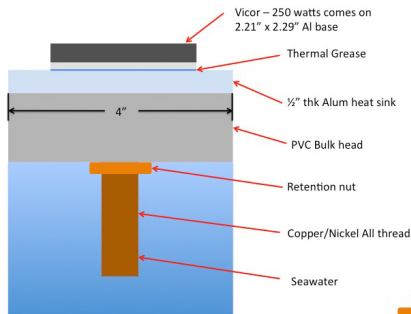
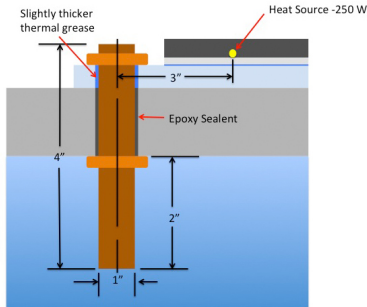


xFOCE Thermal Analysis Spreadsheet



Input values in tan boxes only

250 Watts

Q Heat Flux in BTU / watt-Hr

3.4 BTU : 1 Watt/HR

convertin| 250 * 3.41 = 852.5 BTU/Hr = Q

equation to solve:

$$T_i - T_e = Q \cdot R_t$$

Ti = Temp Internal

Ti = 80 C 176 F

Te = Temp External

Te = 15 C 59 F

$$\Delta T = T_i - T_e$$

$$\Delta T = 176 - 59$$

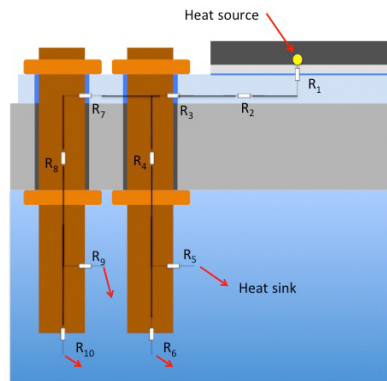
$$\text{Maximum } \Delta T = 117 \text{ F}$$

resistor network calcs:

$$R = L / (k \cdot A) \quad [\text{BTU} / \text{HR F}]^{-1}$$

Assume we will need 2 bolts for securing the internal heat sink.

The image below shows equivalent thermal resistor values for each interface and each material path.



For purposes of general heat transfer calculations we can think of each piece in the path as a resistor and each interface between paths as an additional resistor.

This example shows the assembly with a second parallel path which effectively cuts the resistance to heat transfer in 1/2 from R2 on.

Also, being more accurate we've included the rods ends as a transfer surface

Thermal Transfer Coefficients

$$\text{Thermal Grease} = .381 \frac{\text{BTU}}{\text{Hr Ft}^2 \text{F}}$$

$$\text{Aluminum} = 118.53 \frac{\text{BTU}}{\text{Hr Ft}^2 \text{F}}$$

$$\text{PVC} = 1.02 \frac{\text{BTU}}{\text{Hr Ft}^2 \text{F}}$$

$$\text{Copper Nickel} = 26.0 \frac{\text{BTU}}{\text{Hr Ft}^2 \text{F}}$$

$$\text{Seawater} = .346 \frac{\text{BTU}}{\text{Hr Ft}^2 \text{F}}$$

Resistor Math

Resistors in Series

$$R_{\text{total}} = R_1 + R_2 + R_3 + \dots$$

Two Resistors in Parallel

$$R_t = \frac{R_1 R_2}{R_1 + R_2}$$

$$R_t = \frac{R_1 R_2}{R_2 + R_1}$$

Equal Resistors in Parallel

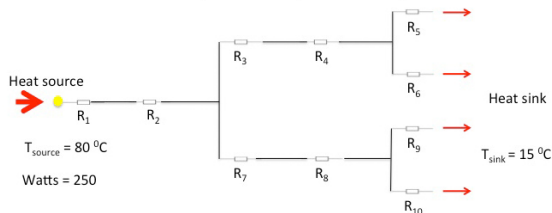
$$R_{\text{total}} = \frac{R}{n}, \text{ Where } n \text{ is the number of resistors}$$

Resistors in Parallel, General Formula

$$R_{\text{total}} = \frac{1}{\frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3} + \dots}$$

