<sub>0</sub>, B<sub>0</sub>, C<sub>0</sub> = Callendar-Van Dusen coefficients

T = temperature in degrees Celsius (°C)

Table 25: Callendar-Van Dusen coefficients for different RTD standards

|                | IEC-751 DIN 43760<br>BS 1904 ASTM-E1137<br>EN-60751 | JISC 1604  | US Industrial<br>Standard<br>D-100 American | US Industrial<br>Standard<br>American | ITS-90     |
|----------------|-----------------------------------------------------|------------|---------------------------------------------|---------------------------------------|------------|
| A <sub>0</sub> | +3.9083E-3                                          | +3.9739E-3 | +3.9787E-3                                  | +3.9692E-3                            | +3.9888E-3 |
| B <sub>0</sub> | -5.775E-7                                           | -5.870E-7  | -5.8686E-7                                  | -5.8495E-7                            | -5.915E-7  |
| C <sub>0</sub> | -4.183E-12                                          | -4.4E-12   | -4.167E-12                                  | -4.233E-12                            | -3.85E-12  |

Example

What is the temperature given an ITS-90 PT100 resistance of 120Ω?

Answer

T = 
$$\frac{-(3.9888 \cdot 10^{-3}) + \sqrt{(3.9888 \cdot 10^{-3})^2 - 4(-5.915 \cdot 10^{-7}) \left(1 - \frac{120}{100}\right)}}{2(-5.915 \cdot 10^{-7})} = 50.5^{\circ}\text{C}$$

**RTD equation resistance to temperature ( $T < 0^{\circ}\text{C}$  or  $R_{\text{RTD}} < R_0$ )**

$$T = \sum_{i=0}^n \alpha_i (R_{\text{RTD}})^i \quad (167) \text{ Temperature for } T < 0^{\circ}\text{C} \text{ or } R_{\text{RTD}} < R_0$$

**Where**

$T$  = temperature in degrees Celsius ( $^{\circ}\text{C}$ )

$R_{\text{RTD}}$  = resistance of RTD over temperature range of ( $T < 0^{\circ}\text{C}$ )

$\alpha_i$  = polynomial coefficients for converting RTD resistance to temperature for  $T < 0^{\circ}\text{C}$

**Table 26: Coefficients for 5th order RTD resistance to temperature**

|            | IEC-751<br>DIN 43760<br>BS 1904<br>ASTM-E1137<br>EN-60751 | JISC 1604     | US Industrial<br>Standard<br>D-100 American | US Industrial<br>Standard<br>American | ITS-90        |
|------------|-----------------------------------------------------------|---------------|---------------------------------------------|---------------------------------------|---------------|
| $\alpha_0$ | -2.420199E+02                                             | -2.381987E+02 | -2.381832E+02                               | -2.386381E+02                         | -2.379147E+02 |
| $\alpha_1$ | 2.222812E+00                                              | 2.189835E+00  | 2.195550E+00                                | 2.197285E+00                          | 2.201058E+00  |
| $\alpha_2$ | 2.585894E-03                                              | 2.522738E-03  | 2.441461E-03                                | 2.480324E-03                          | 2.322506E-03  |
| $\alpha_3$ | -4.825976E-06                                             | -4.781625E-06 | -4.751529E-06                               | -4.778784E-06                         | -4.628394E-06 |
| $\alpha_4$ | -2.818583E-08                                             | -2.704445E-08 | -2.385758E-08                               | -2.518695E-08                         | -1.971986E-08 |
| $\alpha_5$ | 1.524399E-10                                              | 1.473912E-10  | 1.350936E-10                                | 1.403820E-10                          | 1.184331E-10  |

**Example**

Find the temperature given an ITS-90 PT100 resistance of 60  $\Omega$ .

**Answer**

$R=60$

$$T = (-2.379147\text{E}+02) + (2.201058\text{E}+00) \cdot R + (2.322506\text{E}-03) \cdot R^2 + (-4.628394\text{E}-06) \cdot R^3 + (-1.971986\text{E}-08) \cdot R^4 + (1.184331\text{E}-10) \cdot R^5 = -98.653^{\circ}\text{C}$$

## Diode equation vs. temperature

$$V_D = \frac{nkT}{q} \ln\left(\frac{I}{I_S} + 1\right) \approx \frac{nkT}{q} \ln\left(\frac{I}{I_S}\right) \quad (168) \text{ Diode voltage}$$

### Where

$V_D$  = diode voltage vs. temperature and current

$n$  = diode ideality factor (ranges from 1 to 2)

$k = 1.38 \times 10^{-23}$  J/K, Boltzmann's constant

$T$  = temperature in Kelvin

$q = 1.60 \times 10^{-19}$  C, charge of an electron

$I$  = forward diode current in amps

$I_S$  = saturation current

$$I_S = \alpha T^{(3/n)} \exp\left(-\frac{qV_G}{nkT}\right) \quad (169) \text{ Saturation current}$$

### Where

$I_S$  = saturation current

$\alpha$  = constant related to the cross sectional area of the junction

$V_G$  = diode voltage vs. temperature and current

$n$  = diode ideality factor (ranges from 1 to 2)

$k = 1.38 \times 10^{-23}$  J/K, Boltzmann's constant

$T$  = temperature in Kelvin

$q = 1.60 \times 10^{-19}$  C, charge of an electron

Diode voltage versus temperature

Figure 67 shows an example of the temperature drift for a diode. Depending on the characteristics of the diode and the forward current the slope and offset of this curve will change. However, typical diode drift is about  $-2\text{mV}/^\circ\text{C}$ . A forward drop of about  $0.6\text{V}$  is typical for room temperature.

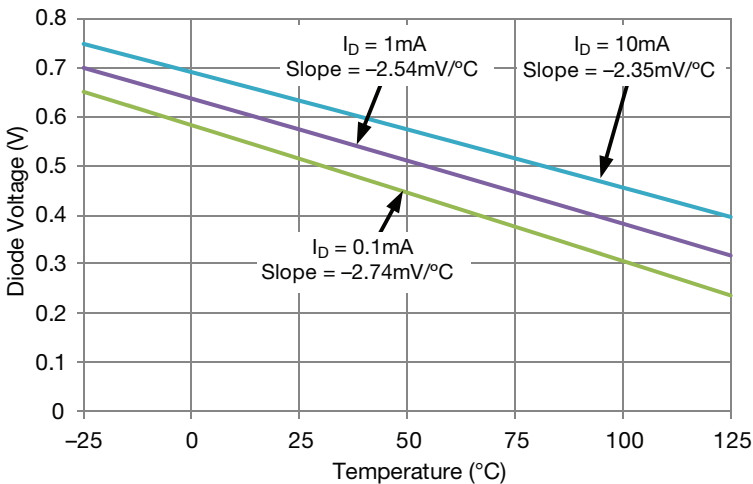


Figure 67: Diode voltage drop vs. temperature

Type J thermocouples translating temperature to voltage  
(ITS-90 standard)

$$V_T = \sum_{i=0}^n c_i(T)^i$$

(170) Thermoelectric voltage

Where

- $V_T$  = thermoelectric voltage
- $T$  = temperature in degrees Celsius
- $c_i$  = translation coefficients

Table 27: Type J thermocouple temperature to voltage coefficients

| Type J thermocouple temperature to voltage |                   |                   |
|--------------------------------------------|-------------------|-------------------|
| Temperature                                | −219°C to 760°C   | 760°C to 1,200°C  |
| $c_0$                                      | 0.0000000000E+00  | 2.9645625681E+05  |
| $c_1$                                      | 5.0381187815E+01  | −1.4976127786E+03 |
| $c_2$                                      | 3.0475836930E-02  | 3.1787103924E+00  |
| $c_3$                                      | −8.5681065720E-05 | −3.1847686701E-03 |
| $c_4$                                      | 1.3228195295E-07  | 1.5720819004E-06  |
| $c_5$                                      | −1.7052958337E-10 | −3.0691369056E-10 |
| $c_6$                                      | 2.0948090697E-13  | —                 |
| $c_7$                                      | −1.2538395336E-16 | —                 |
| $c_8$                                      | 1.5631725697E-20  | —                 |

Type J thermocouples translating voltage to temperature  
(ITS-90 standard)

$$T = \sum_{i=0}^n c_i (V_t)^i$$

(171) Temperature

Table 28: Type J thermocouple voltage to temperature coefficients

| Type J thermocouple voltage to temperature |                  |                  |                      |
|--------------------------------------------|------------------|------------------|----------------------|
| Temperature                                | −219°C to 0°C    | 0°C to 760°C     | 760°C to 1,200°C     |
| Voltage                                    | −8.095mV to 0V   | 0V to 42.919mV   | 42.919mV to 69.553mV |
| c <sub>0</sub>                             | 0.000000000E+00  | 0.000000000E+00  | −3.113581870E+03     |
| c <sub>1</sub>                             | 1.952826800E-02  | 1.978425000E-02  | 3.005436840E-01      |
| c <sub>2</sub>                             | −1.228618500E-06 | −2.001204000E-07 | −9.947732300E-06     |
| c <sub>3</sub>                             | −1.075217800E-09 | 1.036969000E-11  | 1.702766300E-10      |
| c <sub>4</sub>                             | −5.908693300E-13 | −2.549687000E-16 | −1.430334680E-15     |
| c <sub>5</sub>                             | −1.725671300E-16 | 3.585153000E-21  | 4.738860840E-21      |
| c <sub>6</sub>                             | −2.813151300E-20 | −5.344285000E-26 | —                    |
| c <sub>7</sub>                             | −2.396337000E-24 | 5.099890000E-31  | —                    |
| c <sub>8</sub>                             | −8.382332100E-29 | —                | —                    |

Type K thermocouples translating temperature to voltage  
(ITS-90 standard)

$$V_T = \sum_{i=0}^n c_i(T)^i$$

(172) Thermoelectric voltage for T<0°C

$$V_T = \left[ \sum_{i=0}^n c_i(T)^i \right] + \alpha_0 e^{[\alpha_1(T-126.9686)]^2}$$

(173) Thermoelectric voltage for T>0°C

Where

- V<sub>T</sub> = thermoelectric voltage
- T = temperature in degrees Celsius
- c<sub>i</sub> = translation coefficients
- α<sub>0</sub>, α<sub>1</sub> = translation coefficients

Table 29: Type K thermocouple temperature to voltage coefficients

| Temperature     | −270°C to 0°C     | 0°C to 1,372°C    |
|-----------------|-------------------|-------------------|
| C <sub>0</sub>  | 0.000000000E+00   | −1.7600413686E+01 |
| C <sub>1</sub>  | 3.9450128025E+01  | 3.8921204975E+01  |
| C <sub>2</sub>  | 2.3622373598E-02  | 1.8558770032E-02  |
| C <sub>3</sub>  | −3.2858906784E-04 | −9.9457592874E-05 |
| C <sub>4</sub>  | −4.9904828777E-06 | 3.1840945719E-07  |
| C <sub>5</sub>  | −6.7509059173E-08 | −5.6072844889E-10 |
| C <sub>6</sub>  | −5.7410327428E-10 | 5.6075059059E-13  |
| C <sub>7</sub>  | −3.1088872894E-12 | −3.2020720003E-16 |
| C <sub>8</sub>  | −1.0451609365E-14 | 9.7151147152E-20  |
| C <sub>9</sub>  | −1.9889266878E-17 | −1.2104721275E-23 |
| C <sub>10</sub> | −1.6322697486E-20 | —                 |
| α <sub>0</sub>  | —                 | 1.1859760000E+02  |
| α <sub>1</sub>  | —                 | −1.1834320000E-04 |

Type K thermocouples translating voltage to temperature  
(ITS-90 standard)

$$T = \sum_{i=0}^n c_i (V_t)^i$$

(174) Temperature

Table 30: Type K thermocouple voltage to temperature coefficients

| Temperature    | -200°C to 0°C  | 0°C to 500°C   | 500°C to 1,372°C     |
|----------------|----------------|----------------|----------------------|
| Voltage        | -5.891mV to 0V | 0V to 20.644mV | 20.644mV to 54.886mV |
| C <sub>0</sub> | 0.0000000E+00  | 0.0000000E+00  | -1.3180580E+02       |
| C <sub>1</sub> | 2.5173462E-02  | 2.5083550E-02  | 4.8302220E-02        |
| C <sub>2</sub> | -1.1662878E-06 | 7.8601060E-08  | -1.6460310E-06       |
| C <sub>3</sub> | -1.0833638E-09 | -2.5031310E-10 | 5.4647310E-11        |
| C <sub>4</sub> | -8.9773540E-13 | 8.3152700E-14  | -9.6507150E-16       |
| C <sub>5</sub> | -3.7342377E-16 | -1.2280340E-17 | 8.8021930E-21        |
| C <sub>6</sub> | -8.6632643E-20 | 9.8040360E-22  | -3.1108100E-26       |
| C <sub>7</sub> | -1.0450598E-23 | -4.4130300E-26 | —                    |
| C <sub>8</sub> | -5.1920577E-28 | 1.0577340E-30  | —                    |
| C <sub>9</sub> | —              | -1.0527550E-35 | —                    |

Table 31: Seebeck coefficients for different material

| Material   | Seebeck coefficient | Material  | Seebeck coefficient | Material  | Seebeck coefficient |
|------------|---------------------|-----------|---------------------|-----------|---------------------|
| Aluminum   | 4                   | Gold      | 6.5                 | Rhodium   | 6                   |
| Antimony   | 47                  | Iron      | 19                  | Selenium  | 900                 |
| Bismuth    | -72                 | Lead      | 4                   | Silicon   | 440                 |
| Cadmium    | 7.5                 | Mercury   | 0.6                 | Silver    | 6.5                 |
| Carbon     | 3                   | Nichrome  | 25                  | Sodium    | -2.0                |
| Constantan | -35                 | Nickel    | -15                 | Tantalum  | 4.5                 |
| Copper     | 6.5                 | Platinum  | 0                   | Tellurium | 500                 |
| Germanium  | 300                 | Potassium | -9.0                | Tungsten  | 7.5                 |

Note: Units are  $\mu\text{V}/^\circ\text{C}$ . All data at temperature of 0°C.

