

Design and Modeling of Fluid Power Systems

ME 597/ABE 591 - Lecture 2

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Fluid Properties



Density

Compressibility

Viscosity

Properties of Fluids

Change of density with pressure

Viscosity- temperature behavior

Change of density with temperature

Viscosity-pressure behavior

- Oxidative, hydrolytic and thermal stability
- Foaming (release air without forming emulsions)
- Lubricity (boundary lubricating property)
- Air/gas absorption
- Pour point
- Flash point/fire point

Fluid Properties

Compressibility of a real fluid



Density is defined: $\rho = \frac{m}{V}$ and $\rho = f(p, \theta)$

Change of fluid volume with pressure and temperature: $V = f(p, \theta)$

$$dV = \left(\frac{\partial V}{\partial p} \right)_{\theta} \cdot dp + \left(\frac{\partial V}{\partial \theta} \right)_p \cdot d\theta$$

$$\rho_{oil} \approx 870 \text{ kg} \cdot \text{m}^3$$

Isothermal coefficient of compressibility

$$\beta_p = -\frac{1}{V} \left(\frac{\partial V}{\partial p} \right)_{\theta} = \frac{1}{\rho} \left(\frac{\partial \rho}{\partial p} \right)_{\theta} \quad \Rightarrow \quad dV = -V \cdot \beta_p \cdot dp$$

Bulk modulus is defined as reciprocal of compressibility coefficient

$$K = \frac{1}{\beta_p}$$

Therefore we can write:

$$dV = -\frac{V}{K} \cdot dp$$

Fluid Properties

Bulk modulus



Fluid can be compressed isothermally or isentropically (adiabatic process)



Isothermal bulk modulus K

$$\tan \alpha = \frac{dV}{dp} = -\frac{V}{K} \quad \Rightarrow \quad \int_1^2 \frac{dV}{V} = -\int_1^2 \frac{1}{K} \cdot dp$$

$$\ln V_2 - \ln V_1 = -\frac{1}{K} \cdot (p_2 - p_1)$$

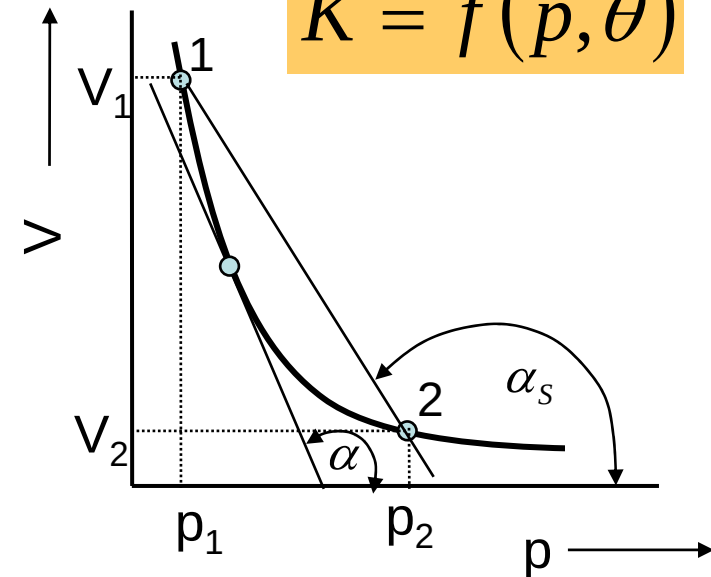
$$V_2 = V_1 \cdot e^{-\frac{1}{K}(p_2 - p_1)}$$

$$\Delta V = V_1 - V_2 = V_1 \cdot \left[1 - e^{-\frac{1}{K}(p_2 - p_1)} \right]$$



Adiabatic bulk modulus K_A

$$K = f(p, \theta)$$



In practice secant bulk modulus K_S is often used!

$$\tan \alpha_s = \frac{\Delta V}{\Delta p} = \frac{V_2 - V_1}{p_2 - p_1} = -\frac{V_1}{K_S}$$

$$K = 1.8 \cdot 10^9 \div 2.1 \cdot 10^9 \text{ Pa}$$

Influence of unsolved air



Due to unsolved air the compressibility of the fluid (fluid-air mixture) changes.
For the bulk modulus of fluid – air mixture K^* can be derived:

p_0 ... atmospheric pressure

In a simplified way for the change of volume of the fluid – air mixture dV_M we can derive:

$$dV_M = dV_F + dV_{Air}$$

$$\frac{K^*}{K} = \frac{1 + \frac{V_{air}}{V_F}}{1 + \frac{p_0 \cdot V_{air}}{p \cdot V_F} \cdot \frac{K}{p}}$$

