

# PROJECT: Precision Underwater Positioner

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## Title: Angular motion requirement

### SYSTEM SPECIFICATIONS:

- Max travel increment: 0.1mm
- Max hysteresis: 0.1mm
- Relative position: 0.1mm
- Relative Accuracy: 1mm
- Travel time for 150mm = 60 sec

### PROPERTIES & ASSUMPTIONS:

$$180 \text{ degrees} = \pi \text{ radians}$$

$$\text{arc}_{\min} := \frac{1}{60} \cdot \text{deg}$$

$$\text{arc}_{\sec} := \frac{1}{3600} \cdot \text{deg}$$

Given: Angle at vertex  $\theta_A := .01 \cdot \text{deg}$

$$\text{One radian} = \text{deg}$$

$$\text{rad} = 57.296 \text{ deg}$$

$$\theta_A = 1.745 \times 10^{-4} \text{ rad}$$

$$\text{One degree} = \text{rad}$$

$$\text{deg} = 0.017 \text{ rad}$$

$$\text{Arm length} = r_x$$

Rotary Axis-1  $r_1 := 16 \cdot \text{in}$

Rotary Axis-(Pan)  $r_2 := 8 \cdot \text{in}$

Rotary Axis-(Tilt)  $r_3 := 4 \cdot \text{in}$

### CALCULATION:

Arc Length = S1 & S2

$$S_1 := \theta_A \cdot r_1 \quad S_2 := \theta_A \cdot r_2$$

$$S_1 = 2.793 \times 10^{-3} \text{ in} \quad S_2 = 1.396 \times 10^{-3} \text{ in}$$

(Alternate check @ arc length = .002 inch)

Therefore if Arc length =  $S_X$   $S_X := .002 \cdot \text{in}$

$$\theta_1 := \frac{S_X}{r_1} \quad \theta_2 := \frac{S_X}{r_2} \quad \theta_3 := \frac{S_X}{r_3}$$

$$\theta_1 = 1.25 \times 10^{-4} \text{ rad} \quad \theta_1 = 7.162 \times 10^{-3} \text{ deg} \quad \theta_1 = 25.783 \text{ arc}_{\sec}$$

$$\theta_2 = 2.5 \times 10^{-4} \text{ rad} \quad \theta_2 = 0.014 \text{ deg} \quad \theta_2 = 51.566 \text{ arc}_{\sec}$$

$$\theta_3 = 5 \times 10^{-4} \text{ rad} \quad \theta_3 = 0.029 \text{ deg} \quad \theta_3 = 103.132 \text{ arc}_{\sec}$$