**Thermistor: Resistance to temperature, Steinhart-Hart equation**

$$\frac{1}{T} = a + b \ln(R) + c [\ln(R)]^3 \quad (175) \text{ Convert resistance to temperature for a thermistor}$$

**Where**

T = temperature in Kelvin

a, b, c = Steinhart-Hart equation constants

R = resistance in ohms

**Thermistor: Temperature to resistance, Steinhart-Hart equation**

$$R = \exp \left[ \left( y - \frac{x}{2} \right)^{\frac{1}{3}} - \left( y + \frac{x}{2} \right)^{\frac{1}{3}} \right] \quad (176) \text{ Convert temperature to resistance for a thermistor}$$

$$x = \frac{a - \frac{1}{T}}{c} \quad (177) \text{ Factor used in Equation 165}$$

$$y = \sqrt{\left( \frac{b}{3c} \right)^3 + \frac{x^2}{4}} \quad (178) \text{ Factor used in Equation 165}$$

**Where**

R = resistance in  $\Omega$

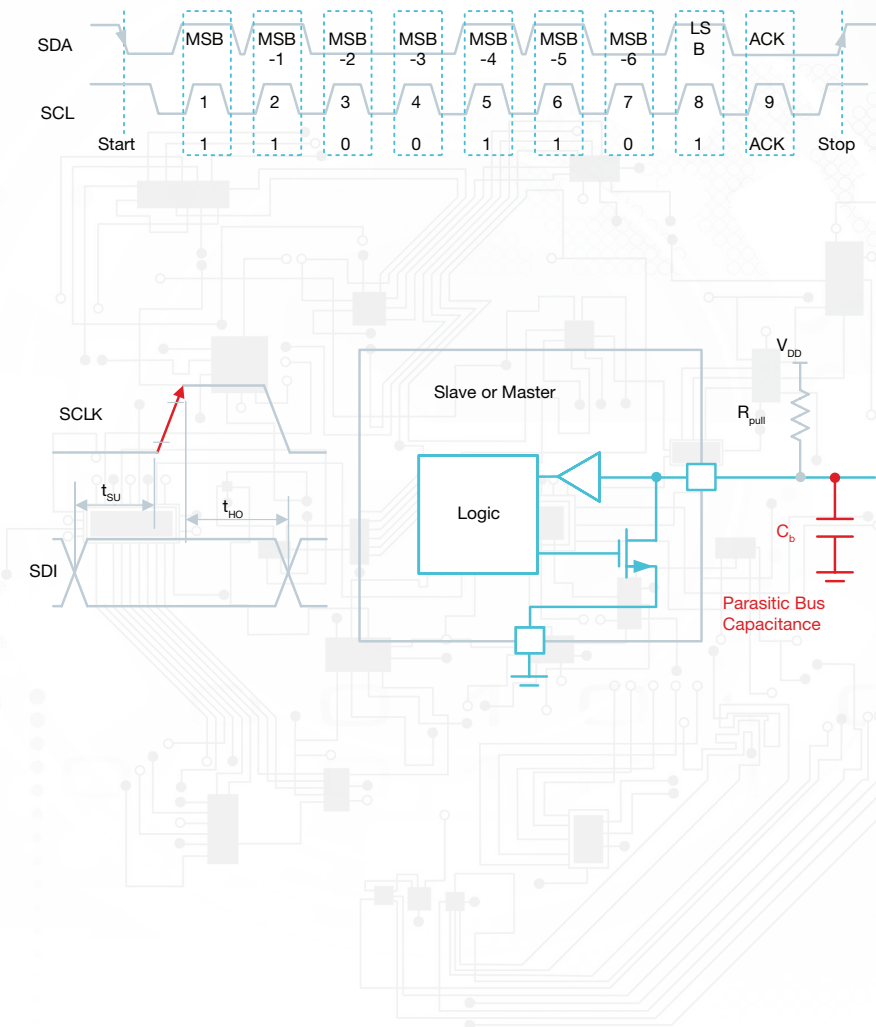
T = temperature in Kelvin

a, b, c = Steinhart-Hart equation constants

x, y = Steinhart-Hart factors used in temperature to resistance equation

# Digital

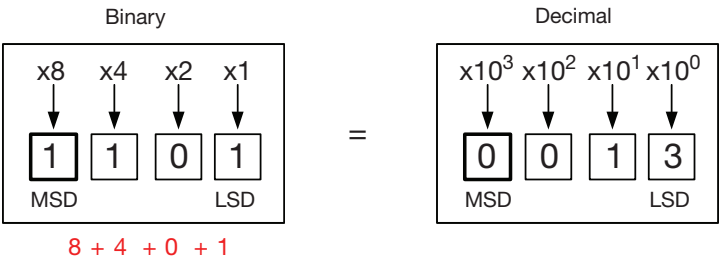
- Binary/hex conversions
- Digital logic thresholds
- Serial peripheral interface
- Inter-integrated circuit (I<sup>2</sup>C) bus



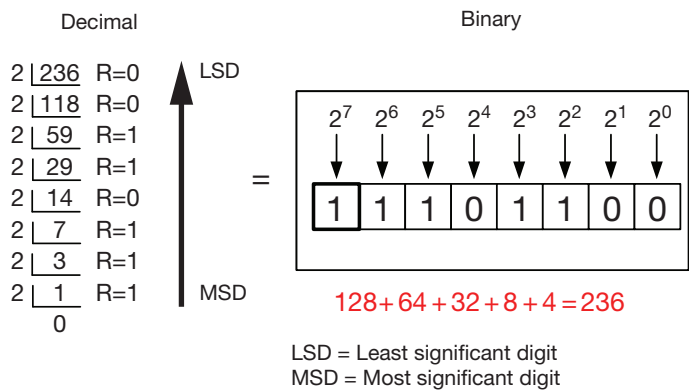
Numbering systems: Binary, decimal, and hexadecimal

|                       |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |
|-----------------------|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|
| Binary (Base-2)       | 0 |   |   |   |   | 1 |   |   |   |   |   |   |   |   |   |   |
| Decimal (Base-10)     | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |   |   |   |   |   |   |
| Hexadecimal (Base-16) | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | A | B | C | D | E | F |

Example conversion: Binary to decimal

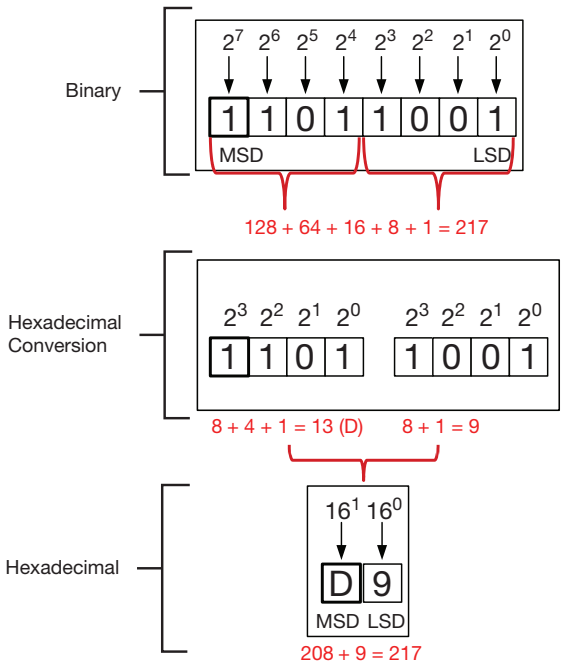


Example conversion: Decimal to binary



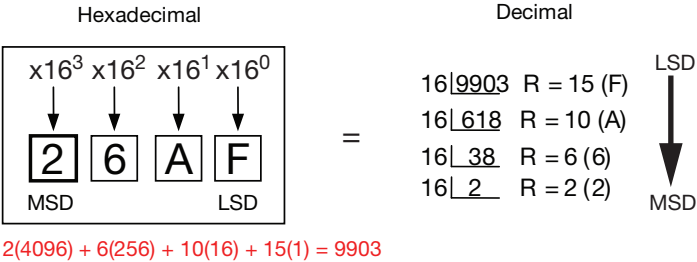
Numbering systems: Binary, decimal, and hexadecimal (cont.)

Example conversion: Binary to hexadecimal



Example conversion: Hexadecimal to decimal and decimal to hexadecimal

|                       |   |   |   |   |   |   |   |   |   |   |    |    |    |    |    |    |
|-----------------------|---|---|---|---|---|---|---|---|---|---|----|----|----|----|----|----|
| Decimal (Base-10)     | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 |
| Hexadecimal (Base-16) | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | A  | B  | C  | D  | E  | F  |



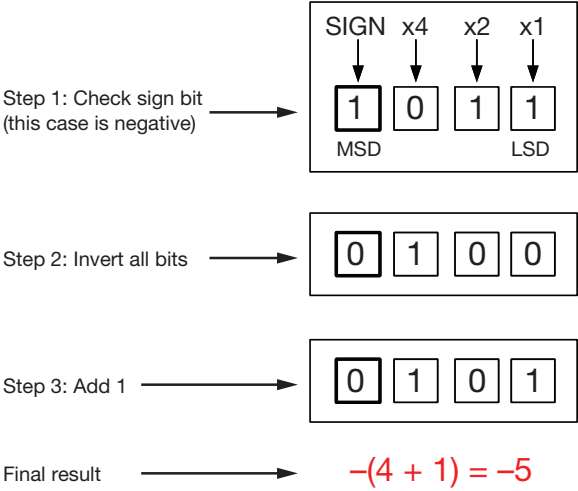
LSD = Least significant digit  
MSD = Most significant digit

Data formats

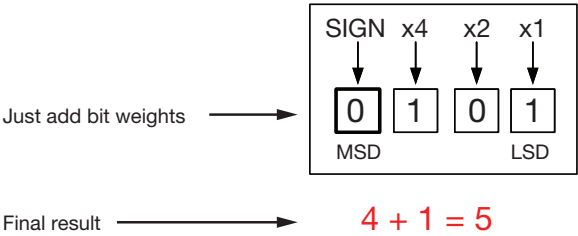
Table 32: Different data formats

| Code     | Straight binary | Offset binary | 2's complement |
|----------|-----------------|---------------|----------------|
| Binary   | Decimal value   | Decimal value | Decimal value  |
| 11111111 | 255             | 127           | -1             |
| 11000000 | 192             | 64            | -64            |
| 10000000 | 128             | 0             | -128           |
| 01111111 | 127             | -1            | 127            |
| 01000000 | 64              | -64           | 64             |
| 00000000 | 0               | -128          | 0              |

Converting two's complement to decimal:  
Negative number example



Converting two's complement to decimal:  
Positive number example



## Digital logic thresholds

**Input logic thresholds** = the voltage range a logic device will sense a logic high or low as specified in the data sheet. Applying an input voltage outside of this range to the device will have unpredictable results.

**Output logic thresholds** = the output voltage range of a logic device driving a logic high or low as specified in the data sheet. The output level range is normally specified with current loads (sourcing for logic high and sinking for logic low).

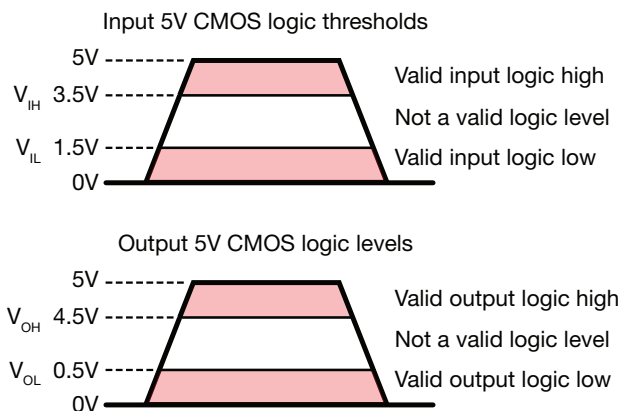


Figure 68: Valid input logic levels for 5V CMOS

Table 33: CMOS logic thresholds

|                 | 5V CMOS |           | 3.3V CMOS |           | 2.5V CMOS | 1.8V CMOS |
|-----------------|---------|-----------|-----------|-----------|-----------|-----------|
| V <sub>CC</sub> | 5.0     |           | 3.3       |           | 2.5       | 1.8       |
| V <sub>OH</sub> | 4.5     | 0.9 · VCC | 2.97      | 0.9 · VCC | 2.0       | 1.35      |
| V <sub>IH</sub> | 3.5     | 0.7 · VCC | 2.31      | 0.7 · VCC | 1.7       | 1.17      |
| V <sub>IL</sub> | 1.5     | 0.3 · VCC | 0.99      | 0.3 · VCC | 0.7       | 0.63      |
| V <sub>OL</sub> | 0.5     | 0.1 · VCC | 0.33      | 0.1 · VCC | 0.4       | 0.45      |
| GND             | 0.0     |           | 0.0       |           | 0.0       | 0.0       |

Table 34: TTL logic thresholds

|                 | 5V TTL | 3.3V LVTTTL |
|-----------------|--------|-------------|
| V <sub>CC</sub> | 5.0    | 3.3         |
| V <sub>OH</sub> | 2.4    | 2.4         |
| V <sub>IH</sub> | 2.0    | 1.5         |
| V <sub>IL</sub> | 0.8    | 0.8         |
| V <sub>OL</sub> | 0.4    | 0.4         |
| GND             | 0.0    | 0.0         |

Where

V<sub>CC</sub> and GND = supply voltage and ground for the device

V<sub>OH</sub> = minimum output logic high level

V<sub>IH</sub> = minimum input high logic level

V<sub>IL</sub> = maximum input logic low level

V<sub>OL</sub> = maximum output logic low level

## SPI bus (Serial Peripheral Interface) hardware overview

- In SPI interfaces the master can connect to one or more slave devices
- In cases when multiple slave devices are used, the master will use multiple chip select ( $\overline{CS}$ ) lines

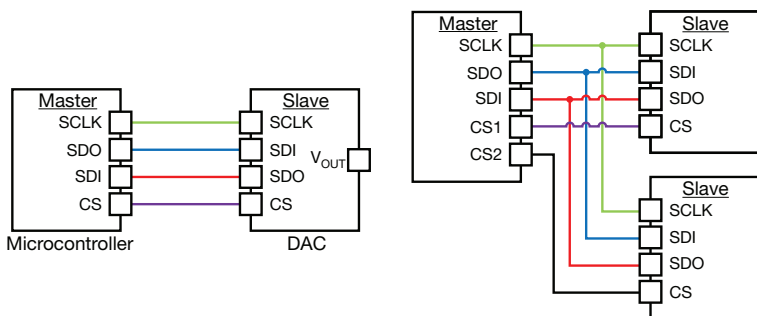


Figure 69: SPI master and slave configurations

### Data and control lines

$\overline{CS}$  (chip select) = sometimes referred to as slave select.  $\overline{CS}$  is driven by the master and arbitrates over the SPI bus. When driven low, the SPI bus is active.