For isothermal process follows:

$$p \cdot V_{Air} = (p + dp) \cdot (V_{Air} - dV_{Air})$$

simplified:



$$dp \cdot V_{Air} = dV_{Air} \cdot p$$

Change of air volume with pressure:

and for the change of fluid volume:

$$dV_{Air} = \frac{V_{Air}}{p} dp$$

$$dV_F = \frac{V_F}{K} dp$$

$$dV_M = dV_F + dV_{Air} = \frac{V_F}{K} \cdot dp + \frac{V_{Air}}{p} \cdot dp$$



Influence of unsolved air

$$dV_M = dV_F + dV_{Air} = \frac{V_F}{K} \cdot dp + \frac{V_{Air}}{p} \cdot dp \quad (1) \quad \text{and} \quad dV_M = \frac{V}{K^*} dp \quad (2)$$

Due to $V_{Air} \ll V_F$ we can make the following simplification: $V_F = V$

then

$$dV_F = \frac{V}{K} dp \quad (3)$$

Substituting Eq. (3) in Eq. (1) and (2) follows:

$$\frac{V}{K^*} \cdot dp = \frac{V}{K} \left(1 + \frac{V_{Air}}{V} \cdot \frac{K}{p} \right) \cdot dp \quad \Rightarrow$$

$$\frac{K^*}{K} = \frac{1}{1 + \frac{V_{Air}}{V} \cdot \frac{K}{p}}$$

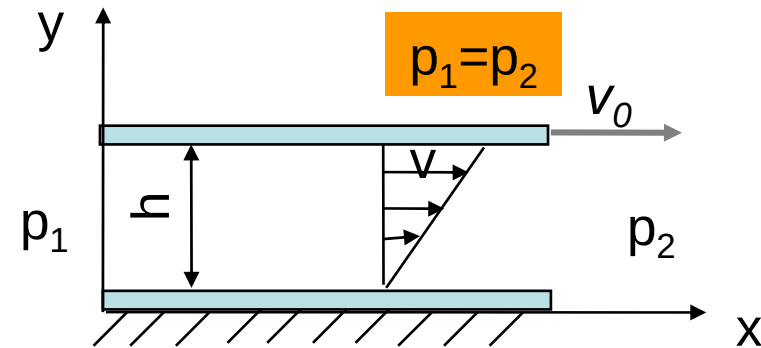
Example: Calculate how the bulk modulus of the fluid – air mixture with 0.5% unsolved air at $p = 100 \text{ bar} = 10^7 \text{ Pa}$ is changed. The bulk modulus of the fluid is $K = 2 \cdot 10^9 \text{ Pa}$.

$$K^* = \frac{K}{1 + \frac{V_{Air}}{V} \cdot \frac{K}{p}} = \frac{2 \cdot 10^9 \text{ Pa}}{1 + 0.005 \cdot \frac{2 \cdot 10^9 \text{ Pa}}{10^7 \text{ Pa}}} = 1 \cdot 10^9 \text{ Pa} = 0.5 K$$

Viscosity of a real fluid



The viscosity of a fluid is the measure of its resistance to flow or of its internal friction. According to Newton's law the shearing stress between adjacent layers of a viscous fluid is proportional to the rate of shear in the direction perpendicular to the fluid motion (flow direction).



$$\tau = \mu \cdot \frac{\partial v}{\partial y} \quad \mu \dots \text{dynamic viscosity [Pa}\cdot\text{s}=\text{N}\cdot\text{s/m}^2\text{]}$$

$$\mu = f(p, \theta) = \mu_0 \cdot e^{\alpha_p \cdot p - k_\theta \cdot (\theta - \theta_0)}$$

α_p and k_θ are empirical constants for a given fluid, whereas $\alpha_p = f(\theta)$

Typical values for mineral oil: $\alpha_p = 2.1 \cdot 10^{-8} \text{ Pa}^{-1}$
 $k_\theta = 0.036 \text{ K}^{-1} \div 0.057 \text{ K}^{-1}$