Layout of Resistor Network

An easier way to look at the problem for analysis



$$R_5 = R_9 \text{ and } R_6 = R_{10}$$

Area of R5 = exposed length of rod * perimeter in ft²

$$\text{Length of rod in inches} = 3 \text{ inches} \\ = 0.25 \text{ ft}$$

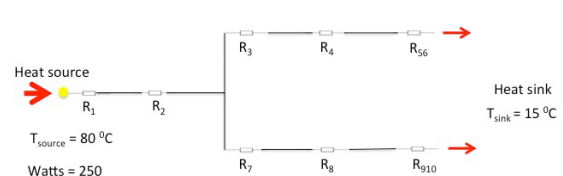
$$\text{Diameter of rod in inches} = 0.5 \text{ inches} \\ \text{perimeter of rod} = 0.1309 \text{ ft}$$

$$R_5 = 0.00736$$

$$\text{Area of rod end} = 0.00136$$

Layout of Resistor Network - 2

Network substitution for analysis



$$R_{56} = (R_5 \cdot R_6) / (R_5 + R_6)$$

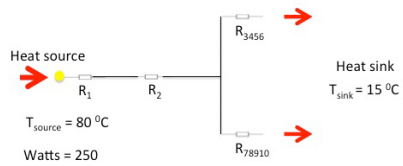
$$R_{910} = (R_9 \cdot R_{10}) / (R_9 + R_{10})$$

These are pushing heat into the water with a
k = .346

$$R_{56} = 0.00707 = R_{910}$$

Layout of Resistor Network - 3

Network substitution cont'd for analysis



$$R_{3456} = R_3 + R_4 + [(R_5 * R_6) / (R_5 + R_6)]$$

$$R_{78910} = R_7 + R_8 + [(R_9 * R_{10}) / (R_9 + R_{10})]$$

$$R6 = 0.17664$$

Continuing on with our reduction refer to diagram Network 3:

Again $R3 = R7$ and $R4 = R8$

These are pushing heat into the copper nick
 $k = 26$

$R4$ is the entire rod length now so it must be longer than the above calculation:

$$\begin{aligned} \text{Length of rod in inches} &= 5 \\ &= 0.4167 \text{ ft} \end{aligned} \quad R4 = 0.1224 = R8$$

$R3$ is a little more involved since it has a surface interface in the aluminum heat sink:

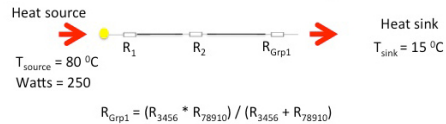
$$\begin{aligned} \text{The heat sink thickness is} &= 0.5 \text{ inches} \quad \text{and the same perimeter as for } R5 \\ &= 0.0417 \text{ ft} \\ \text{assume thermal thickness is .005} \end{aligned} \quad R3 = 0.0029 = R7$$

We further reduce the network of resistors by the formula to the left

$$>>>>> \quad R3456 = 0.1324 = R78910$$

Layout of Resistor Network - 4

Network substitution cont'd for analysis



$$R_{\text{grp1}} = (R_{3456} * R_{78910}) / (R_{3456} + R_{78910})$$

Further reducing the $R3456$ and $R78910$ into an equivalent thermal resistor we get:

$$R_{\text{grp1}} = 0.06622$$

The heat sink is $R2$ and made of Aluminum with a $k = 118.53$

L we will estimate as being slightly longer than half the Vicor and 1/2 the rod diameter ~ 3 inch

$$\begin{aligned} L &= 3 \text{ inches} & A \text{ is the width of the heat sink times the thickness} \\ &= 0.25 \text{ ft} & \text{Width} = 2.5 \text{ inches} &= 0.2083 \text{ ft} \\ & & \text{Thk} = 0.5 \text{ inches} &= 0.0417 \text{ ft} \end{aligned}$$

$$R2 = 0.24298$$

The Vicor base is the area of $R1$ for the calc = 5.0609 sq in 0.0351 Sq ft

We'll say the thermal grease is the limiting thermal coefficient $k = .381$

$$R1 = 0.06249$$

$$R_{\text{total}} = R1 + R2 + R_{\text{grp1}}$$

$$R_{\text{total}} = 0.37169$$

Back to our original equation:

$$\Delta T = Q * R_{\text{t}} = 316.86$$

This must be a positive number to work properly:

$$\Delta T_{\text{Max}} - \Delta T = -199.86 \text{ Red = Bad} \quad \text{Green = Good}$$

$$\text{If we doubled the number of rods again:} \quad R_{\text{new}} = 0.1858$$

$$\Delta T = Q * R_{\text{t}} = 158.43$$

$$\Delta T_{\text{Max}} - \Delta T = -41.43 \text{ Red = Bad} \quad \text{Green = Good}$$

$$\text{now 6 rods: } R_{\text{new}} = 0.0929$$

$$\Delta T = Q * R_{\text{t}} = 79.216$$

$$\Delta T_{\text{Max}} - \Delta T = 37.784 \text{ Red = Bad} \quad \text{Green = Good}$$