SDO/SDI (serial data in and serial data out) = these names describe data flow for the device. The system names describe the data flow relationship between the master and slave. System names: MOSI = Master Out Slave In and MISO = Master In Slave Out. Example: SDO on a slave is MISO in the system and SDI is MOSI in the system.

SCLK (serial clock) = this is a square wave driven by the SPI master. Data on SDO and SDI have relative timing to the SCLK signal which controls the latching of the data on the SPI bus.

## SPI data latching

- SPI data is latched on the rising or falling edge of SCLK
- The edge data is latched on is called the critical edge
- The figure below illustrates latching logic 1 on rising edge and logic 0 on falling edge



Figure 70: SPI SCLK critical edge

## SPI read sequence example

1. Critical edge is rising edge
2. Master output writing to slave (SDI label relative to slave device)
3. The active low  $\overline{CS}$  pin is driven low to 0V, activating the slave SPI bus
4. Data is clocked in from MSB to LSB on the rising edge of SCLK
5. Completed SPI transaction data is binary 1011001

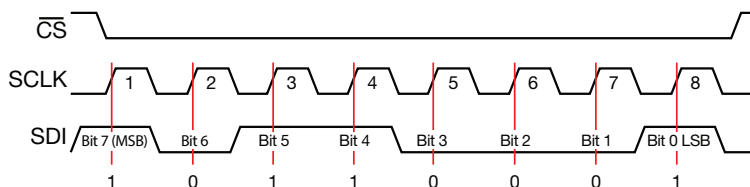


Figure 71: Example SPI write sequence

## SPI critical edge

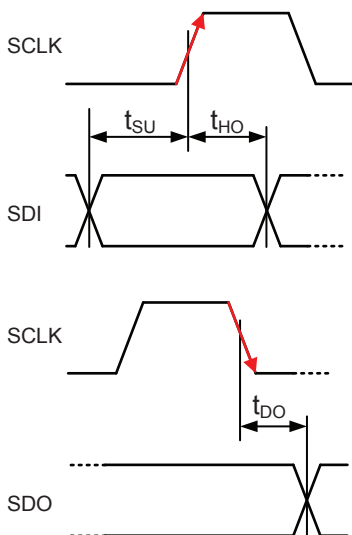
$t_{SU}$  (setup time) = defines how long before the critical edge that the data on SDI must already be set and settled

$t_{HO}$  (hold time) = defines how long after the critical edge data must be maintained on SDI.

$t_{DO}$  (delay time) - defines the delay before data is valid after the critical edge for SDO.

Violation of any timing requirement could result in corruption of data.

The timing parameters,  $t_{SU}$ ,  $t_{HO}$  and  $t_{DO}$ , are defined relative to the critical edge. In the example below for SDI the rising edge of SCLK is the critical edge and for SDO the falling edge of SCLK is the critical edge.



**Figure 72: Setup and hold timing illustration**

SPI modes

CPHA (clock phase) = defines which edge data is latched on, a 0 representing the first edge and a 1 representing the second edge

CPOL (clock polarity) = defines whether the clock idles high or low in between SPI frames. CPOL = 0 idles low, CPOL = 1 idles high.

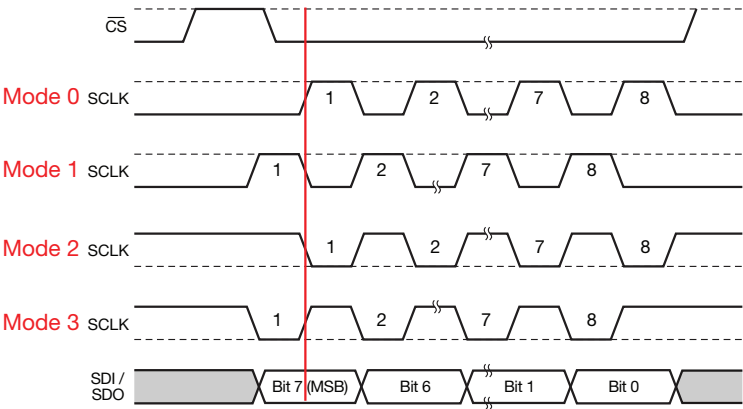


Figure 73: SPI modes of operation

| Mode | CPOL | CPHA | Critical edge | Clock phase |
|------|------|------|---------------|-------------|
| 0    | 0    | 0    | Rising edge   | Idles low   |
| 1    | 0    | 1    | Falling edge  | Idles low   |
| 2    | 1    | 0    | Rising edge   | Idles high  |
| 3    | 1    | 1    | Falling edge  | Idles high  |

## I<sup>2</sup>C bus (Inter-Integrated Circuit) hardware overview

- On I<sup>2</sup>C buses the master can connect to one or more slave devices
- The slave is selected by its I<sup>2</sup>C address. This allows one controller to connect to many slaves on the two-wire bus.

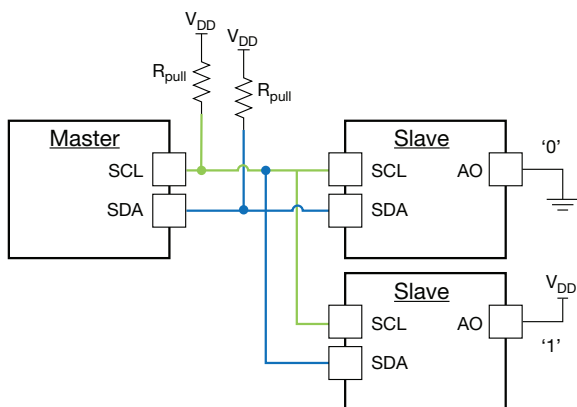


Figure 74: : I<sup>2</sup>C master and slave hardware connections

### Data and control lines

SCL (serial clock) = this is a square wave driven by the master that controls how fast data is sent and when data is latched to the slave device(s)

SDA (serial data) = both master and slave place data on this line in sync with the clock pulses in a half-duplex fashion. Data on this line includes address, control, and communication data.

I<sup>2</sup>C addressing

- Typical addressing in I<sup>2</sup>C is 7-bit addressing with an additional bit for read or write indication
- Each device on the I<sup>2</sup>C bus must have a unique address
- Duplicate addresses will result in communication errors
- Some devices may have pin programmable I<sup>2</sup>C addresses

Address byte

| MSB |   |   |   |   |   | LSB | R/ $\overline{W}$ |
|-----|---|---|---|---|---|-----|-------------------|
| 1   | 0 | 0 | 1 | 1 | 0 | A0  | 1/0               |

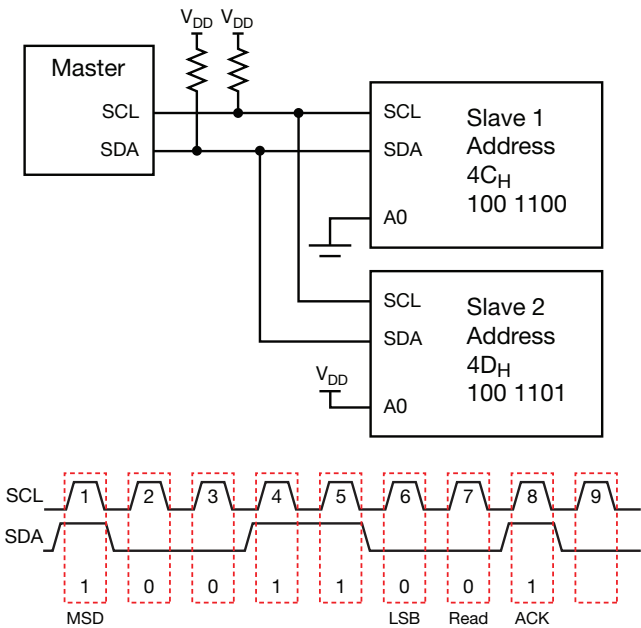


Figure 75: : I<sup>2</sup>C addressing

## I<sup>2</sup>C communication

START = initiated by the master pulling SDA low while SCL is high

STOP = initiated by the master releasing the SDA pin high while SCL is high

ACK (acknowledge) = each transfer in I<sup>2</sup>C is a single byte or 8-bits, with one SCL pulse per bit. The 9th pulse in each exchange is reserved for an acknowledgement signal from the slave, or an ACK signal. The ACK signal indicates that the previous transfer was successful.

Example I<sup>2</sup>C write sequence:

1. The master pulls down SDA to generate a START condition
2. The first bit is set up and the master pulls down and releases SCL to clock data into the DAC
3. On the 9<sup>th</sup> bit the master does not pull down SDA. If the slave pulls down SDA the 8-bit transaction is acknowledged.
4. The completed transaction in binary is 11001101

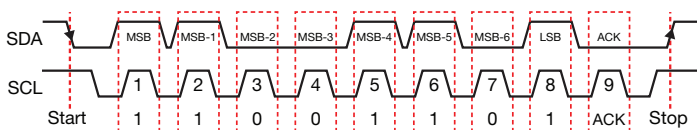
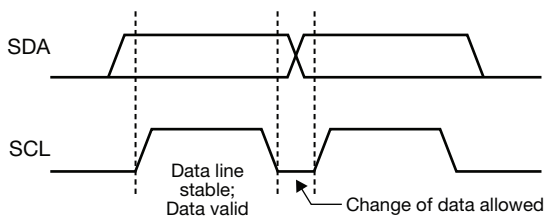


Figure 76: Complete I<sup>2</sup>C transaction

## I<sup>2</sup>C communication (cont.)

For valid data transfer:

- SDA must remain stable the entire time that SCL is high for a bit transfer to be valid
- SDA is only allowed to transition in between SCL pulses when SCL is low
- Instances where SDA changes while SCL is high are interpreted as START, RESTART, or STOP conditions



**Figure 77: I<sup>2</sup>C data transfer**

## I<sup>2</sup>C interface circuitry and rise/fall timing

The figure below illustrates the internal structure for an I<sup>2</sup>C SCL or SDA pin. The transistor will turn on for logic low discharging  $C_b$  to logic low. The transistor will turn off for a logic high and the pull-up,  $R_{pull}$ , will charge  $C_b$  to a logic high.

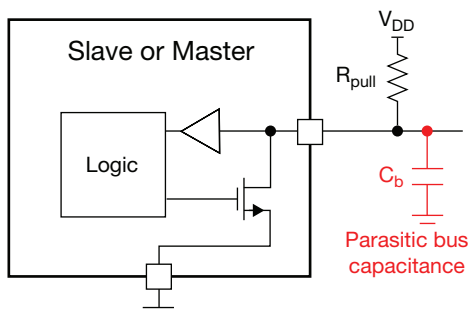


Figure 78: I<sup>2</sup>C data transfer

$t_r$  (rise time) = the maximum amount of time for the signal to transition from logic low to logic high. Since I<sup>2</sup>C data is an open drain signal, rise time is set by the RC time constant of the pull-up resistance and the bus capacitance.

$t_f$  (fall time) = the maximum amount of time for the signal to transition from logic high to logic low

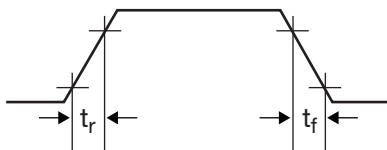


Figure 79: I<sup>2</sup>C rise and fall timing

## I<sup>2</sup>C pull-up resistor selection

$$R_{\text{Pull(Min)}} = \frac{(V_{\text{DD}} - V_{\text{OLMAX}})}{I_{\text{SinkMax}}} \quad (179) \text{ Minimum I}^2\text{C pull-up resistance}$$

$$R_{\text{Pull(Max)}} = \frac{t_r}{(0.8473 \times C_b)} \quad (180) \text{ Maximum I}^2\text{C pull-up resistance}$$

### Where

$R_{\text{Pull(Min)}}$  = this is the minimum pull-up resistance. This will give the shortest rise time. Using a pull-up smaller than this will draw too much current when the output transistor is on (logic low) and violate the maximum logic low output specification.

$R_{\text{Pull(Max)}}$  = maximum pull-up resistance. This will give the longest rise time. Using a pull-up resistance larger than this will violate timing requirements.

$V_{\text{DD}}$  = supply voltage

$V_{\text{OLMAX}}$  = maximum logic low output found in device data sheet. Typically 0.4V.

$I_{\text{SinkMax}}$  = maximum sink current when the output transistor is on (logic low) found in device data sheet. Typically 3mA.

$C_b$  = bus capacitance. Depends on width and length of PCB trace (see equation 155), and the capacitance of the devices connected to the bus.

### Example

Find a pull-up resistor for:  $V_{\text{DD}} = 5\text{V}$ ,  $V_{\text{OLMAX}} = 0.4\text{V}$ ,  $t_r = 300\text{ns}$ , and  $C_b = 100\text{pF}$ .