Viscosity of a real fluid

Kinematic viscosity

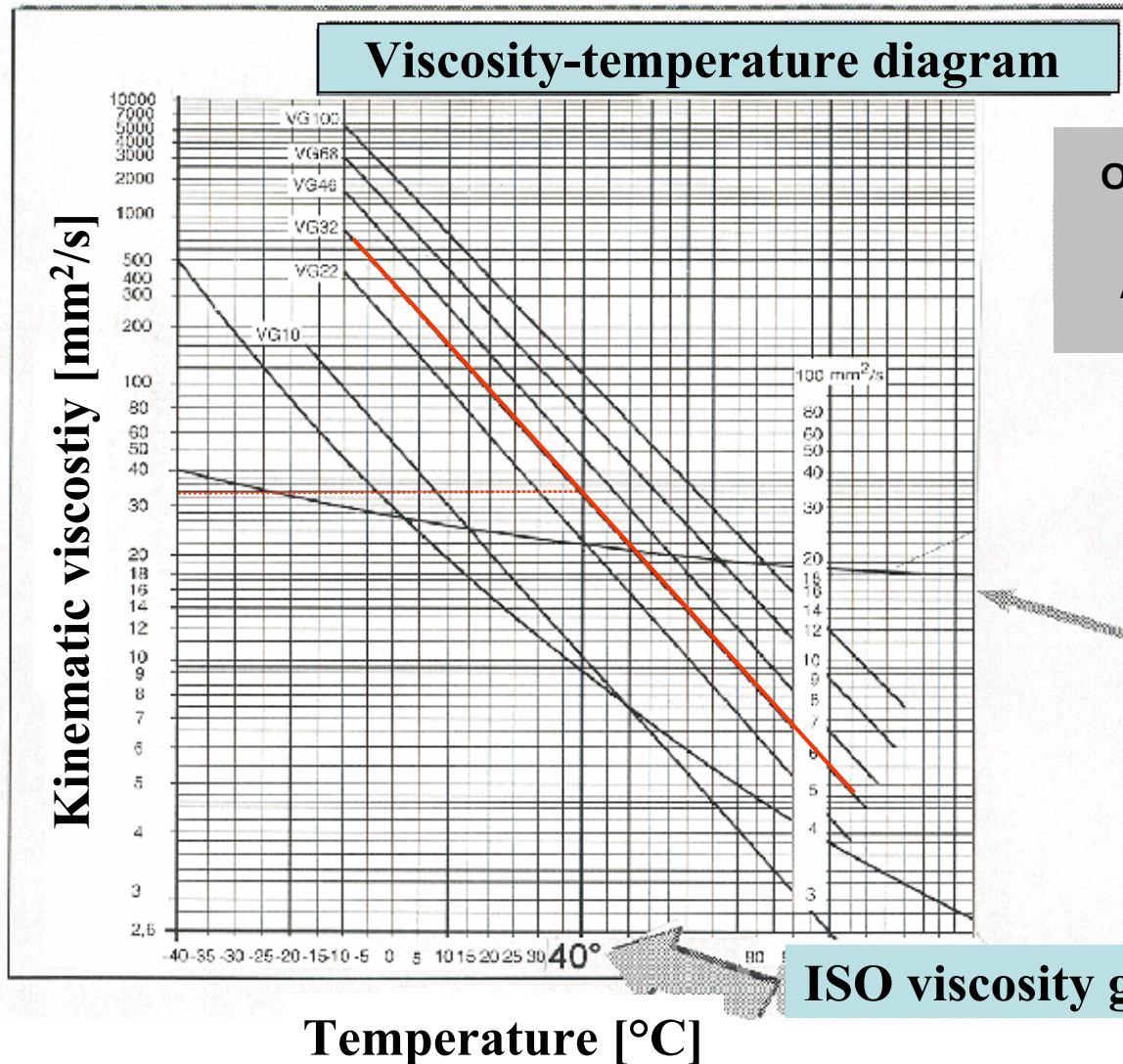


Kinematic viscosity:
$$\nu = \frac{\text{dynamic viscosity}}{\text{density}} = \frac{\mu}{\rho} \quad [\text{m}^2 \cdot \text{s}^{-1}] \text{ or } [\text{cSt}]$$

ISO Viscosity Grades for mineral oils (ISO 3448)

ISO VG 10	mean value at 40°C	10 mm ² ·s ⁻¹ , (cSt)
ISO VG 22		22 mm ² ·s ⁻¹
ISO VG 32		32 mm ² ·s ⁻¹
ISO VG 46		46 mm ² ·s ⁻¹
ISO VG 100		100 mm ² ·s ⁻¹

Viscosity-Temperature



Ordinate: $\lg \lg (v+0.8)$

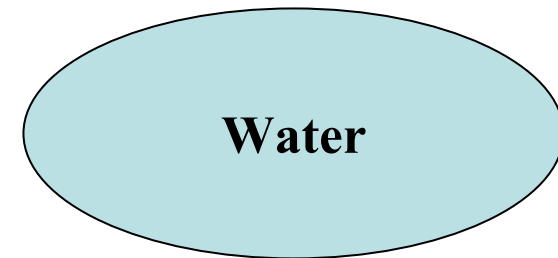
Abszissa: $\lg T$

Skydrol (Phosphate ester)

Types of Hydraulic Fluids



- **Petroleum based fluids (mineral oils)** usually with additives to
 - prevent oxidation and corrosion
 - reduce foaming
 - improve lubricity
 - increase viscosity index
- **Fire resistant fluids**
 - oil – water emulsions (20% H₂O)
 - water in oil emulsion (about 40% H₂O)
 - water free synthetic fluids (Phosphate ester)
- **Biodegradable fluids**
 - Vegetable oil base
 - Polyglycol base
 - Synthetic ester



Water versus Mineral Oil



Viscosity 30 lower

50% reduction of
pressure loss

Viscosity-temperature dependency 14 lower

Specific heat 2.3 higher

Better cooling-
ability

5 times higher thermal conductivity

50 % higher bulk modulus

Higher stiffness

Air –release ability 30times better

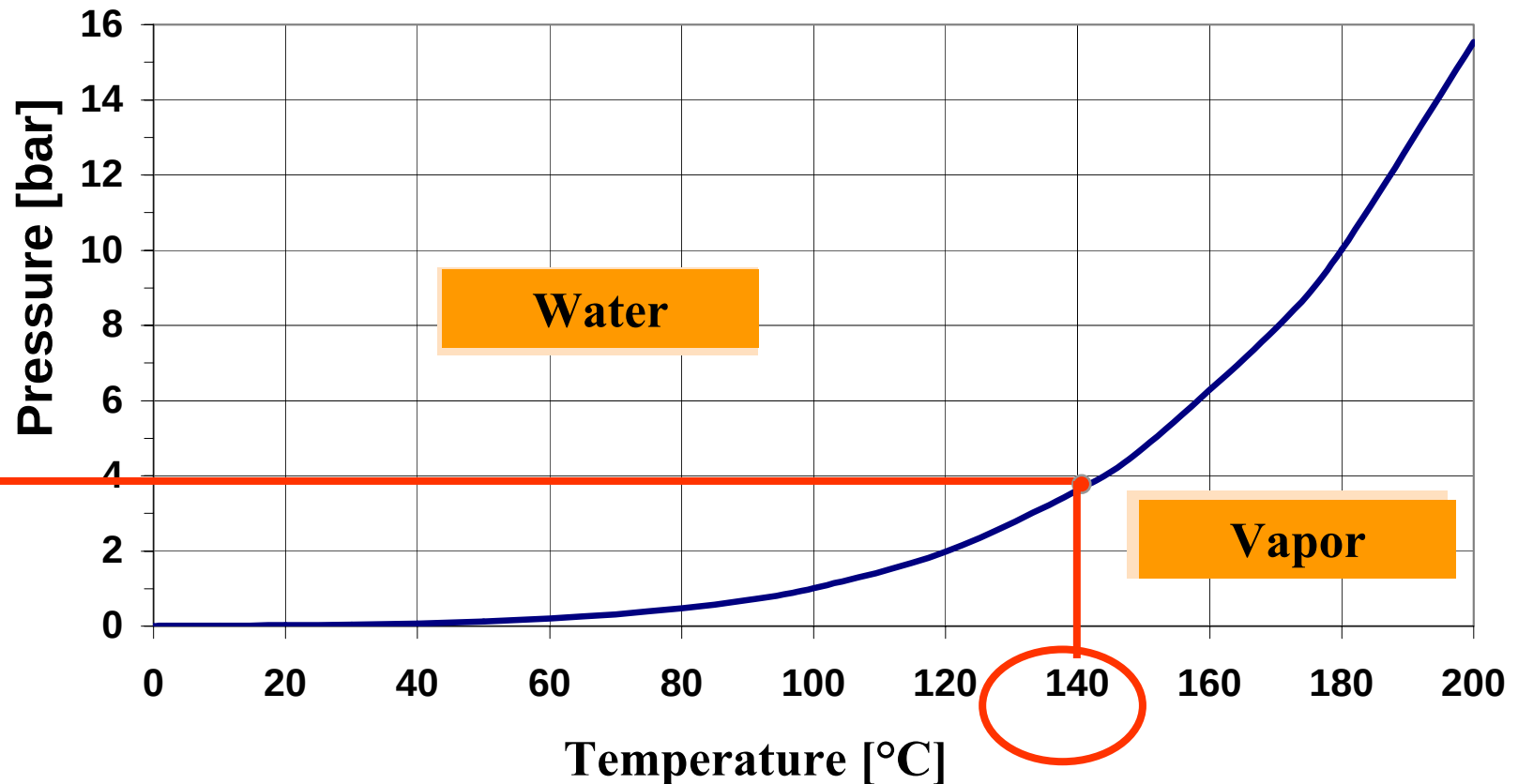


but

Higher vapor pressure



Vapor Pressure Water

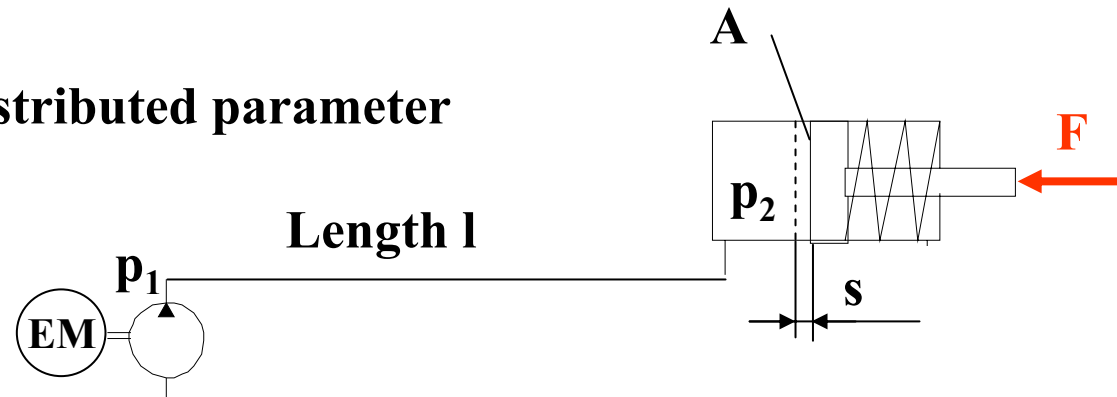


Modeling of transmission lines



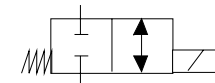
Purpose of the model

Lumped parameter versus distributed parameter



Pressure loss (type of flow)