### Answer

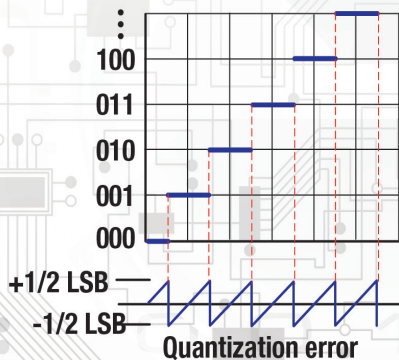
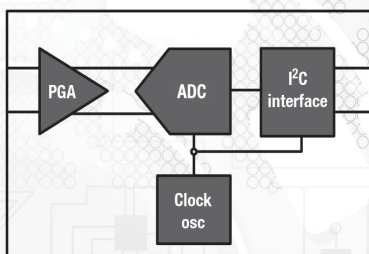
$$R_{\text{Pull(Min)}} = \frac{(V_{\text{DD}} - V_{\text{OLMAX}})}{I_{\text{SinkMax}}} = \frac{(5\text{V} - 0.4\text{V})}{0.003\text{A}} = 1.53\text{k}\Omega$$

$$R_{\text{Pull(Max)}} = \frac{t_r}{(0.8473 \times C_b)} = \frac{300\text{ns}}{0.8473 \times 100\text{pF}} = 3.54\text{k}\Omega$$

$$R_{\text{Pull}} = 2\text{k}\Omega \quad \text{Selected as a standard value between } R_{\text{Pull(Min)}} \text{ and } R_{\text{Pull(Max)}}$$

# ADC

- ADC transfer function •
- Quantization error •
- Signal-to-noise ratio (SNR) •
- Signal-to-noise and distortion (SINAD) •
- Total harmonic distortion (THD) •
- Effective number of bits (ENOB) •
- Noise-free resolution and effective resolution •



ADC definitions

|                                                                                  |                                                    |
|----------------------------------------------------------------------------------|----------------------------------------------------|
| Resolution = n                                                                   | The number of bits used to quantify the input      |
| Number of codes = 2 <sup>n</sup>                                                 | The number of output code combinations             |
| Full-scale range input = FSR                                                     | Sets the converter input range and the LSB voltage |
| LSB = FSR / 2 <sup>n</sup>                                                       | The voltage step size of each LSB                  |
| Full-scale input voltage = (2 <sup>n</sup> – 1) • 1LSB                           | Full-scale input voltage of the ADC                |
| Full-scale output code = 2 <sup>n</sup> – 1                                      | Largest code that can be read                      |
| Transfer function: Output Code = round [V <sub>IN</sub> / (FSR/2 <sup>n</sup> )] | Relationship between input voltage and output code |

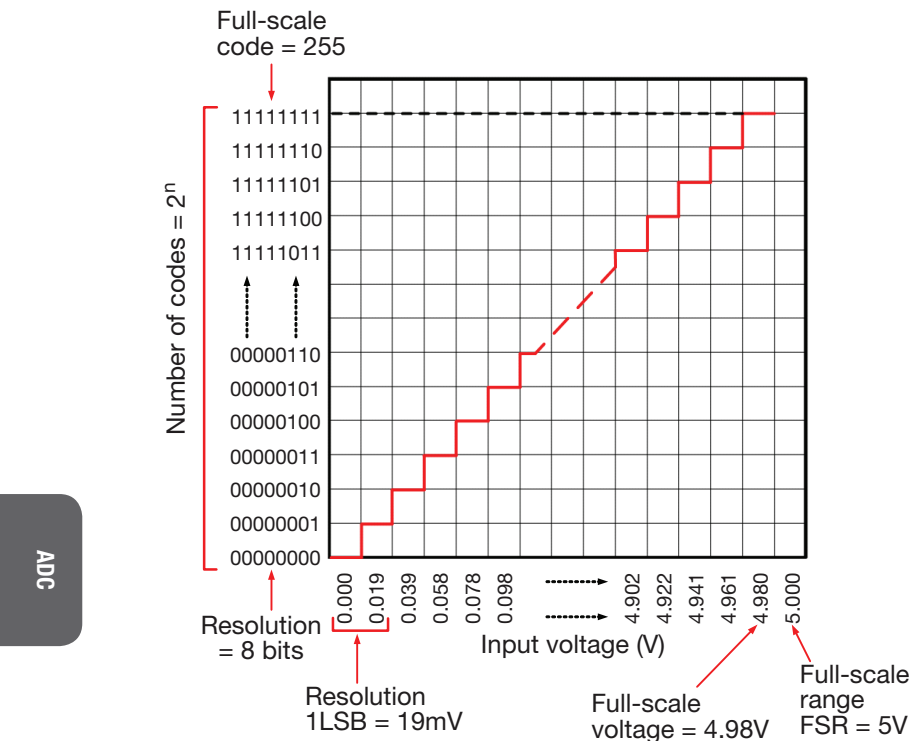


Figure 80: ADC transfer function

## ADC resolution for unipolar

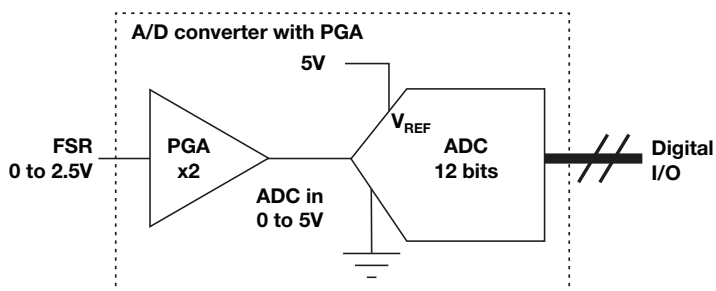


Figure 81: ADC full-scale range (FSR) unipolar

### Full-scale range (FSR) unipolar

$$\text{FSR} = \frac{V_{\text{REF}}}{\text{PGA}} \quad (181) \text{ Full-scale range}$$

$$1\text{LSB} = \frac{\text{FSR}}{2^n} \quad (182) \text{ One least significant bit}$$

#### Where

FSR = full-scale range

PGA = PGA gain

1LSB = one least significant bit or resolution of the data converter

n = resolution number of bits

$V_{\text{REF}}$  = reference voltage

### Example calculation for the circuit above

$$\text{FSR} = \frac{V_{\text{REF}}}{\text{PGA}} = \frac{5\text{V}}{2} = 2.5\text{V}$$

$$1\text{LSB} = \frac{\text{FSR}}{2^n} = \frac{2.5\text{V}}{2^{12}} = 610.35\mu\text{V}$$

## ADC resolution for bipolar

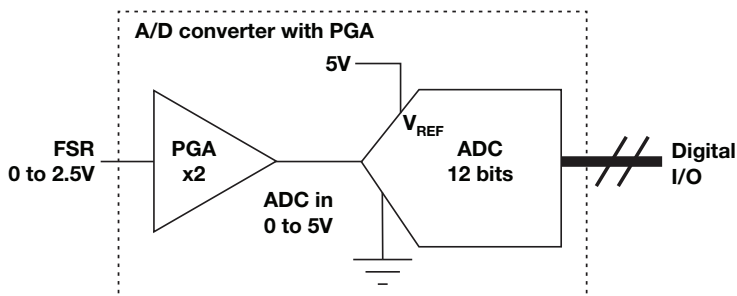


Figure 82: ADC full-scale range (FSR) bipolar

### Full-scale range (FSR) bipolar

$$\text{FSR} = \frac{V_{\text{REF}}}{\text{PGA}} \quad (183) \text{ Full-scale range}$$

$$1\text{LSB} = \frac{\text{FSR}}{2^n} \quad (184) \text{ One least significant bit}$$

#### Where

FSR = full-scale range

PGA = PGA gain

1LSB = one least significant bit or resolution of the data converter

n = resolution number of bits

V<sub>REF</sub> = reference voltage

### Example calculation for the circuit above

$$\text{FSR} = \frac{\pm V_{\text{REF}}}{\text{PGA}} = \frac{\pm 2.5\text{V}}{2} = \pm 1.25\text{V} \Rightarrow 2.5\text{V}$$

$$1\text{LSB} = \frac{\text{FSR}}{2^n} = \frac{2.5\text{V}}{2^{12}} = 610.35\mu\text{V}$$

## Resolution voltage vs. full-scale range

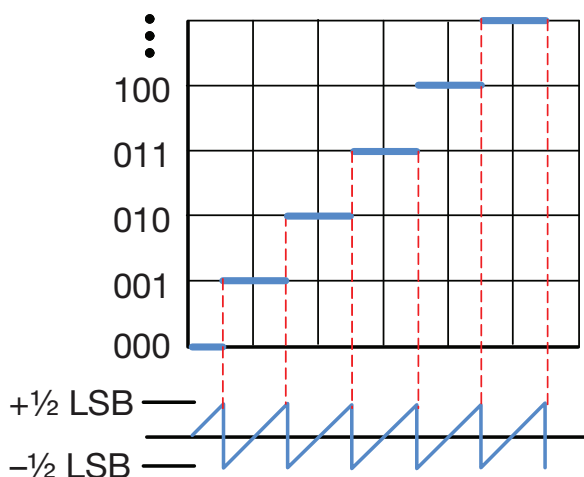
Table 35: LSB voltage vs. resolution and reference voltage

|            |    | FSR (Full-Scale Range) |              |              |               |
|------------|----|------------------------|--------------|--------------|---------------|
|            |    | 1.024V                 | 1.25V        | 2.048V       | 2.5V          |
| Resolution | 8  | 4 mV                   | 4.88 mV      | 8 mV         | 9.76 mV       |
|            | 10 | 1 mV                   | 1.22 mV      | 2 mV         | 2.44 mV       |
|            | 12 | 250 $\mu$ V            | 305 $\mu$ V  | 500 $\mu$ V  | 610 $\mu$ V   |
|            | 14 | 52.5 $\mu$ V           | 76.3 $\mu$ V | 125 $\mu$ V  | 152.5 $\mu$ V |
|            | 16 | 15.6 $\mu$ V           | 19.1 $\mu$ V | 31.2 $\mu$ V | 38.14 $\mu$ V |
|            | 18 | 3.91 $\mu$ V           | 4.77 $\mu$ V | 7.81 $\mu$ V | 9.53 $\mu$ V  |
|            | 20 | 0.98 $\mu$ V           | 1.19 $\mu$ V | 1.95 $\mu$ V | 2.384 $\mu$ V |
|            | 22 | 244 nV                 | 299 nV       | 488 nV       | 596 nV        |
|            | 24 | 61 nV                  | 74.5 nV      | 122 nV       | 149 nV        |

Table 36: LSB voltage vs. resolution and reference voltage

|            |    | FSR (Full-Scale Range) |               |              |               |
|------------|----|------------------------|---------------|--------------|---------------|
|            |    | 3V                     | 3.3V          | 4.096V       | 5V            |
| Resolution | 8  | 11.7 mV                | 12.9 mV       | 16 mV        | 19.5 mV       |
|            | 10 | 2.93 mV                | 3.222 mV      | 4 mV         | 4.882 mV      |
|            | 12 | 732 $\mu$ V            | 806 $\mu$ V   | 1 mV         | 1.221 mV      |
|            | 14 | 183 $\mu$ V            | 201 $\mu$ V   | 250 $\mu$ V  | 305 $\mu$ V   |
|            | 16 | 45.77 $\mu$ V          | 50.35 $\mu$ V | 62.5 $\mu$ V | 76.29 $\mu$ V |
|            | 18 | 11.44 $\mu$ V          | 12.58 $\mu$ V | 15.6 $\mu$ V | 19.07 $\mu$ V |
|            | 20 | 2.861 $\mu$ V          | 3.147 $\mu$ V | 3.91 $\mu$ V | 4.768 $\mu$ V |
|            | 22 | 715 nV                 | 787 nV        | 976 nV       | 1.192 $\mu$ V |
|            | 24 | 179 nV                 | 196 nV        | 244 nV       | 298 nV        |

## Quantization error of ADC



**Figure 83: Quantization error of an ADC converter**

### Quantization error

The error introduced as a result of the quantization process. The amount of this error is a function of the resolution of the converter. The quantization error of an ADC converter is  $1/2 \text{ LSB}$ . The quantization error signal is the difference between the actual voltage applied and the ADC output (Figure 83). The RMS of the quantization signal is  $1\text{LSB}/\sqrt{12}$ .

**Signal-to-noise ratio (SNR) from quantization noise only**

$$\text{MaxRMSSignal} = \frac{\text{FSR} / 2}{\sqrt{2}} = \frac{1 \text{ LSB} \times 2^{N-1}}{\sqrt{2}} \quad (185)$$

$$\text{RMSNoise} = \frac{1 \text{ LSB}}{\sqrt{12}} \quad \text{from quantization only} \quad (186)$$

$$\text{SNR} = \frac{\text{MaxRMSSignal}}{\text{RMSNoise}} = \frac{1 \text{ LSB} \times 2^{N-1} / \sqrt{2}}{1 \text{ LSB} / \sqrt{12}} = 2^{N-1} \sqrt{6} \quad (187)$$

$$\text{SNR(dB)} = 20 \log(\text{SNR}) = [20 \log(2)]N + 20 \log\left(\frac{\sqrt{6}}{2}\right) \quad (188)$$

$$\text{SNR(dB)} \approx 6.02N + 1.76 \quad (189)$$

**Where**

FSR = full-scale range of the ADC converter

1LSB = the voltage of 1LSB,  $V_{\text{REF}}/2^N$

N = the resolution of the ADC converter

MaxRMSSignal = the RMS equivalent of the ADC's full-scale input

RMSNoise = the RMS noise from quantization

SNR = the ratio of RMS signal to RMS noise

**Example**

What is the SNR for an 8-bit ADC converter with 5V reference, assuming only quantization noise?

**Answer**

$$\text{SNR} = 2^{N-1} \sqrt{6} = 2^{8-1} \sqrt{6} = 314$$

$$\text{SNR(dB)} = 20 \log(314) = 49.9 \text{ dB}$$

$$\text{SNR(dB)} = 6.02(8) + 1.76 = 49.9 \text{ dB}$$

Total harmonic distortion (**V<sub>RMS</sub>**)

$$THD(\%) = \left( \frac{RMSDistortion}{MaxRMSSignal} \right) \cdot 100 = \frac{\sqrt{V_2^2 + V_3^2 + V_4^2 + \dots + V_n^2}}{V_1} \cdot 100 \tag{190}$$

$$THD(dB) = 20\log\left( \frac{RMSDistortion}{MaxRMSSignal} \right) \tag{191}$$

Where

THD = Total Harmonic Distortion, the ratio of the RMS distortion to the RMS signal

RMSDistortion = the RMS sum of all harmonic components

MaxRMSSignal = the RMS value of the input signal

V<sub>1</sub> = the fundamental, generally the input signal

V<sub>2</sub>, V<sub>3</sub>, V<sub>4</sub>, ...V<sub>n</sub> = harmonics of the fundamental

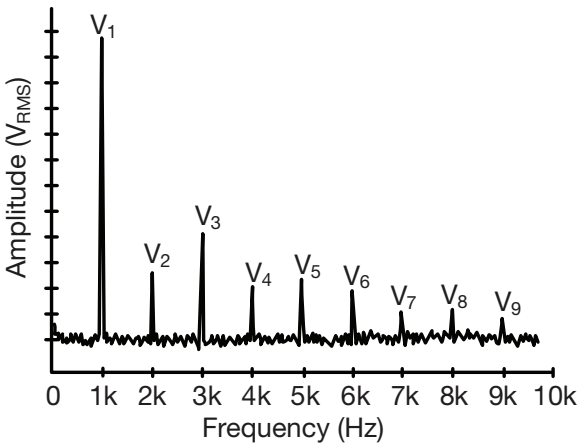


Figure 84: Fundamental and harmonics in **V<sub>RMS</sub>**

## Total harmonic distortion (dBc)

$$\text{THD(dBc)} = 10 \log \left[ 10^{\left(\frac{D_2}{10}\right)} + 10^{\left(\frac{D_3}{10}\right)} + 10^{\left(\frac{D_4}{10}\right)} + \dots + 10^{\left(\frac{D_n}{10}\right)} \right] \quad (192)$$

### Where

THD = Total Harmonic Distortion. The ratio of the RMS distortion to the RMS signal.

$D_1$  = the fundamental, generally the input signal. This is normalized to 0 dBc.

$D_2, D_3, D_4, \dots, D_n$  = harmonics of the fundamental measured relative to the fundamental

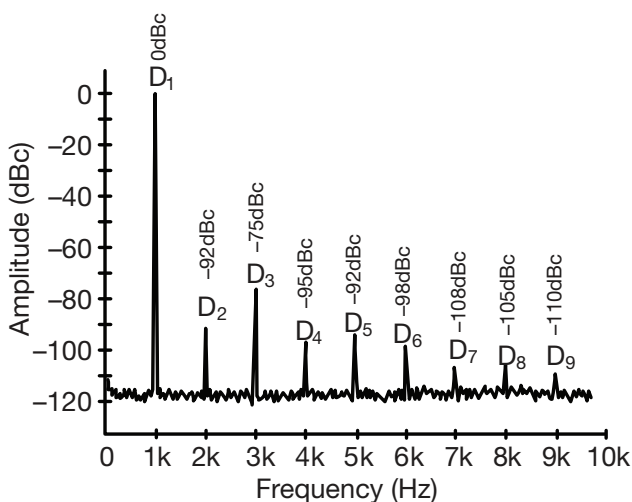


Figure 85: Fundamental and harmonics in dBc

### Example

Determine THD for the example above.

### Answer

$$\text{THD(dBc)} = 10 \log \left[ 10^{\left(\frac{-92}{10}\right)} + 10^{\left(\frac{-75}{10}\right)} + 10^{\left(\frac{-95}{10}\right)} + \dots + 10^{\left(\frac{-110}{10}\right)} \right]$$

$$\text{THD(dBc)} = -74.76 \text{ dB}$$

## AC signals

### Signal-to-noise and distortion (SINAD) and effective number of bits (ENOB)

$$\text{SINAD(dB)} = 20 \log \left( \frac{\text{MaxRMSSignal}}{\sqrt{\text{RMSNoise}^2 + \text{RMSDistortion}^2}} \right) \quad (193)$$

$$\text{SINAD(dB)} = -20 \log \left( \sqrt{10^{\left(\frac{-\text{SNR(dB)}}{10}\right)} + 10^{\left(\frac{-\text{THD(dB)}}{10}\right)}} \right) \quad (194)$$

$$\text{ENOB} = \frac{\text{SINAD(dB)} - 1.76\text{dB}}{6.02} \quad (195)$$

#### Where

MaxRMSSignal = the RMS equivalent of the ADC's full-scale input

RMSNoise = the RMS noise integrated across the ADC converters

RMSDistortion = the RMS sum of all harmonic components

SINAD = the ratio of the full-scale signal-to-noise ratio and distortion

THD = Total Harmonic Distortion. The ratio of the RMS distortion to the RMS signal.

SNR = the ratio of RMS signal to RMS noise

### Example

Calculate the SNR, THD, SINAD and ENOB given the following information:

MaxRMSSignal =  $1.76 V_{\text{RMS}}$

RMSDistortion =  $50 \mu V_{\text{RMS}}$

RMSNoise =  $100 \mu V_{\text{RMS}}$

#### Answer

$$\text{SNR(dB)} = 20 \log \left( \frac{1.76 V_{\text{RMS}}}{100 \mu V_{\text{RMS}}} \right) = 84.9 \text{ dB}$$

$$\text{THD(dB)} = 20 \log \left( \frac{50 \mu V_{\text{RMS}}}{1.76 V_{\text{RMS}}} \right) = -90.9 \text{ dB}$$

$$\text{SINAD(dB)} = 20 \log \left( \frac{1.76 V_{\text{RMS}}}{\sqrt{(100 \mu V_{\text{RMS}})^2 + (50 \mu V_{\text{RMS}})^2}} \right) = 83.9 \text{ dB}$$

$$\text{SINAD(dB)} = -20 \log \left( \sqrt{10^{\left(\frac{-84.9 \text{ dB}}{10}\right)} + 10^{\left(\frac{-90.9 \text{ dB}}{10}\right)}} \right) = 83.9 \text{ dB}$$

$$\text{ENOB} = \frac{83.9\text{dB} - 1.76\text{dB}}{6.02} = 13.65$$

## DC signals

### Noise free resolution and effective resolution

$$\text{NoiseFreeResolution} = \log_2 \left( \frac{2^N}{\text{PeaktoPeakNoiseinLSB}} \right) \quad (196)$$

$$\text{EffectiveResolution} = \log_2 \left( \frac{2^N}{\text{rmsNoiseinLSB}} \right) \quad (197)$$

$$\text{PeaktoPeakNoiseinLSB} \approx 6.6 \times \text{rmsNoiseinLSB} \quad (198)$$

$$\text{EffectiveResolution} \approx \text{NoiseFreeResolution} + 2.7 \quad (199)$$

Note: The maximum effective resolution is never greater than the ADC resolution. For example, a 24-bit converter cannot have an effective resolution greater than 24 bits.

---

### Example

What is the noise-free resolution and effective resolution for a 24-bit converter assuming the peak-to-peak noise is 7 LSBs?

### Answer

$$\text{NoiseFreeResolution} = \log_2 \left( \frac{2^{24}}{7} \right) = 21.2$$

$$\text{EffectiveResolution} = \log_2 \left( \frac{2^{24}}{6.6} \right) = 23.9$$

$$\text{EffectiveResolution} = 21.2 + 2.7 = 23.9$$

---

Settling time and conversion accuracy

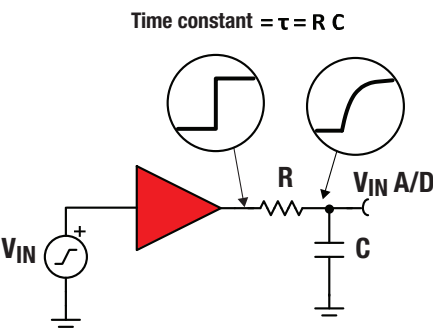


Figure 86: Settling time for RC circuit-related to ADC converters

Table 37: Conversion accuracy achieved after a specified time

| Settling time in time constants ( $N_{TC}$ ) | Accuracy in bits ( $N$ ) | Settling time in time constants ( $N_{TC}$ ) | Accuracy in bits |
|----------------------------------------------|--------------------------|----------------------------------------------|------------------|
| 1                                            | 1.44                     | 10                                           | 14.43            |
| 2                                            | 2.89                     | 11                                           | 15.87            |
| 3                                            | 4.33                     | 12                                           | 17.31            |
| 4                                            | 5.77                     | 13                                           | 18.76            |
| 5                                            | 7.21                     | 14                                           | 20.20            |
| 6                                            | 8.66                     | 15                                           | 21.64            |
| 7                                            | 10.10                    | 16                                           | 23.08            |
| 8                                            | 11.54                    | 17                                           | 24.53            |
| 9                                            | 12.98                    | 18                                           | 25.97            |

$$N = \log_2(e^{-N_{TC}}) \tag{200}$$

Where

$N$  = the number of bits of accuracy the RC circuit has settled to after  $N_{TC}$  number of time constants

$N_{TC}$  = the number of RC time constants. Where one time constant equals  $R \cdot C$ .

Note: For a FSR step. For single-ended input ADC with no PGA front end, FSR (full-scale range) =  $V_{REF}$ .

Settling time and conversion accuracy (cont.)

Table 38: Time required to settle to a specified conversion accuracy

| Accuracy in bits<br>(N) | Settling time in time<br>constants (N <sub>TC</sub> ) | Accuracy in bits<br>(N) | Settling time in time<br>constants (N <sub>TC</sub> ) |
|-------------------------|-------------------------------------------------------|-------------------------|-------------------------------------------------------|
| 8                       | 5.5                                                   | 17                      | 11.78                                                 |
| 9                       | 6.24                                                  | 18                      | 12.48                                                 |
| 10                      | 6.93                                                  | 19                      | 13.17                                                 |
| 11                      | 7.62                                                  | 20                      | 13.86                                                 |
| 12                      | 8.32                                                  | 21                      | 14.56                                                 |
| 13                      | 9.01                                                  | 22                      | 15.25                                                 |
| 14                      | 9.70                                                  | 23                      | 15.94                                                 |
| 15                      | 10.40                                                 | 24                      | 16.64                                                 |
| 16                      | 11.04                                                 | 25                      | 17.33                                                 |

$$N_{TC} = \ln(2^N) \qquad (201)$$

Where

N<sub>TC</sub> = the number of time constants required to achieve N bits of settling. Where one time constant equals R·C.

N = the number of bits of accuracy

Note: For a FSR step. For single-ended input ADC with no PGA front end,  
FSR (full-scale range) = V<sub>REF</sub>.

## ADC system noise calculation

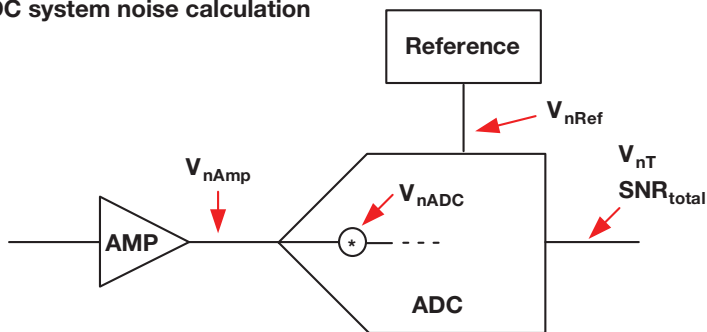


Figure 87: ADC noise

$$V_{FSR\_RMS} = \frac{V_{FSR} \cdot 0.707}{2} \quad (202) \text{ Full-scale RMS input}$$

$$SNR_{ADC} = 20 \cdot \log \left( \frac{V_{FSR\_RMS}}{V_{nADC}} \right) \quad (203) \text{ Solve for noise}$$

$$V_{nADC} = \frac{V_{FSR\_RMS}}{10^{\left( \frac{SNR_{ADC}}{20} \right)}} \quad (204) \text{ From ADC data sheet}$$

$$V_{nT} = \sqrt{(V_{nADC})^2 + (V_{nAmp})^2 + (V_{nRef})^2} \quad (205) \text{ Total RMS noise}$$

## Where

$V_{FSR}$  = the ADC full scale range from the data sheet

$V_{FSR\_RMS}$  = this finds the maximum RMS amplitude of a sine wave applied to an ADC. Dividing the ADC full scale range by 2 converts peak-to-peak to peak. Multiplying by 0.707 converts to RMS.

$SNR_{ADC}$  = Data converter signal to noise ratio specification from data sheet

$V_{nADC}$  = noise in volts RMS derived from the SNR equation. Converting noise to volts allows it to be combined with amplifier and reference noise.