Transient pressure, $p=f(\text{time})$



Fluid inertia

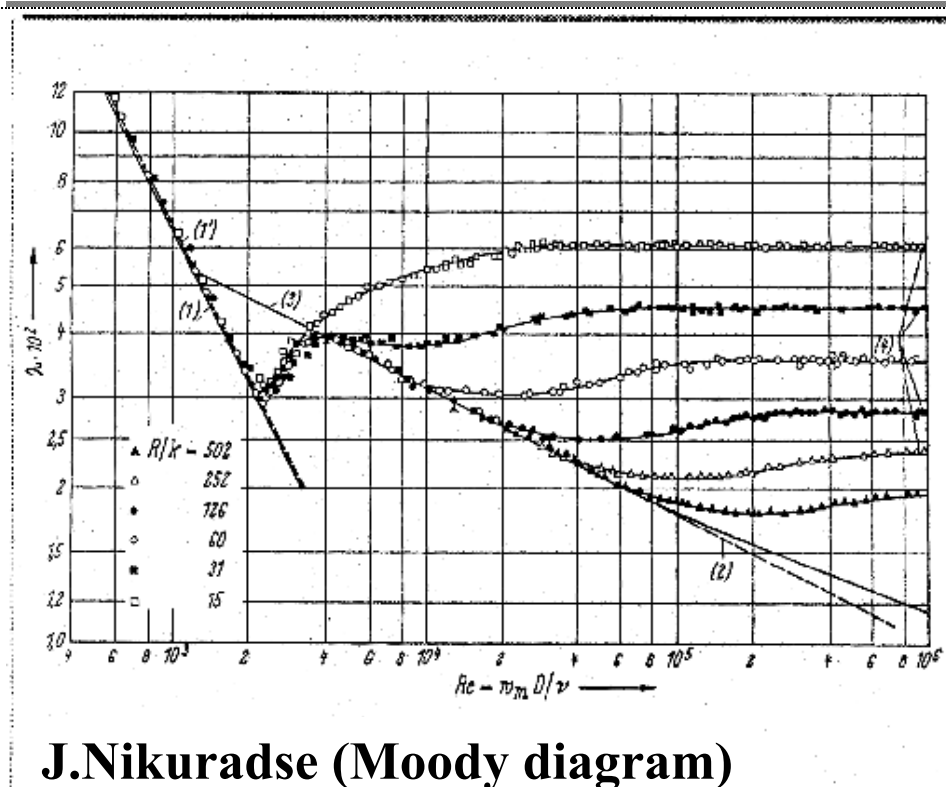
Pressure loss



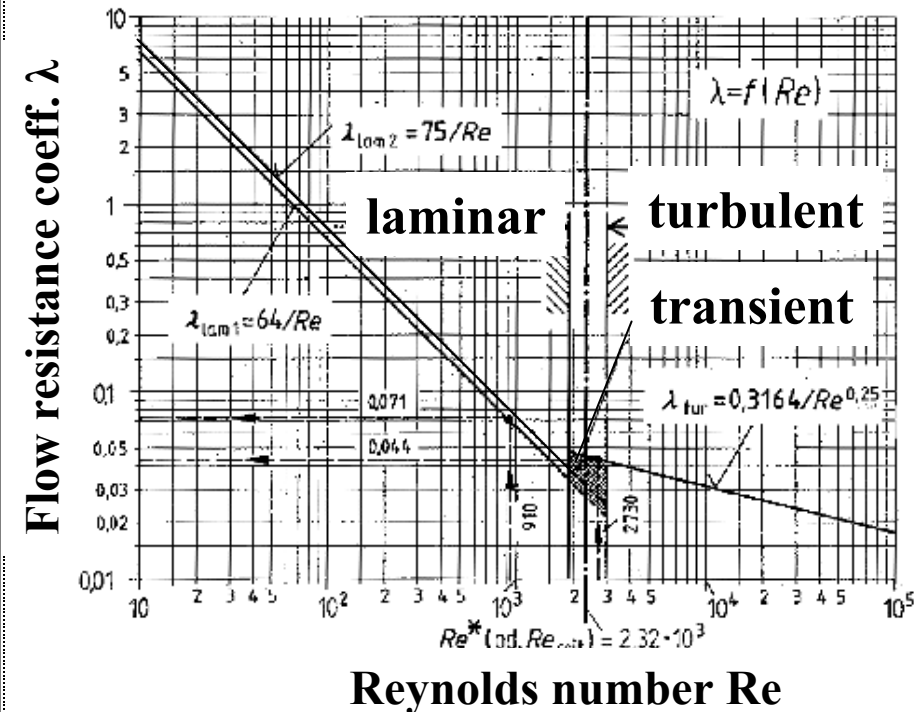
Flow resistance coefficient (friction factor) $\lambda = f(Re)$

@ high Re dependent on surface roughness

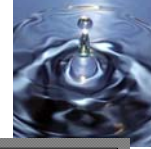
for hydraulically smooth pipes



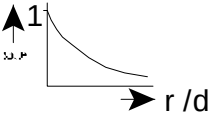
J.Nikuradse (Moody diagram)



Pressure loss



Drag coefficient ξ - experimentally determined

Type	ξ	
Inlet	0,5	
Outlet	1	
Tee	0,5 3 1,3	
Bend		
Seat valve	2.5	
Spool Valve	8 - 16	
Check valve	3 - 10	
Double change of flow direction	1,5 1,8 2,3	