$V_{nAmp}$  = amplifier noise in volts RMS calculated or simulated using data sheet parameters

$V_{nRef}$  = reference noise in volts RMS calculated or simulated using data sheet parameters

$V_{nT}$  = total noise in volts RMS calculated by combining ADC, amplifier, and reference noise

## Effect of clock jitter on ADC SNR

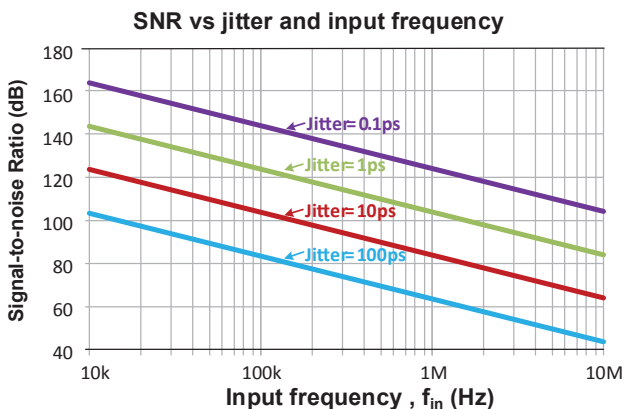


Figure 88: SNR vs jitter and input frequency

$$\text{SNR} = -20 \cdot \log(2 \cdot \pi \cdot f_{in} \cdot t_{\text{jitter}}) \quad (206) \text{ From ADC data sheet}$$

$$\text{SNR} = -20 \cdot \log(2 \cdot \pi \cdot f_{in} \cdot t_{\text{jitter}}) + 10 \cdot \log(\text{OSR}) \quad (207) \text{ SNR limitation from jitter including oversampling}$$

Where

$f_{in}$  = input frequency (Hz)

$t_{\text{jitter}}$  = ADC clock jitter time (seconds)

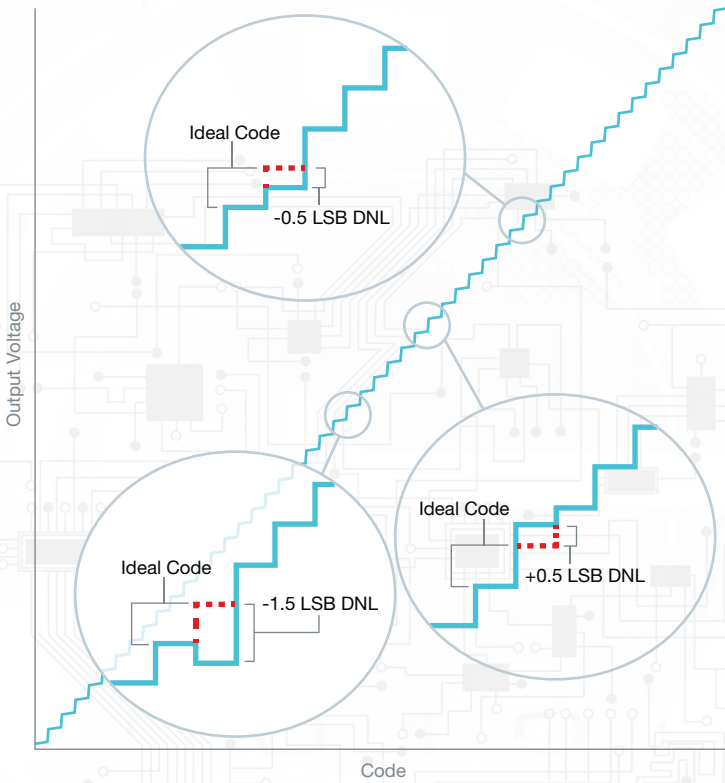
OSR = oversampling ratio

## Notes

[illegible]

# DAC

- DAC errors •
- DAC non-linearity •
- DAC total unadjusted error •



DAC definitions

|                                                                               |                                                     |
|-------------------------------------------------------------------------------|-----------------------------------------------------|
| Resolution = n                                                                | The number of bits used to quantify the output      |
| Number of codes = 2 <sup>n</sup>                                              | The number of input code combinations               |
| Full-scale range output = FSR                                                 | Sets the converter output range and the LSB voltage |
| LSB = FSR / 2 <sup>n</sup>                                                    | The voltage step size of each LSB                   |
| Full-scale output voltage = (2 <sup>n</sup> - 1) × 1LSB                       | Full-scale output voltage of the DAC                |
| Full-scale input code = 2 <sup>n</sup> - 1                                    | Largest code that can be written                    |
| Transfer function: V <sub>OUT</sub> = number of codes × (FSR/2 <sup>n</sup> ) | Relationship between output voltage and input code  |

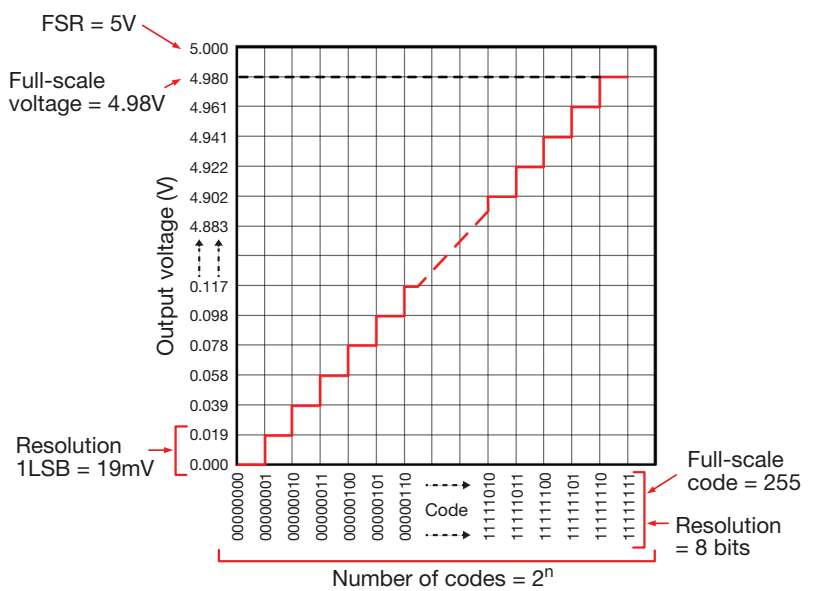


Figure 89: DAC transfer function

## DAC offset error

Offset error is the y-axis intercept based on a two-point best fit measurement extrapolated to a zero input code. This is different from zero code error which is measured with Code = 0H and includes the nonlinear effects as the DAC output approaches zero volts.

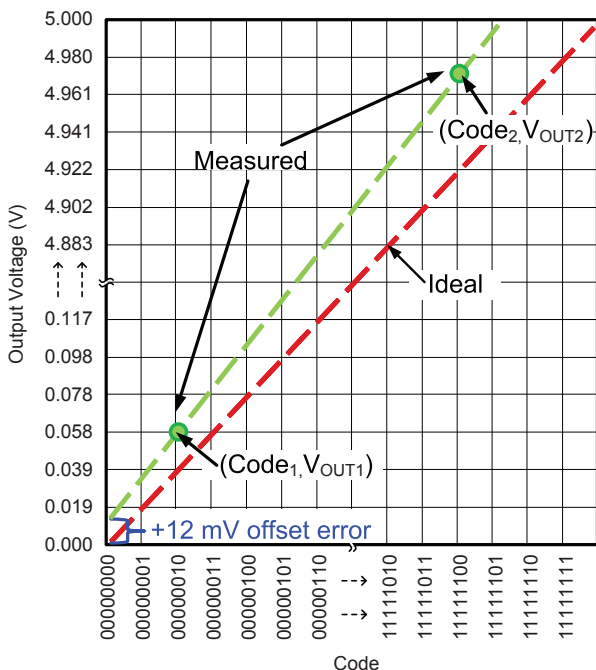


Figure 90: Offset error illustration

$$V_{OUT} = m_m \cdot \text{Code} + \text{Offset} \quad (208) \text{ General equation for best fit line}$$

$$m_m = \frac{V_{OUT2} - V_{OUT1}}{\text{Code}_2 - \text{Code}_1} \quad (209) \text{ Measured slope}$$

$$\text{Offset} = V_{OUT1} - m_m \cdot \text{Code}_1 \quad (210) \text{ Offset}$$

Where

$V_{OUT}$  = DAC output voltage

$m_m$  = measured slope

Code = input digital code

Offset = the offset of a best fit line

DAC gain error

Gain error describes the deviation from the ideal slope of the DAC transfer function. Similar to offset error, this specification is measured at the DAC output using a two-point line of best fit, which is then compared against the ideal gain and expressed in a percentage.

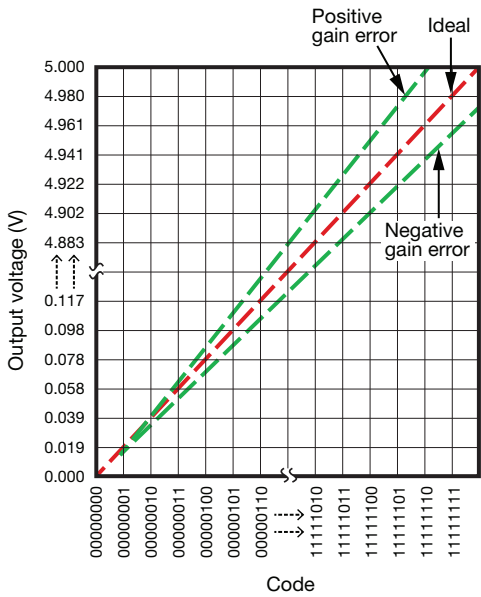


Figure 91: Gain error illustration

$V_{OUT} = m_m \cdot \text{Code} + \text{Offset}$  (211) General equation for best fit line

$m_m = \frac{V_{OUT2} - V_{OUT1}}{\text{Code}_2 - \text{Code}_1}$  (212) Measured slope

$GE = \left( \frac{m_m - m_{ideal}}{m_{ideal}} \right) \cdot 100$  (213) Gain error in percentage

Where

$V_{OUT}$  = DAC output voltage

$m_m$  = measured slope

Code = input digital code

Offset = the offset of a best fit line

Note: ( $\text{Code}_1$ ,  $V_{OUT1}$ ) and ( $\text{Code}_2$ ,  $V_{OUT2}$ ) are two data points on the measured transfer function. See Figure 90.

## DAC zero-code error / negative full-scale error

Zero-code error (sometimes called negative full-scale error) is an end-point error measured when all 0's are loaded into the DAC data register. For a DAC with bipolar outputs, this may also be called negative full-scale error. The intention is to describe how close to the negative rail the DAC output can get when set to the minimal output value. Zero-code error is different from offset error in that it includes the potentially nonlinear output swing limitations, whereas the offset error is the offset of the best fit transfer function. The specified test conditions will indicate what, if any, negative supply was used to help assess the swing to ground capability at zero code.

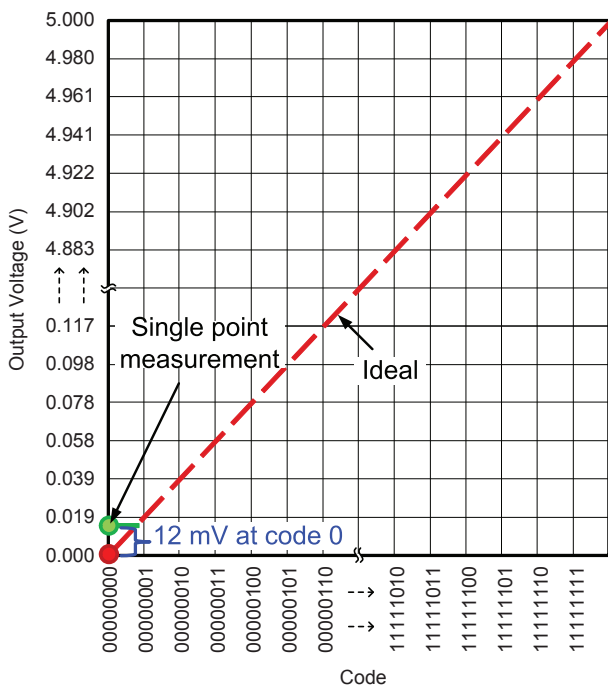


Figure 92: Zero-code error illustration

DAC bipolar zero error

Bipolar zero error is a special datasheet parameter reserved for DACs with bipolar voltage or current outputs. It describes the DAC error when set to mid-scale, assuming a symmetrical output span, where the ideal DAC should be 0V or 0A. This specification is the mid-scale combination of both offset and gain errors. The specification is arrived at based on statistical analysis and, therefore, mathematically the summation of offset and gain errors may not match this value exactly.

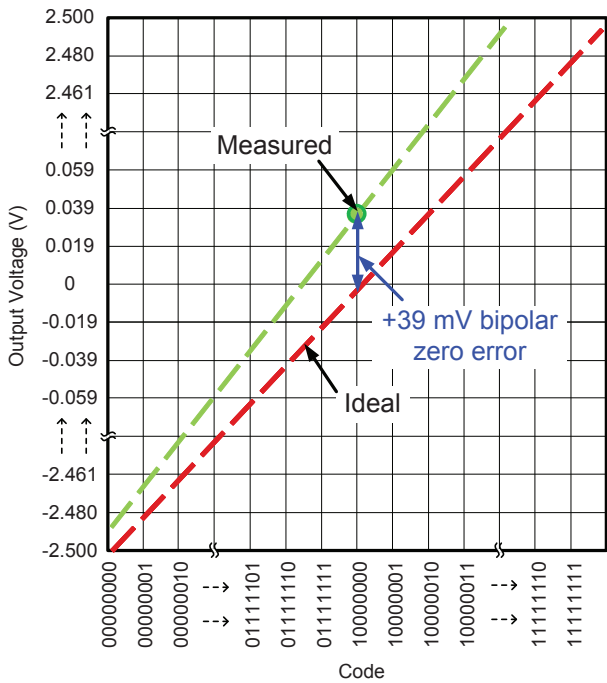


Figure 93: Bipolar zero error illustration

DAC full-scale error

Full-scale error is an end-point error measured when all 1's are loaded into the DAC data register. The intention is to describe how close to the positive rail the DAC output can get when set to the maximum output value. The specified test conditions will indicate what positive supply was used.

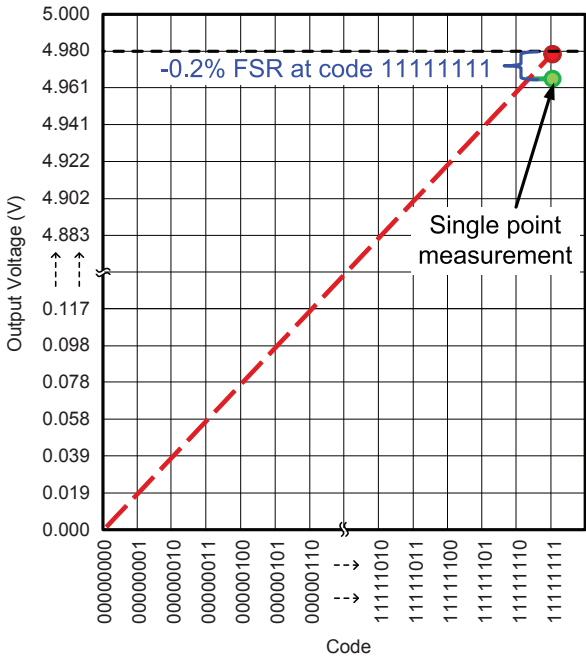


Figure 94: Full-scale error illustration

## DAC differential non-linearity

Differential non-linearity, or commonly abbreviated DNL, describes the actual measured step sizes versus ideal and is expressed in terms of least significant bits or LSBs. The electrical characteristics table of a DAC datasheet will only express a single minimum and maximum value, expressing the worst case observed across every code in the linear region of the DAC transfer function. When near the positive or negative rails, especially outside of the ranges defined by the high-code and low-code used to measure offset and gain errors, DNL performance will be degraded due to saturation near the rails. Most modern DACs are monotonic meaning that the output voltage will always increase as input codes increase. Figure 95 shows both monotonic and non-monotonic DNL.

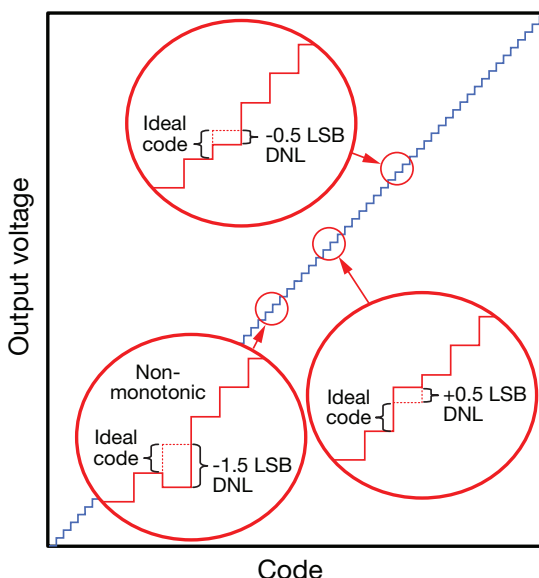


Figure 95: DNL error illustration

## DAC integral non-linearity

INL (Integral Non-Linearity) is sometimes referred to as relative accuracy. This is the deviation of the transfer function from an end point fit. While DNL describes the relationship of actual code step-sizes to ideal, INL expresses the cumulative effects of sequential DNL errors. INL is the maximum deviation from an end point fit straight line. This error source cannot be corrected using a simple two point fit calibration.

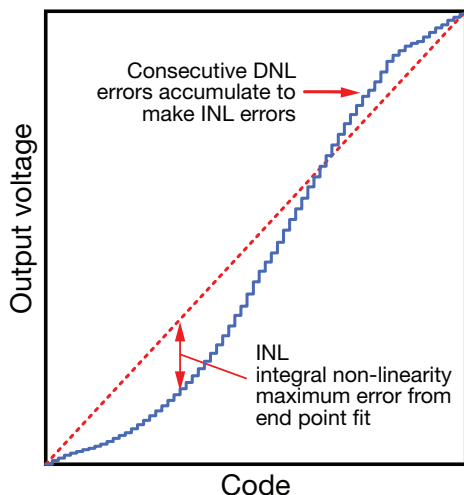


Figure 96: INL error illustration

## DAC total unadjusted error

The equation below is for the total unadjusted error (or TUE). TUE is the statistical combinations of error sources in the linear region of operation for the DAC. In order to perform the above TUE calculation it is necessary to have each of the parametric error sources in the same units. Table 7 shows the calculations required to convert to different units (e.g. from percentage to parts per million).

$$\text{TUE} = \sqrt{\text{OffsetError}^2 + \text{GainError}^2 + \text{INLError}^2} \quad (214) \text{ Gain error in percentage}$$

### Where

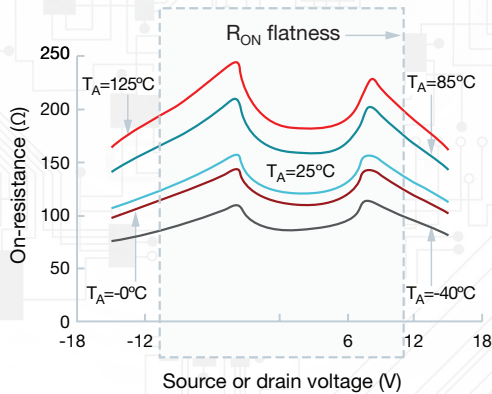
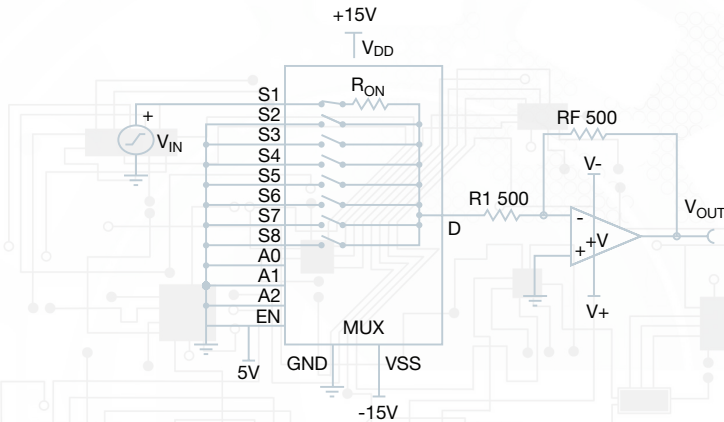
OffsetError = the offset of a best fit line through the transfer function. See Figure 90.

GainError = the difference between the ideal slope and the measured slope.  
See Figure 91.

INLError = the maximum deviation from a best fit line through the transfer function.  
See Figure 96.

# Multiplexer

- CMOS switch construction •
- ON-resistance •
- ON and OFF capacitance •
- Leakage current •
- Charge injection •
- Bandwidth •
- Channel-to-channel crosstalk •
- OFF-isolation •
- Total harmonic distortion plus noise •



## CMOS switch construction

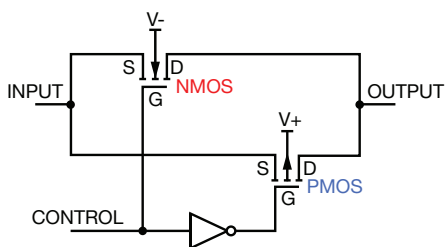


Figure 97: Typical CMOS switch construction

Typical CMOS switch elements

- Parallel combination of N channel and P channel FET
- Control signal that controls the state of the switch

## ON-resistance ( $R_{ON}$ )

Resistance between sources to drain terminal when switch is closed

- PMOS conducts for positive input voltages
- NMOS conducts for negative input voltages
- Combined  $R_{ON}$  is lower than individual resistance of the NMOS or PMOS that form the switch

Varies with

- MUX input voltage
- Operating ambient temperature

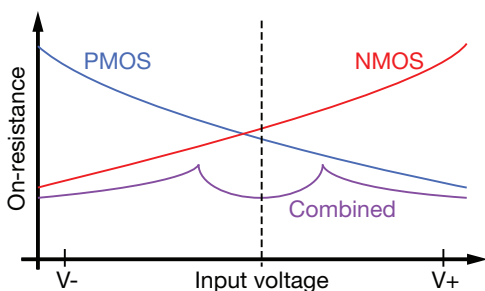


Figure 98: Typical MUX ON-resistance curve vs input voltage

## $R_{ON}$ flatness

Difference between maximum and minimum ON-resistance over a specified input range

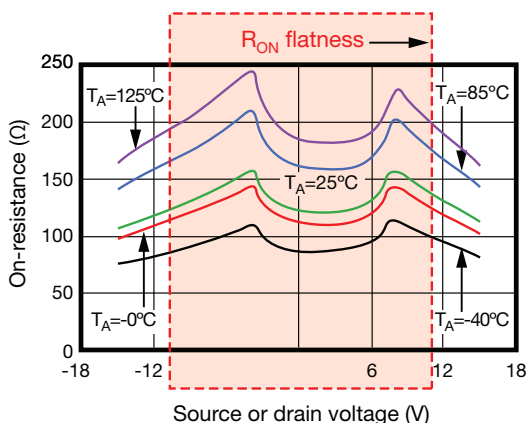


Figure 99:  $R_{ON}$  flatness illustration

## Effective op amp gain including MUX $R_{ON}$

This section shows the impact of  $R_{ON}$  flatness on gain error and non-linearity. Figure 99 shows the circuit and Figure 100 shows the measured results.

$$AG = \frac{V_{OUT}}{V_{IN}} = \frac{-R_F}{(R_1 + R_{ON})}$$

(215) Effective gain for op amp with MUX

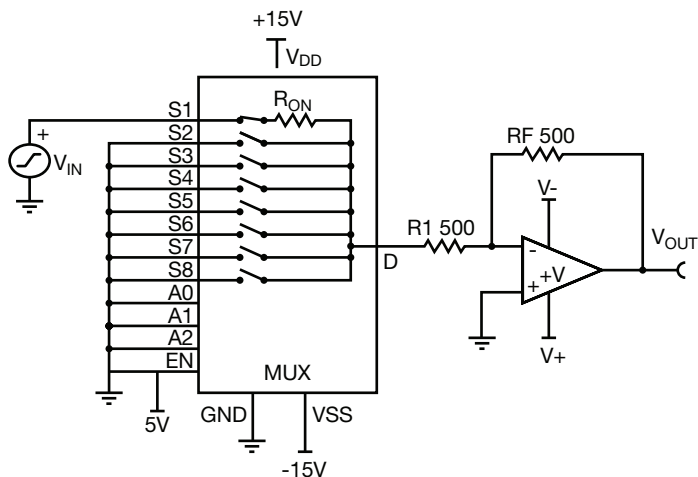
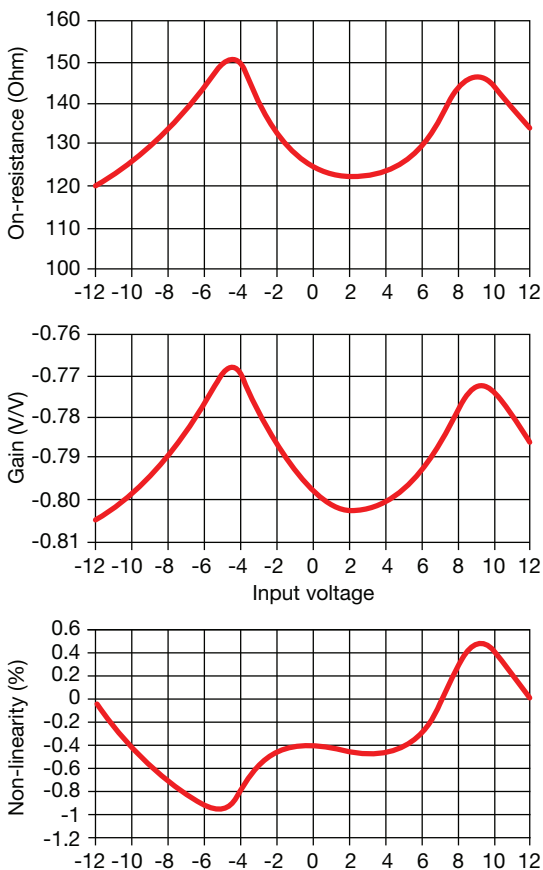


Figure 100: Front-end MUX followed by an inverting amplifier stage

Effective op amp gain including MUX  $R_{ON}$  (cont.)Figure 101: Effect of varying  $R_{ON}$  causing gain error and non-linearity

## Design tips

- Use high impedance stage between MUX output and signal conditioning
- Use a multiplexer with lower  $R_{ON}$  (at the expense of other design trade-offs)

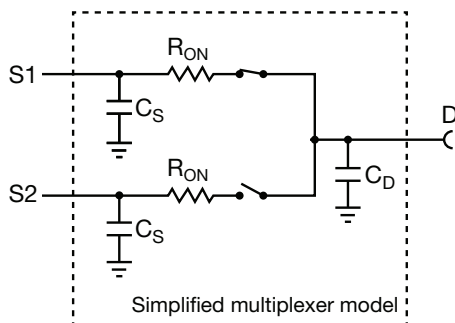
## ON and OFF capacitance ( $C_{ON}$ / $C_{OFF}$ )

- $C_{OFF}$  = parasitic capacitance when the switch is OFF

$$C_{OFF} = C_S \text{ (on source side) or } C_D \text{ (on drain side)} \quad (216)$$

- $C_{ON}$  = parasitic capacitance when the switch is ON

$$C_{ON} \approx C_S + C_D \quad (217)$$



**Figure 102: Simplified model for MUX parasitic capacitance calculation**

## Design tips

$$\text{Settling time} = t_{\text{TRANSITION}} + (R_{ON} \cdot C_D \cdot K) \quad (218)$$

## Where

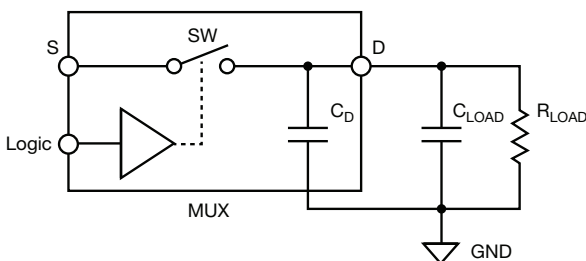
$t_{\text{TRANSITION}}$  = MUX channel-to-channel transition time (refer to MUX specification)

$R_{ON}$  = switch ON-resistance between sources and drain

$C_D$  = switch drain parasitic capacitance

$K$  = number of time constants to settle to a N bit resolution ADC,  $K = \ln(2^N)$

## MUX settling time with $C_{LOAD}$ and $R_{LOAD}$



**Figure 103: Simplified model for MUX settling time calculation**

$$\text{Settling time} = t_{\text{TRANSITION}} + \frac{R_{\text{ON}} \cdot R_{\text{LOAD}}}{R_{\text{ON}} + R_{\text{LOAD}}} (C_{\text{LOAD}} + C_D) \cdot K \quad (219)$$

### Where

$t_{\text{TRANSITION}}$  = MUX channel-to-channel transition time (refer to MUX specification)

$R_{\text{ON}}$  = switch ON-resistance between sources and drain

$R_{\text{LOAD}}$  = resistor connected to MUX output

$C_{\text{LOAD}}$  = capacitor connected to MUX output

$C_D$  = switch drain parasitic capacitance

$K$  = number of time constants to settle to a  $N$  bit resolution ADC,  $K = \ln(2^N)$

### Example

Determine the settling time of a MUX to 14-bit accuracy.