$$\Delta p_F = \sum_{i=1}^k \xi_i \cdot \rho \cdot \frac{v_i^2}{2}$$

Due to change of flow path in fittings, bends, valves



$$\Delta p_S = \Delta p_F + \Delta p_L$$

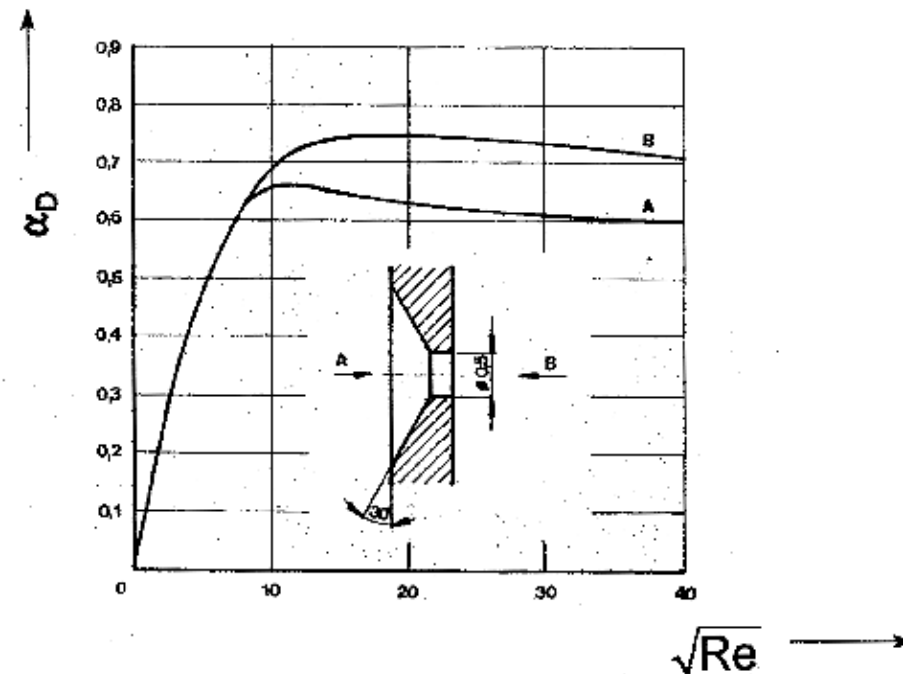
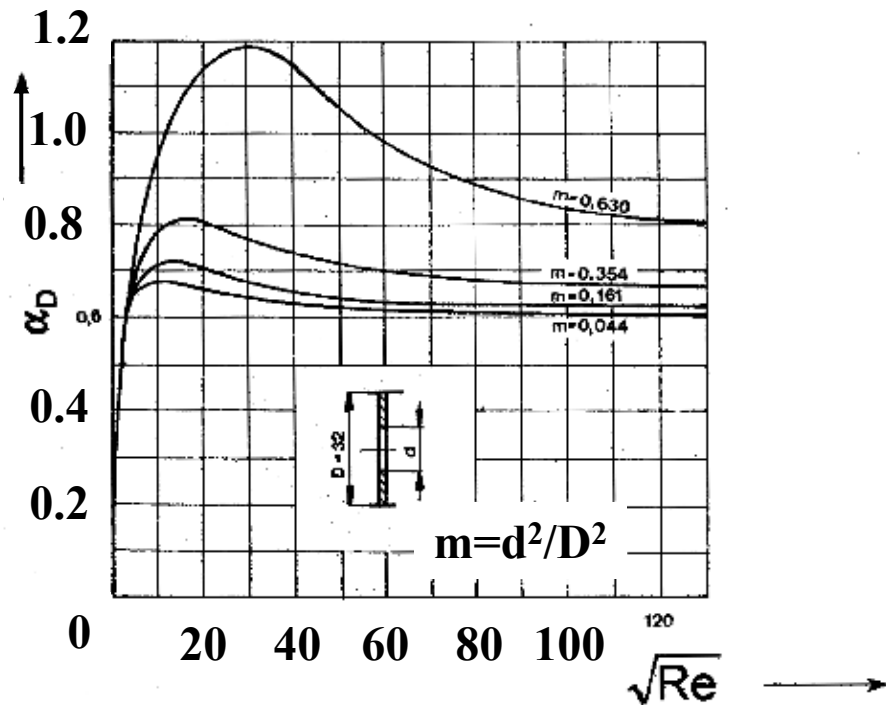
Pressure loss in hydraulic lines (pipes)

$$\Delta p_L = \sum_{j=1}^m \lambda_j \cdot \frac{l_j}{d_j} \cdot \rho \cdot \frac{v_j^2}{2}$$

Orifice Flow



"_D ... Discharge coefficient



Hydraulic Accumulators



Types of hydropneumatic accumulators (gas loaded)