$R_{\text{ON}}=125\Omega$ ;  $C_{D(\text{OFF})}=7.5\text{pF}$

$R_{\text{LOAD}}=1\text{k}\Omega$ ;  $C_{\text{LOAD}}=5\text{pF}$

$t_{\text{TRANSITION}}=92\text{ns}$

### Answer

$$\text{Settling time} = 92\text{ns} + \frac{125 \cdot 1000}{125 + 1000} \cdot (5\text{pF} + 7.5\text{pF}) \cdot \ln(2^{14}) = 105.5\text{ns}$$

## Leakage current

### Off leakage current

- $I_{S(OFF)}$  = input leakage current flows through  $R_{SOURCE}$
- $I_{D(OFF)}$  = output leakage current flows through  $R_L$

$$V_{ERROR(OUTPUT)} = R_L \cdot I_{D(OFF)} \quad (220)$$

### On leakage current

- $I_{D(ON)} = I_{LEAKAGE}$

$$V_{ERROR(OUTPUT)} = (R_{ON} + R_{SOURCE}) \cdot I_{D(ON)} \quad (221)$$

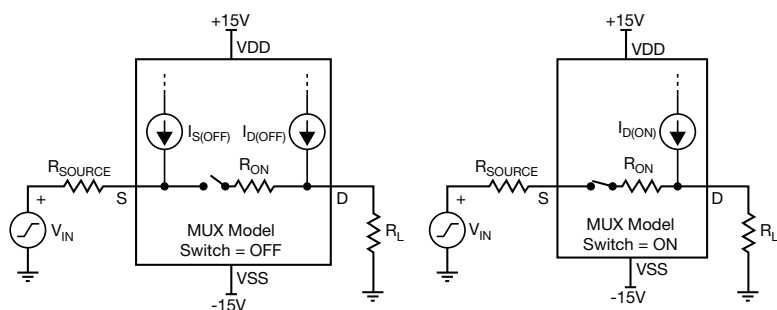


Figure 104: Simplified models for OFF and ON leakage current through a MUX

## Example

Determine the Switch = ON error caused by MUX leakage current in an 18-bits system:  
Assume  $R_L$  is a very high input impedance ( $R_L > 100M\Omega$ , i.e. an op amp input)

$$R_{SOURCE} = 1M\Omega$$

$$R_{ON} = 100\Omega$$

$$I_{D(ON)} = 100pA$$

$$V_{REF} = 5V$$

## Answer

$$V_{LSB} = \frac{5V}{2^{18}} = 19.073\mu V$$

$$V_{ERROR} = I_{D(ON)} \cdot (R_{SOURCE} + R_{ON}) = (100pA) \cdot (1M\Omega + 100\Omega) = 100\mu V$$

$$BIT_{ERROR} = \frac{V_{ERROR}}{V_{LSB}} = \frac{100\mu V}{19.073\mu V} = 5.24 \text{ codes}$$

## Charge injection ( $Q_{INJ}$ )

Voltage change introduced at the output of switch when switch is turned ON or OFF

$$Q_{INJ} = (C_D + C_L) \cdot \Delta V_{OUT} \quad (222)$$

With large load capacitance, effect of  $C_D$  can be ignored

$$V_{ERROR} = \Delta V_{OUT} \approx \frac{Q_{INJ}}{C_L} \quad (223)$$

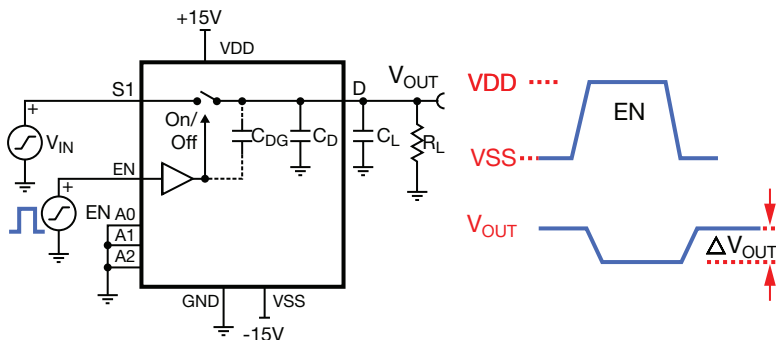


Figure 105: Simplified model for MUX charge injection error

A typical multiplexer charge injection curve vs. input (source) voltage is shown below.

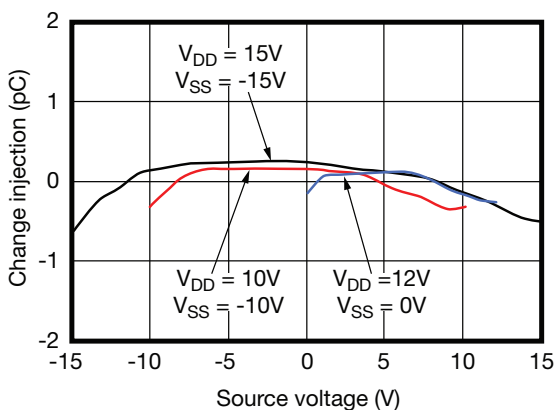


Figure 106: Typical charge injection curve vs. source voltage

## Bandwidth (BW)

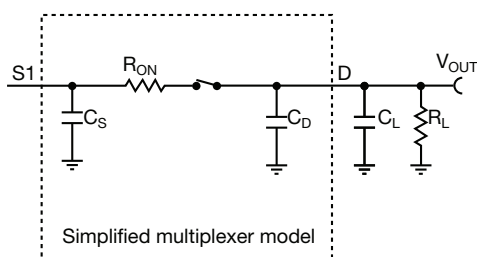
The frequency at which the output is attenuated by 3 dB from the pass band (DC) response.

$$\frac{V_{OUT}}{V_{IN}} = \left( \frac{R_L}{R_L + R_{ON}} \right) \cdot \left( \frac{1}{\frac{f}{f_{-3dB}} + 1} \right) \quad (224)$$

$$f_{-3dB} = \frac{1}{2\pi \left( \frac{R_L R_{ON}}{R_L + R_{ON}} \right) (C_D + C_L)} \quad (225)$$

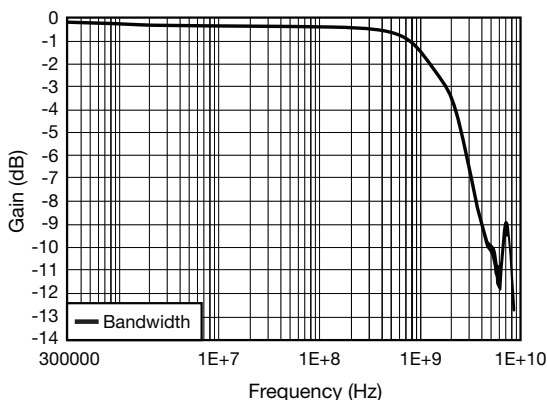
If  $R_L \gg R_{ON}$ :

$$f_{-3dB} = \frac{1}{2 \cdot \pi \cdot R_{ON} \cdot (C_D + C_L)} \quad (226)$$



**Figure 107: Simplified model for MUX bandwidth calculation**

A typical multiplexer bandwidth response vs. frequency is shown below. The device exhibits a -3dB bandwidth of approximately 2GHz.



**Figure 108: Typical bandwidth response vs. frequency curve**

Channel-to-channel crosstalk ( $X_{TALK}$ )

Crosstalk is defined as the amount of signal read at the input of an OFF channel ( $V_{OUT}$ ), when  $V_S$  is applied to an ON channel.

$$X_{TALK} = 20 \cdot \log \left( \frac{V_{OUT}}{V_S} \right) \tag{227}$$

Where

$V_{OUT}$  = voltage measured at source pin of OFF channel

$V_S$  = voltage applied to source pin of ON channel

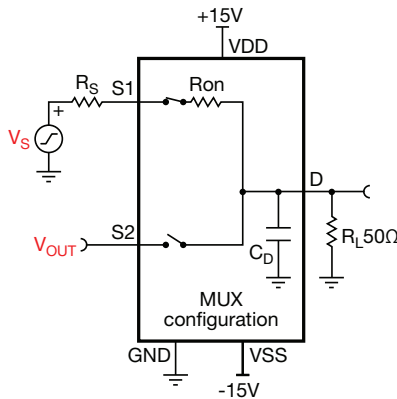


Figure 109: Simplified model for MUX crosstalk calculation

A typical multiplexer crosstalk vs. frequency is shown below for both adjacent and non-adjacent channels.

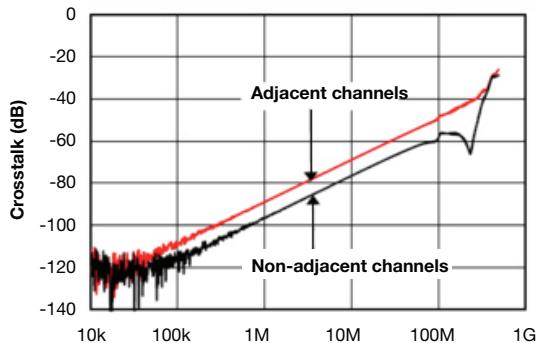


Figure 110: Typical channel-to-channel crosstalk vs. frequency curve

OFF-isolation

Voltage at output pin of a multiplexer when a known signal is applied at the source pin of an off-channel

$$\text{OFF\_isolation} = 20 \cdot \log\left(\frac{V_{\text{OUT}}}{V_{\text{IN}}}\right)$$

(228)

Where

$V_{\text{OUT}}$  = voltage measured at source pin of OFF channel

$V_{\text{IN}}$  = voltage applied at source pin of OFF channel

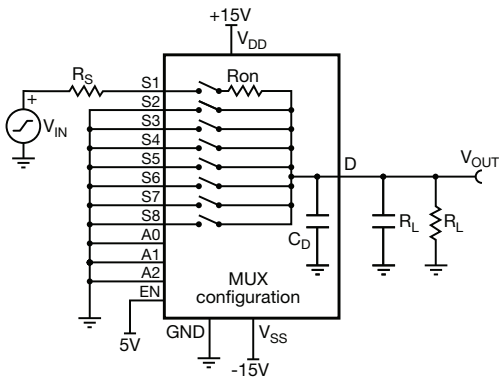


Figure 111: Simplified model for MUX OFF-isolation calculation

A typical multiplexer OFF-isolation vs. frequency is shown below for both adjacent and non-adjacent channels.

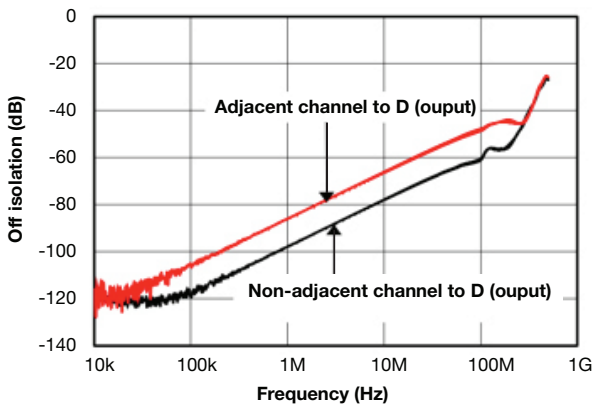


Figure 112: Typical OFF-isolation vs. frequency curve

## Total harmonic distortion plus noise (THD+N)

- The ratio of the sum of all harmonic components and total RMS noise to the fundamental signal at the multiplexer output
- Highly dependent on the ON-resistance ( $R_{ON}$ ) of the multiplexer

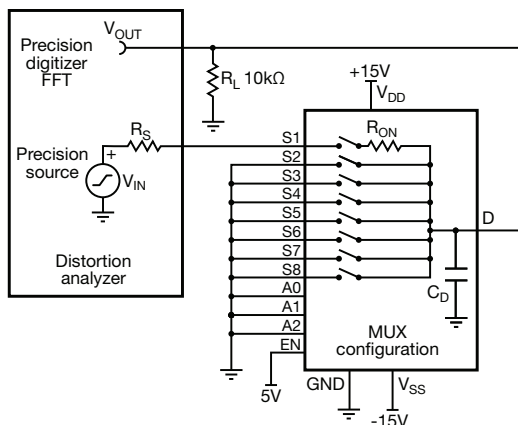


Figure 113: Typical THD+ measurement setup

A typical multiplexer THD+N vs. frequency curve is shown below

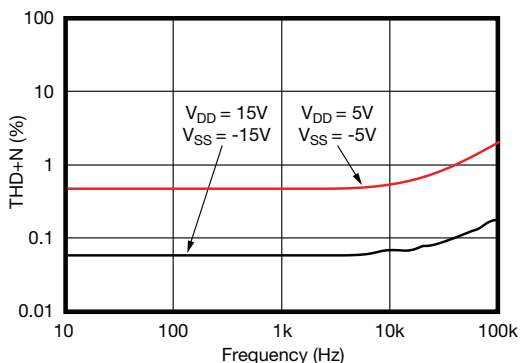


Figure 114: Typical THD+N vs. frequency curve

## Design tips

- Use high impedance stage between MUX output and signal conditioning
- Use a multiplexer with lower  $R_{ON}$  (at the expense of other design trade-offs)

## Notes

[illegible]

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