Piston design

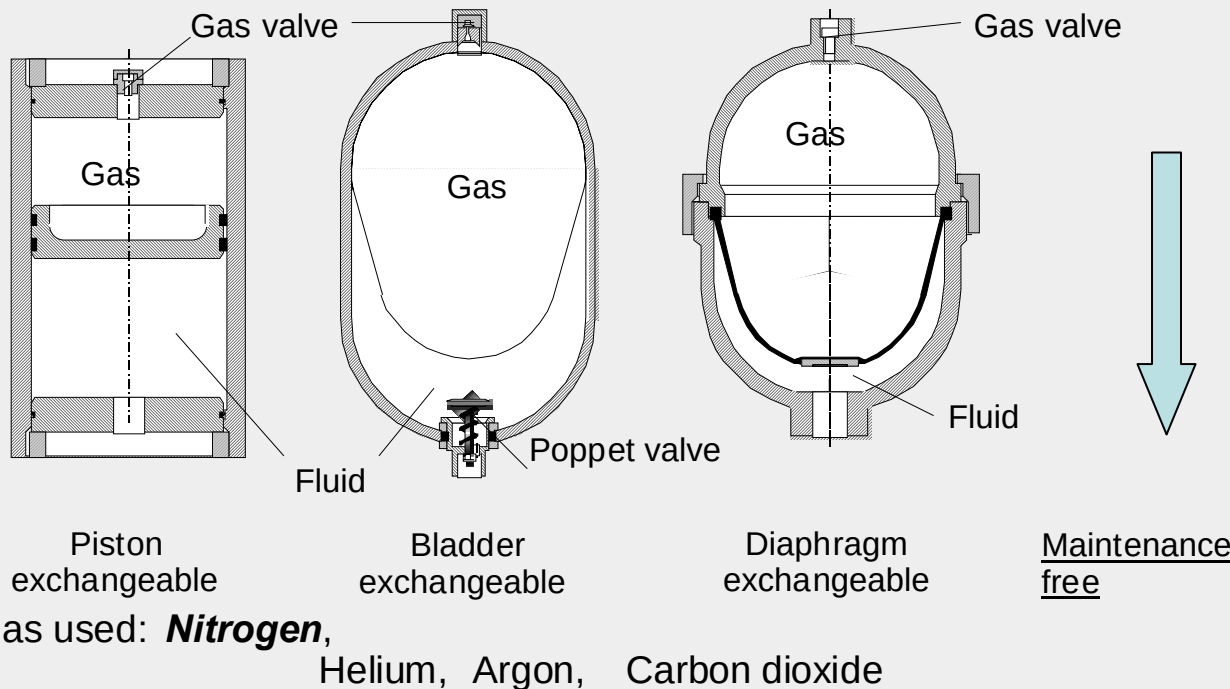
Bladder design

Diaphragm design

Screwed

Welded

Weight loaded



large
uncommon
piston loaded design

Advantage:

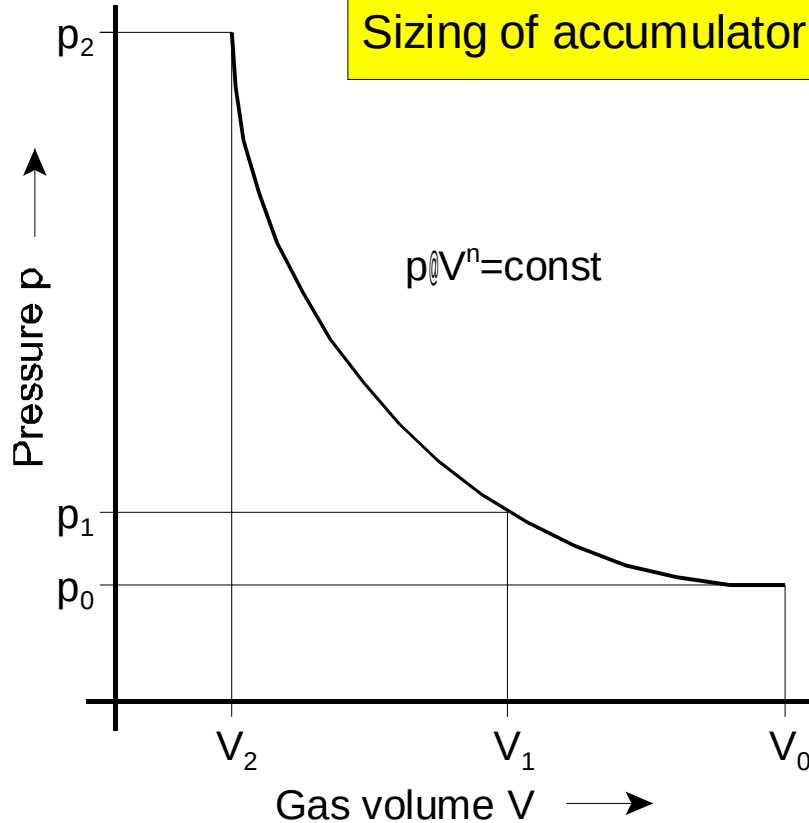
**Maintain fluid
pressure constant**

Hydraulic Accumulators

Gas loaded



Sizing of accumulator & working principle



Thermodynamic process

6 adiabatic $n=1.4$

6 isothermal $n=1$

$$\Delta V = V_0 \left[\left(\frac{p_0}{p_1} \right)^{\frac{1}{n}} - \left(\frac{p_0}{p_2} \right)^{\frac{1}{n}} \right]$$

ΔV ... useable fluid volume

V_0 ... size of the accumulator

p_0 ... precharge gas pressure $p_0 = 0.9 p_1$
 V_0 ... effective gas volume @ p_0